

FOUNDATIONS OF SEMANTIC WEB TECHNOLOGIES

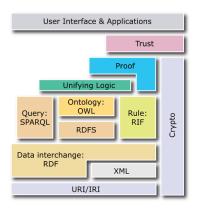
OWL & Description Logics

Sebastian Rudolph



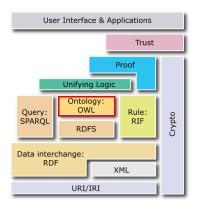


OWL





OWL





Agenda

- Motivation
- Introduction Description Logics
- The Description Logic \mathcal{ALC}
- Extensions of ALC
- Inference Problems



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Description Logics

- description logics (DLs) are one of the current KR paradigms
- · have significantly influenced the standardization of Semantic Web languages
 - OWL is essentially based on DLs
- numerous reasoners

Quonto Owlgres OWLIM Trowl	JFact Pellet Jena HermiT	FaCT++ SHER Oracle Prime condor	RacerPro snorocket QuOnto CB
HOWI			
	ELK	konclude	RScale











OWL Tools

good support by editors

- Protégé, http://protege.stanford.edu
- SWOOP, http://code.google.com/p/swoop/
- OWL Tools, http://owltools.ontoware.org/
- Neon Toolkit, http://neon-toolkit.org/







Description Logics

- origin of DLs: semantic networks and frame-based systems
- downside of the former: only intuitive semantics diverging interpretations
- DLs provide a formal semantics on logical grounds
- can be seen as decidable fragments of first-order logic (FOL), closely related to modal logics
- significant portion of DL-related research devoted to clarifying the computational effort of reasoning tasks in terms of their worst-case complexity
- despite high complexities, even for expressive DLs exist optimized reasoning algorithms with good average case behavior



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DL building blocks

- individuals: birte, cs63.800, sebastian, etc.
 - → constants in FOL, resources in RDF
- concept names: Person, Course, Student, etc.
 - → unary predicates in FOL, classes in RDF
- role names: hasFather, attends, worksWith, etc.
 - → binary predicates in FOL, properties in RDF
 - can be subdivided into abstract and concrete roles (object und data properties)

the set of all individual, concept and role names is called signature or vocabulary



Constituents of a DL Knowledge Base

TBox ${\mathcal T}$

information about concepts and their taxonomic dependencies

ABox $\mathcal A$

informationen about individuals, their concept and role memberships

in more expressive DLs also:

 $\mathsf{RBox}\,\mathcal{R}$

information about roles and their mutual dependencies



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Complex Concepts

 $\mathcal{ALC},$ Attribute Language with Complement, is the simplest DL that is Boolean closed

we define (complex) \mathcal{ALC} concepts as follows:

- every concept name is a concept,
- \top and \bot are concepts,
- for concepts C and D, $\neg C$, $C \sqcap D$, and $C \sqcup D$ are concepts,
- for a role r and a conceptC, $\exists r.C$ and $\forall r.C$ are concepts

Example: $Student \sqcap \forall attends Course. Master Course$ Intuitively: describes the concept comprising all students that attend only master courses



Concept Constructors vs. OWL

- T corresponds to owl: Thing
- ⊥ corresponds to owl: Nothing
- ☐ corresponds to owl:intersectionOf
- ☐ corresponds to owl:unionOf
- ¬ corresponds to owl:complementOf
- ∀ corresponds to owl:allValuesFrom
- \exists corresponds to owl:someValuesFrom



Concept Axioms

For concepts C, D, a general concept inclusion (GCI) axiom has the form

$$C \sqsubseteq D$$

- $C \equiv D$ is an abbreviation for $C \sqsubseteq D$ and $D \sqsubseteq C$
- a TBox (terminological Box) consists of a set of GCIs

 $\mathsf{TBox}\ \mathcal{T}$



ABox

an ALC ABox assertion can be of one of the following forms

- *C*(*a*), called concept assertion
- r(a,b), called role assertion

an ABox consists of a set of ABox assertions

 $\mathsf{ABox}\,\mathcal{A}$

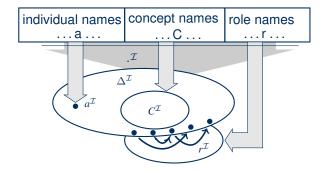


The Description Logic ALC

- ALC is a syntactic variant of the modal logic K
- semantics defined in a model-theoretic way, that is, via interpretations
- can be expressed in first-order predicate logic
- a DL interpretation $\mathcal I$ consists of a domain $\Delta^\mathcal I$ and a function $\cdot^\mathcal I$, that maps
 - individual names a to domain elements $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$
 - concept names C to sets of domain elements $C^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$
 - role names r to sets of pairs of domain elements $r^{\overline{\mathcal{I}}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$



