



# SEMINAR ABSTRACT ARGUMENTATION

## Implementing Abstract Argumentation Frameworks

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# Outline

- Direct- vs. Reduction-based Approach
- Propositional Logic
- Answer-Set Programming
- ASP Encodings of AF Semantics

# Motivation

- **Argumentation Frameworks** provide a formalism for a compact **representation** and **evaluation** of such scenarios.
- More complex semantics, especially in combination with an increasing amount of data, requires an **automated computation** of such solutions.
- Most of these problems are **intractable**, so implementing dedicated systems from the scratch is not the best idea.
- Distinction between **direct implementation** and **reduction-based approach**.
- We focus on reductions to **propositional logic** and **Answer-Set Programming (ASP)**.

# Laziness and Implementations

## Alternative 1: **The Japanese way**

- Implement a separate algorithm for each reasoning task
- Implementation is complicated because most reasoning tasks are inherently intricate (→ the complexity results given before)
- Implementation, testing, etc. require much effort and time

# Laziness and Implementations

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## Alternative : **The southern way**

- Life is short; try to keep your effort as small as possible
- Let others work for you and use their results and software
- Be smart; apply what you have learned

# The rapid implementation approach (RIA)

## We know:

- Any complete problem can be translated into any other complete problem of the same complexity class
- Moreover, there exists poly-time translations (reductions)
- Complexity results (incl. completeness) for many reasoning tasks

## We used already:

- e.g., the PTIME reduction from a CNF  $\varphi$  to an AF  $F(\varphi)$  such that  $\varphi$  is satisfiable iff  $F(\varphi)$  has an admissible set containing  $\varphi$
- Can we “reverse” the reduction, i.e., from AFs to formulas?
- YES! Reduce to formalisms for which “good” solvers are available  
❗ But we have to find the PTIME reduction!

## The rapid implementation approach (2)

- Reduce reasoning tasks for AF, e.g., to SAT problems of (Q)BFs
- Reductions are “cheap” (wrt runtime and implementation effort!)
- Good SAT and QSAT solvers are available; simply use them

### Benefits:

- Reductions are much easier to implement than full-fledged algorithms especially for “hard” reasoning tasks
- Basic reductions can be combined and reused
- Different formalisms can be reduced to same target formalism
  - ➔ beneficial for comparative studies

# The rapid implementation approach (3)

## Target formalisms are:

- The SAT problem for propositional formulas
- The SAT problem for quantified Boolean formulas
- Answer-set programs

Tools are available to solve all these three formalisms

Many developers are happy to give away their tool

They work hard to improve the tool's performance (for you!)



# Required properties of reductions:

## Faithfulness

- Let  $\Pi$  be a decision problem
- $F_{\Pi}(\cdot)$  a reduction to a target formalism
- $F_{\Pi}(\cdot)$  has to satisfy the following three conditions:
  - 1  $F_{\Pi}(\cdot)$  is **faithful**, i.e.,  $F_{\Pi}(K)$  is true iff  $K$  is a yes-instance of  $\Pi$
  - 2 For each instance  $K$ ,  $F_{\Pi}(K)$  is poly-time computable wrt size of  $K$
  - 3 Determining the truth of  $F_{\Pi}(K)$  is computationally not harder than deciding  $\Pi$

Faithfulness guarantees a correct “simulation” of  $K$

# Reductions to Propositional Logic

Given an AF  $F = (A, R)$ , for each  $a \in A$  a propositional variable  $v_a$  is constructed.

- $S \subseteq A$  is a  $\sigma$  extension of  $F$  iff  $\{v_a \mid a \in S\} \models \varphi$ ,
- with  $\varphi$  a propositional formula that evaluates  $F$  under semantics  $\sigma$ .

## Admissible Sets

$$adm_{A,R} := \bigwedge_{a \in A} ((v_a \rightarrow \bigwedge_{(b,a) \in R} \neg v_b) \wedge (v_a \rightarrow \bigwedge_{(b,a) \in R} (\bigvee_{(c,b) \in R} v_c)))$$

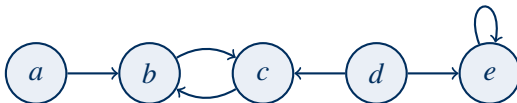
Models of  $adm_{A,R}$  correspond to admissible sets of  $F$  [Besnard & Doutre 04].

# Reductions to Propositional Logic ctd.

## Admissible Sets

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## Example



$$adm_{A,R} = ((v_a \rightarrow \top) \wedge (v_b \rightarrow (\neg v_a \wedge \neg v_c))) \wedge (v_c \rightarrow (\neg v_b \wedge \neg v_d)) \wedge (v_d \rightarrow \top) \wedge (v_e \rightarrow (\neg v_d \wedge \neg v_e)) \wedge ((v_a \rightarrow \top) \wedge (v_b \rightarrow (\perp \wedge (v_b \vee v_d)))) \wedge (v_c \rightarrow ((v_a \vee v_c) \wedge \perp)) \wedge (v_d \rightarrow \top) \wedge (v_e \rightarrow (\perp \wedge v_d))$$

# General Idea of Answer-Set Programming

## Fundamental concept:

- **Models** = set of atoms
- **Models**, not proofs, **represent solutions!**
- Need techniques to **compute models** (not to compute proofs)
- ➔ Methodology to solve **search problems**

## Solving search problems with ASP

- Given a problem  $\Pi$  and an instance  $K$ , reduce it to the problem of computing intended models of a logic program:
  - 1 Encode  $(\Pi, K)$  as a logic program  $P$  such that the solutions of  $\Pi$  for the instance  $K$  are represented by the intended models of  $P$
  - 2 Compute one intended model  $M$  (an "answer set") of  $P$
  - 3 Reconstruct a solution for  $K$  from  $M$
- Variant: Compute all intended models to obtain all solutions

# ASP Solvers

## Efficient solvers available

- `gringo/clasp` (University of Potsdam)
- `dlv` (TU Wien, University of Calabria)
- `smodels`, `GnT` (Aalto University, Finland)
- `ASSAT` (Hong Kong University of Science and Technology)

# Answer-Set Programming Syntax

- We assume a first-order vocabulary  $\Sigma$  comprised of nonempty finite sets of **constants**, **variables**, and **predicate symbols**, but **no function symbols**
- A **term** is either a variable or a constant
- An **atom** is an expression of form  $p(t_1, \dots, t_n)$ , where
  - $p$  is a predicate symbol of arity  $n \geq 0$  from  $\Sigma$ , and
  - $t_1, \dots, t_n$  are terms
- A **literal** is an atom  $p$  or a negated atom  $\neg p$ 
  - $\neg$  is called **strong negation**, or **classical negation**
- A literal is **ground** if it contains no variable.

## ASP Syntax

A rule  $r$  is an expression of the form

$$a_1 \vee \cdots \vee a_n \leftarrow b_1, \dots, b_k, \text{ not } b_{k+1}, \dots, \text{ not } b_m,$$

with  $n \geq 0$ ,  $m \geq k \geq 0$ ,  $n + m > 0$ , where  $a_1, \dots, a_n, b_1, \dots, b_m$  are atoms, and “not” stands for **default negation**.

We call

- $H(r) = \{a_1, \dots, a_n\}$  the **head** of  $r$ ;
- $B(r) = \{b_1, \dots, b_k, \text{ not } b_{k+1}, \dots, \text{ not } b_m\}$  the **body** of  $r$ ;
- $B^+(r) = \{b_1, \dots, b_k\}$  the **positive body** of  $r$ ;
- $B^-(r) = \{b_{k+1}, \dots, b_m\}$  the **negative body** of  $r$ .
- Intuitive meaning of  $r$ : if  $b_1, \dots, b_k$  are derivable, but  $b_{k+1}, \dots, b_m$  are **not** derivable, then one of  $a_1, \dots, a_n$  is asserted
- A **program** is a finite set of rules

# Answer-Set Programming Syntax ctd.

A rule  $a_1 \vee \dots \vee a_n \leftarrow b_1, \dots, b_k, \text{ not } b_{k+1}, \dots, \text{ not } b_m$  is