Schematic Representation of an Interpretation





Interpretation of Complex Concepts

the interpretation of complex concepts is defined inductively:

Name	Syntax	Semantics
top	Τ	$\Delta^{\mathcal{I}}$
bottom	1	Ø
negation	$\neg C$	$\Delta^{\mathcal{I}} \setminus C^{\mathcal{I}}$
conjunction	$C \sqcap D$	$C^{\mathcal{I}} \cap D^{\mathcal{I}}$
disjunction	$C \sqcup D$	$C^{\mathcal{I}} \cup D^{\mathcal{I}}$
universal quantifier	$\forall r.C$	$\{x \in \Delta^{\mathcal{I}} \mid (x, y) \in r^{\mathcal{I}} \text{ implies } y \in C^{\mathcal{I}}\}$
existential quantifier	$\exists r.C$	$\{x \in \Delta^{\mathcal{I}} \mid \text{there is some } y \in \Delta^{\mathcal{I}}, \text{ such that } \}$
		$(x,y) \in r^{\mathcal{I}} \text{ and } y \in C^{\mathcal{I}} $



Interpretation of Axioms

interpretation can be extended to axioms:

name	syntax	semantic	notation
			$\mathcal{I} \models C \sqsubseteq D$
equivalence	$C \equiv D$	holds if $C^{\mathcal{I}} = D^{\mathcal{I}}$	$\mathcal{I} \models C \equiv D$
concept assertion	C(a)	holds if $a^{\mathcal{I}} \in C^{\mathcal{I}}$	$\mathcal{I} \models C(a)$
role assertion	r(a,b)	holds if $(a^{\mathcal{I}}, b^{\mathcal{I}}) \in r^{\mathcal{I}}$	$\mathcal{I} \models r(a,b)$



Logical Entailment in Knowledge Bases

- Let $\mathcal I$ be an interpretation, $\mathcal T$ a TBox, $\mathcal A$ an Abox and $\mathcal K=(\mathcal T,\mathcal A)$ a knowledge base
- \mathcal{I} is a model for \mathcal{T} , if $\mathcal{I} \models$ ax for every axiom ax in \mathcal{T} , written $\mathcal{I} \models \mathcal{T}$
- \mathcal{I} is a model for \mathcal{A} , if $\mathcal{I} \models$ ax for every assertion ax in \mathcal{A} , written $\mathcal{I} \models \mathcal{A}$
- \mathcal{I} is a model for \mathcal{K} , if $\mathcal{I} \models \mathcal{T}$ and $\mathcal{I} \models \mathcal{A}$
- An axiom ax follows from K, written K |= ax, if every model I of K is also a model of ax.



translation of TBox axioms into first-order predicate logics through the mapping π with C,D complex classes, r a role and A an atomic class:

$$\pi(C \sqsubseteq D) = \forall x.(\pi_x(C) \to \pi_x(D)) \qquad \pi(C \equiv D) = \forall x.(\pi_x(C) \leftrightarrow \pi_x(D))$$



translation of TBox axioms into first-order predicate logics through the mapping π with C,D complex classes, r a role and A an atomic class:

$$\pi(C \sqsubseteq D) = \forall x. (\pi_x(C) \to \pi_x(D)) \qquad \pi(C \equiv D) = \forall x. (\pi_x(C) \leftrightarrow \pi_x(D))$$

$$\pi_x(A) = A(x)$$

$$\pi_x(\neg C) = \neg \pi_x(C)$$

$$\pi_x(C \sqcap D) = \pi_x(C) \land \pi_x(D)$$

$$\pi_x(C \sqcup D) = \pi_x(C) \lor \pi_x(D)$$

$$\pi_x(\forall r. C) = \forall y. (r(x, y) \to \pi_y(C))$$

$$\pi_x(\exists r. C) = \exists y. (r(x, y) \land \pi_y(C))$$



translation of TBox axioms into first-order predicate logics through the mapping π with C,D complex classes, r a role and A an atomic class:

$$\pi(C \sqsubseteq D) = \forall x.(\pi_x(C) \to \pi_x(D)) \qquad \pi(C \equiv D) = \forall x.(\pi_x(C) \leftrightarrow \pi_x(D))$$