- a **fact** if  $m = 0$  and  $n \geq 1$
- a **constraint** if  $n = 0$  (i.e., the head is empty)
- **basic** if  $m = k$  and  $n \geq 1$
- **non-disjunctive** if  $n = 1$
- **normal** if it is non-disjunctive and contains no strong negation  $\neg$
- **Horn** if it is normal and basic
- **ground** if all its literals are ground

A program is basic, normal, etc., if all of its rules are



# ASP Semantics

- An interpretation  $I$  satisfies a ground rule  $r$  iff  $H(r) \cap I \neq \emptyset$  whenever
  - $B^+(r) \subseteq I$ ,
  - $B^-(r) \cap I = \emptyset$ .
- $I$  satisfies a ground program  $\pi$ , if each  $r \in \pi$  is satisfied by  $I$ .
- A non-ground rule  $r$  (resp., a program  $\pi$ ) is satisfied by an interpretation  $I$  iff  $I$  satisfies all groundings of  $r$  (resp.,  $Gr(\pi)$ ).

## Gelfond-Lifschitz reduct

An interpretation  $I$  is an **answer set** of  $\pi$  iff it is a subset-minimal set satisfying

$$\pi^I = \{H(r) \leftarrow B^+(r) \mid I \cap B^-(r) = \emptyset, r \in Gr(\pi)\}.$$

# Programming methodology

## Simplest technique: Guess and check

- **Guess:** Generate candidates for answer sets in the first step
- **Check:** Filter the answer sets and delete undesirable ones

### Example (Graph coloring)

```
node(a).node(b).node(c).edge(a, b).edge(b, c).           }facts
col(red, X) ∨ col(green, X) ∨ col(blue, X) ← node(X).     }guess
← edge(X, Y), col(C, X), col(C, Y).                       }check
```

- G:** Generate all possible coloring candidates
- C:** Delete all candidates where adjacent nodes have same color

# Corresponding Complexity Results

## Complexity of Argumentation

	<i>adm</i>	<i>pref</i>	<i>semi</i>	<i>stage</i>	<i>grd*</i>
Cred	NP-c	NP-c	$\Sigma_2^P$ -c	$\Sigma_2^P$ -c	NP-c
Skept	(trivial)	$\Pi_2^P$ -c	$\Pi_2^P$ -c	$\Pi_2^P$ -c	co-NP-c

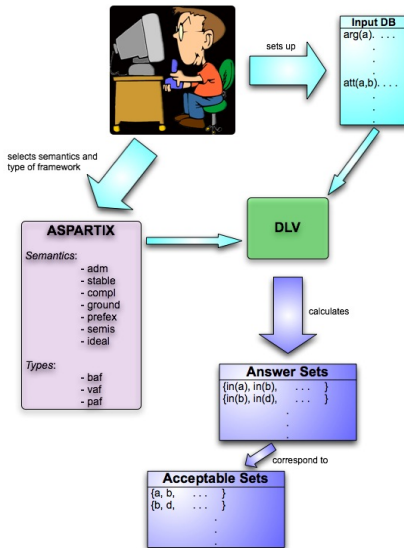
[Baroni et al. 11; Dimopoulos & Torres 96; Dunne & Bench-Capon 02; Dvořák & Woltran 10]

## Recall: Data-Complexity of Datalog

	normal programs	disjunctive program	optimization programs
$\models_c$	NP	$\Sigma_2^P$	$\Sigma_2^P$
$\models_s$	co-NP	$\Pi_2^P$	$\Pi_2^P$

[Dantsin, Eiter, Gottlob, Voronkov 01]

# ASPARTIX - System Description



# ASP Encodings

## Conflict-free Set

Given an AF  $(A, R)$ .

A set  $S \subseteq A$  is **conflict-free** in  $F$ , if, for each  $a, b \in S$ ,  $(a, b) \notin R$ .

## Encoding for $F = (A, R)$

$$\widehat{F} = \{\text{arg}(a) \mid a \in A\} \cup \{\text{att}(a, b) \mid (a, b) \in R\}$$

$$\pi_{cf} = \left\{ \begin{array}{ll} \text{in}(X) & \leftarrow \text{not out}(X), \text{arg}(X) \\ \text{out}(X) & \leftarrow \text{not in}(X), \text{arg}(X) \\ & \leftarrow \text{in}(X), \text{in}(Y), \text{att}(X, Y) \end{array} \right\}$$

**Result:** For each AF  $F$ ,  $cf(F) \equiv \mathcal{AS}(\pi_{cf}(\widehat{F}))$

# ASP Encodings cont.

## Admissible Sets

Given an AF  $F = (A, R)$ . A set  $S \subseteq A$  is **admissible** in  $F$ , if

- $S$  is conflict-free in  $F$
- each  $a \in S$  is **defended** by  $S$  in  $F$ 
  - $a \in A$  is defended by  $S$  in  $F$ , if for each  $b \in A$  with  $(b, a) \in R$ , there exists a  $c \in S$ , such that  $(c, b) \in R$ .

## Encoding

$$\pi_{adm} = \pi_{cf} \cup \left\{ \begin{array}{l} \text{defeated}(X) \leftarrow \text{in}(Y), \text{att}(Y, X) \\ \leftarrow \text{in}(X), \text{att}(Y, X), \text{not defeated}(Y) \end{array} \right\}$$

**Result:** For each AF  $F$ ,  $adm(F) \equiv \mathcal{AS}(\pi_{adm}(\widehat{F}))$

# ASP Encodings ctd.

## Stable Extensions

Given an AF  $F = (A, R)$ . A set  $S \subseteq A$  is a **stable extension** of  $F$ , if

- $S$  is conflict-free in  $F$
- for each  $a \in A \setminus S$ , there exists a  $b \in S$ , such that  $(b, a) \in R$

## Encoding

$$\pi_{stable} = \pi_{cf} \cup \left\{ \begin{array}{l} \text{defeated}(X) \quad \leftarrow \quad \text{in}(Y), \text{att}(Y, X) \\ \text{out}(X), \text{not defeated}(X) \end{array} \right\}$$

**Result:** For each AF  $F$ ,  $stable(F) \equiv \mathcal{AS}(\pi_{stable}(\widehat{F}))$

# ASP Encodings ctd.

## Grounded Extension

Given an AF  $F = (A, R)$ . The characteristic function  $\mathcal{F}_F : 2^A \rightarrow 2^A$  of  $F$  is defined as

$$\mathcal{F}_F(E) = \{x \in A \mid x \text{ is defended by } E\}.$$

The least fixed point of  $\mathcal{F}_F$  is the grounded extension.

## Order over domain

$$\pi_{<} = \left\{ \begin{array}{ll} \text{lt}(X, Y) & \leftarrow \text{arg}(X), \text{arg}(Y), X < Y \\ \text{nsucc}(X, Z) & \leftarrow \text{lt}(X, Y), \text{lt}(Y, Z) \\ \text{succ}(X, Y) & \leftarrow \text{lt}(X, Y), \text{not nsucc}(X, Y) \\ \text{ninf}(X) & \leftarrow \text{lt}(Y, X) \\ \text{nsup}(X) & \leftarrow \text{lt}(X, Y) \\ \text{inf}(X) & \leftarrow \text{not ninf}(X), \text{arg}(X) \\ \text{sup}(X) & \leftarrow \text{not nsup}(X), \text{arg}(X) \end{array} \right\}$$



# ASP Encodings ctd.

## Grounded Extension

Given an AF  $F = (A, R)$ . The characteristic function  $\mathcal{F}_F : 2^A \rightarrow 2^A$  of  $F$  is defined as

$$\mathcal{F}_F(E) = \{x \in A \mid x \text{ is defended by } E\}.$$

The least fixed point of  $\mathcal{F}_F$  is the grounded extension.