$$\pi_x(A) = A(x) \qquad \qquad \pi_y(A) = A(y)$$

$$\pi_x(\neg C) = \neg \pi_x(C) \qquad \qquad \pi_y(\neg C) = \neg \pi_y(C)$$

$$\pi_x(C \sqcap D) = \pi_x(C) \land \pi_x(D) \qquad \qquad \pi_y(C \sqcap D) = \pi_y(C) \land \pi_y(D)$$

$$\pi_x(C \sqcup D) = \pi_x(C) \lor \pi_x(D) \qquad \qquad \pi_y(C \sqcup D) = \pi_y(C) \lor \pi_y(D)$$

$$\pi_x(\forall r.C) = \forall y.(r(x, y) \to \pi_y(C)) \qquad \qquad \pi_y(\forall r.C) = \forall x.(r(y, x) \to \pi_x(C))$$

$$\pi_x(\exists r.C) = \exists y.(r(x, y) \land \pi_y(C)) \qquad \qquad \pi_y(\exists r.C) = \exists x.(r(y, x) \land \pi_x(C))$$



- translation only requires two variables
- \leadsto \mathcal{ALC} is a fragment of FOL with two variables \mathcal{L}_2
- \leadsto satisfiability checking of sets of \mathcal{ALC} axioms is decidable



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Inverse Roles

- a role can be
 - a role name r or
 - an inverse role r⁻
- the semantics of inverse roles is defined as follows:

$$(r^{-})^{\mathcal{I}} = \{(y, x) \mid (x, y) \in r^{\mathcal{I}}\}\$$

- ullet the extension of \mathcal{ALC} by inverse roles is denoted as \mathcal{ALCI}
- corresponds to owl:inverseOf



Parts of a Knowledge Base

 $\mathsf{TBox}\ \mathcal{T}$

information about concepts and their taxonomic dependencies

 $\mathsf{ABox}\ \mathcal{A}$

information about individuals, their concepts and role connections

in more expressive DLs also:

 $\mathsf{RBox}\ \mathcal{R}$

information about roles and their mutual dependencies



Role Axioms

- for r, s roles, a role inclusion axiom RIA has the form $r \sqsubseteq s$
- $r \equiv s$ is the abbreviation for $r \sqsubseteq s$ and $s \sqsubseteq r$
- an RBox (role box) or role hierarchy consists of a set of role axioms
- $r \sqsubseteq s$ holds in an interpretation \mathcal{I} if $r^{\mathcal{I}} \subseteq s^{\mathcal{I}}$, written $\mathcal{I} \models r \sqsubseteq s$
- the extension of ALC by role hierarchies is denoted with ALCH, if we also have inverse roles: ALCHI
- corresponds to owl:subPropertyOf

 $\mathsf{RBox}\,\mathcal{R}$



An Example Knowledge Base

```
\mathsf{RBox}\,\mathcal{R}
            own ⊑ careFor
TBox \mathcal{T}
       Healthy □ ¬ Dead
            Cat ☐ Dead ☐ Alive
HappyCatOwner ☐ ∃owns.Cat □ ∀caresFor.Healthy
ABox A
  HappyCatOwner (schrödinger)
```



An Example Knowledge Base

```
\mathsf{RBox}\,\mathcal{R}
            own □ careFor
"If somebody owns something, they care for it."
TBox T
       Healthy □ ¬ Dead
"Healthy beings are not dead."
            Cat □ Dead □ Alive
"Every cat is dead or alive."
HappyCatOwner □ ∃owns.Cat □ ∀caresFor.Healthy
"A happy cat owner owns a cat and everything he cares for is healthy."
ABox A
  HappyCatOwner (schrödinger)
"Schrödinger is a happy cat owner."
```



Role Transitivity

- for r a role, a transitivity axiom has the form Trans(r)
- Trans(r) holds in an interpretation $\mathcal I$ if $r^{\mathcal I}$ is a transitive relation, i.e., $(x,y)\in r^{\mathcal I}$ and $(y,z)\in r^{\mathcal I}$ imply $(x,z)\in r^{\mathcal I}$, written $\mathcal I\models \operatorname{Trans}(r)$
- the extension of ALC by transitivity axioms is denoted by S (after the modal logic S₅)
- corresponds to owl: TransitiveProperty



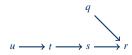
Role Functionality

- for r a role, a functionality axiom has the form Func(r)
- Func(r) holds in an interpretation $\mathcal I$ if $(x,y_1) \in r^{\mathcal I}$ and $(x,y_2) \in r^{\mathcal I}$ imply $y_1 = y_2$, written $\mathcal I \models \mathsf{Func}(r)$
- translation into FOL requires equality (=)
- the extension of \mathcal{ALC} by functionality axioms is denoted by \mathcal{ALCF}
- corresponds to owl:FunctionalProperty



Simple and Non-Simple Roles

- given a role hierarchy R, we let ≛R denote the reflexive and transitive closure w.r.t. □
- for a role hierarchy $\mathcal R$, we can distinguish the roles in $\mathcal R$ into simple and non-simple roles
- a role r is non-simple w.r.t. \mathcal{R} , if there is a role t such that $\operatorname{Trans}(t) \in \mathcal{R}$ and $t \, \overset{\leftarrow}{\sqsubset}_{\mathcal{R}} r$ holds
- all other roles are are simple
- Example: $\mathcal{R} = \{u \sqsubseteq t, t \sqsubseteq s, s \sqsubseteq r, q \sqsubseteq r, \text{Trans}(t)\}$

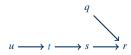


non-simple:



Simple and Non-Simple Roles

- given a role hierarchy R, we let ER denote the reflexive and transitive closure w.r.t.
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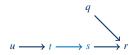


non-simple: t



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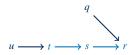


non-simple: t, s



Simple and Non-Simple Roles

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- a role r is non-simple w.r.t. \mathcal{R} , if there is a role t such that $\operatorname{Trans}(t) \in \mathcal{R}$ and $t \not\sqsubseteq_{\mathcal{R}} r$ holds
- all other roles are are simple
- Example: $\mathcal{R} = \{u \sqsubseteq t, t \sqsubseteq s, s \sqsubseteq r, q \sqsubseteq r, \text{Trans}(t)\}$

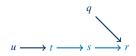


non-simple: t, s, r



Simple and Non-Simple Roles

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- all other roles are are simple
- Example: $\mathcal{R} = \{u \sqsubseteq t, t \sqsubseteq s, s \sqsubseteq r, q \sqsubseteq r, \text{Trans}(t)\}$



non-simple: t, s, r simple: q, u



(Unqualified) Number Restrictions

- for a simple roe s and a natural number n, ≤ n s, ≥ n s and = n s are concepts
- the semantics is defined by:

$$(\leqslant n s)^{\mathcal{I}} = \{x \in \Delta^{\mathcal{I}} \mid \#\{y \in \Delta^{\mathcal{I}} \mid (x, y) \in s^{\mathcal{I}}\} \le n\}$$
$$(\geqslant n s)^{\mathcal{I}} = \{x \in \Delta^{\mathcal{I}} \mid \#\{y \in \Delta^{\mathcal{I}} \mid (x, y) \in s^{\mathcal{I}}\} \ge n\}$$
$$(= n s)^{\mathcal{I}} = \{x \in \Delta^{\mathcal{I}} \mid \#\{y \in \Delta^{\mathcal{I}} \mid (x, y) \in s^{\mathcal{I}}\} = n\}$$

- \bullet the extension of \mathcal{ALC} by (unqualified) number restrictions is denoted by \mathcal{ALCN}
- correspond to owl:maxCardinality, owl:minCardinality, and owl:cardinality
- restriction to simple roles ensures decidability e.g. for checking knowledge base satisfiability
- definition of TBox requires an RBox being already defined



(Unqualified) Number Restrictions in FOL

- translation into FOL requires equality or counting quantifiers
- translation defined as follows (likewise for π_y):

$$\pi_x(\leqslant n \, s) = \exists^{\leqslant n} y.(s(x, y))$$

$$\pi_x(\geqslant n \, s) = \exists^{\geqslant n} y.(s(x, y))$$

$$\pi_x(=n \, s) = \exists^{\leqslant n} y.(s(x, y)) \land \exists^{\geqslant n} y.(s(x, y))$$

• the following equivalences hold:

$$\neg (\leqslant n \, s) = \geqslant n + 1 \, s \qquad \qquad \neg (\geqslant n \, s) = \leqslant n - 1 \, s, \quad n \ge 1$$

$$\neg (\geqslant 0 \, s) = \bot \qquad \qquad \geqslant 1 \, s = \exists s. \, \top$$

$$\leqslant 0 \, s = \forall s. \bot \qquad \qquad \top \sqsubseteq \leqslant 1 s = \mathsf{Func}(s)$$



Nominals or Closed Classes

- defines a class by complete enumeration of its instances
- for a_1, \ldots, a_n individuals, $\{a_1, \ldots, a_n\}$ is a concept
- semantics defined as follows:

DL:
$$(\{a_1, \dots, a_n\})^{\mathcal{I}} = \{a_1^{\mathcal{I}}, \dots, a_n^{\mathcal{I}}\}$$

FOL: $\pi_x(\{a_1, \dots, a_n\}) = (x = a_1 \vee \dots \vee x = a_n)$

- extension of ALC by nominals denoted as ALCO
- corresponds to owl:oneOf



Nominals for Encoding Further OWL Constructors

• owl:hasValue "forces" role to a certain individual

in description logic:

Woman ≡ ∃hasGender.{female}



Further Kinds of ABox Assertions

an ABox assertion can have one of the following forms

- *C*(*a*) (concept assertion)
- r(a,b) (role assertion)
- $\neg r(a,b)$ (negative role assertion)
- $a \approx b$ (equality assertion)
- $a \not\approx b$ (inequality assertion)



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Internalization of ABox Assertions

if nominals are supported, every knowledge base with an ABox can be transformed into an equivalent KB without ABox:

$$C(a) = \{a\} \sqsubseteq C$$

$$r(a,b) = \{a\} \sqsubseteq \exists r.\{b\}$$

$$\neg r(a,b) = \{a\} \sqsubseteq \forall r.(\neg\{b\})$$

$$a \approx b = \{a\} \equiv \{b\}$$

$$a \not\approx b = \{a\} \sqsubseteq \neg\{b\}$$



Overview Nomenclature

- ALC Attribute Language with Complement
 - S ALC + role transitivity
 - \mathcal{H} subroles
 - O closed classes
 - \mathcal{I} inverse roles
 - ${\cal N}$ (unqualified) number restrictions
 - (D) datatypes
 - \mathcal{F} functional roles

OWL DL is $\mathcal{SHOIN}(D)$ and OWL Lite is $\mathcal{SHIF}(D)$



Different Terms in DLs and in OWL

OWL DL class concept role

property object property abstract role data property concrete role oneOf nominal

ontology knowledge base TBox, RBox, ABox



Example: A More Complex Knowledge Base

```
Human 

☐ Animal 
☐ Biped
             \{President\_Obama\} \equiv \{Barack\_Obama\}
           \{\text{john}\} \sqsubseteq \neg\{\text{peter}\}
      hasChild = hasParent
             cost ≡ price
            Trans(ancestor)
             Func(hasMother)
             Func(hasSSN<sup>-</sup>)
```



OWA Open World Assumption

- the existence of further individuals is possible, if they are not explicitly excluded
- OWL uses the OWA

CWA Closed World Assumption

 it is assumed that the knowledge base contains all individuals and facts



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CWA Closed World Assumption

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if we know

no idea

	Are all of Bill's children male?	if we assume not to know everything about Bill	everything then all of Bill's children are male
child(bill, bob) Man(bob)	⊨? (∀ child.Man)(bill)	DL answers	Prolog
$(\leqslant 1 \text{ child})(\text{bill})$	$\models^? (\forall \text{ child.Man)(bill)}$		



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$(\leqslant 1 \text{ child})(\text{bill})$	$\models^? (\forall \text{ child.Man)(bill)}$	yes	yes



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Important Inference Problems for a Knowledge Base $\mathcal K$

- global consistency of the knowledge base: $\mathcal{K} \models$? false? $\mathcal{K} \models$? $\top \sqsubseteq \bot$?
 - Is the knowledge base "plausible"?
- class consistency: $\mathcal{K} \models^? C \sqsubseteq \bot$?
 - Is the class C necessarily empty?
- class inclusion (subsumption): $\mathcal{K} \models^? C \sqsubseteq D$?
 - taxonomic structure of the knowledge base
- class equivalence: $\mathcal{K} \models^? C \equiv D$?
 - Do two classes comprise the same individual sets?
- class disjointness: $\mathcal{K} \models^? C \sqcap D \sqsubseteq \bot$?
 - Are two classes disjoint?
- class membership: $\mathcal{K} \models^? C(a)$?
 - Is the individual a contained in class C?
- instance retrieval: find all x with $\mathcal{K} \models C(x)$
 - Find all (known!) members of the class C.



Decidability of OWL DL

- decidability means that there is a terminating algorithm for all the aforementioned inference problems
- OWL DL is a fragment of FOL, thus FOL inference procedures could be used in principle(Resolution, Tableaux)
 - but these are not guaranteed to terminate!
- problem: find algorithms that are guaranteed to terminate
- no "naive" solutions for this



OWL 2: Outlook

- OWL 2 extends the fragments introduced here by further constructors
- OWL 2 also defines simpler fragments (PTime for standard inferencing problems)
- diverse tools for automated inferencing
- editors support creation of ontologies / knowledge bases