## Encodings Grounded Extension

$$\pi_{ground} = \left\{ \begin{array}{ll} \text{def\_upto}(X, Y) & \leftarrow \text{inf}(Y), \text{arg}(X), \text{not att}(Y, X) \\ \text{def\_upto}(X, Y) & \leftarrow \text{inf}(Y), \text{in}(Z), \text{att}(Z, Y), \text{att}(Y, X) \\ \text{def\_upto}(X, Y) & \leftarrow \text{succ}(Z, Y), \text{def\_upto}(X, Z), \text{not att}(Y, X) \\ \text{def\_upto}(X, Y) & \leftarrow \text{succ}(Z, Y), \text{def\_upto}(X, Z), \text{in}(V), \\ & \text{att}(V, Y), \text{att}(Y, X) \\ \text{defended}(X) & \leftarrow \text{sup}(Y), \text{def\_upto}(X, Y) \\ \text{in}(X) & \leftarrow \text{defended}(X) \end{array} \right\}$$

**Result:** For each AF  $F$ ,  $\text{ground}(F) \equiv \mathcal{AS}(\pi_{ground}(\widehat{F}))$

# ASP Encodings

## Preferred Extensions

Given an AF  $F = (A, R)$ . A set  $S \subseteq A$  is a preferred extension of  $F$ , if

- $S$  is admissible in  $F$
- for each  $T \subseteq A$  admissible in  $F$ ,  $S \not\subseteq T$

## Encoding

- Preferred semantics needs **subset maximization task**.
- Can be encoded in standard ASP but requires **insight** and **expertise**.

# Saturation Encodings

## Preferred Extension

Given an AF  $(A, R)$ . A set  $S \subseteq A$  is **preferred** in  $F$ , if  $S$  is admissible in  $F$  and for each  $T \subseteq A$  admissible in  $T$ ,  $S \not\subseteq T$ .

## Encoding

$$\pi_{\text{sat}} = \left\{ \begin{array}{ll} \text{inN}(X) \vee \text{outN}(X) & \leftarrow \text{out}(X); \\ \text{inN}(X) & \leftarrow \text{in}(X) \\ \text{fail} & \leftarrow \text{eq} \\ \text{fail} & \leftarrow \text{inN}(X), \text{inN}(Y), \text{att}(X, Y) \\ \text{fail} & \leftarrow \text{inN}(X), \text{outN}(Y), \text{att}(Y, X), \\ & \text{undefeated}(Y) \\ \text{inN}(X) & \leftarrow \text{fail}, \text{arg}(X) \\ \text{outN}(X) & \leftarrow \text{fail}, \text{arg}(X) \\ & \leftarrow \text{not fail} \end{array} \right\}$$
$$\pi_{\text{pref}} = \pi_{\text{adm}} \cup \pi_{\text{helpers}} \cup \pi_{\text{sat}}$$

**Result:** For each AF  $F$ ,  $\text{pref}(F) \equiv \mathcal{AS}(\pi_{\text{pref}}(\hat{F}))$

# Metasp [Gebser et al., 2011]

- Recently proposed `metasp` front-end for the `gringo/claspD` package.
- The problem encoding is first grounded with the `reify` option, which outputs ground program as facts.
- Next the meta encodings mirror answer-set generation.
- Meta encodings also implement `subset minimization` for the `#minimize-statement`.



# Metasp Encoding

- Together with the module admissibility, the remaining encoding for subset maximization reduces to

## Preferred Extensions

$$\pi_{adm} \cup \{\#minimize[out(X)]\}.$$

- This relocates the optimization encoding to the **meta-encodings**.
- Enables simple encodings and performs surprisingly well.

# Additional info on encodings and extensions

## ASPARTIX (ASP Argumentation Reasoning Tool)

- Encodings are used together with an ASP-solver, like clasp or dlv
- Implements all prominent argumentation semantics
- Even for extended frameworks like PAFs, VAFs, BAPs, ...
- Easy to use
- Web-interface available:  
<http://rull.dbai.tuwien.ac.at:8080/ASPARTIX/>

## Info and encodings are available under:

<http://www.dbai.tuwien.ac.at/research/project/argumentation/>

# Related work

## Other encodings

- by [Nieves et al., 2008] and follow-up papers; mostly a new program has to be constructed for each instance
- Related approaches: reductions to SAT/QSAT [Besnard and Doutre, 2004, Egly and Woltran, 2006]
- DIAMOND (DIAlectical MOdels eNcoDing) is a software system to compute different ADF models (see <https://isysrv.informatik.uni-leipzig.de/diamond>)
- ConArg is a tool, based on Constraint Programming [Bistarelli and Santini, 2012] (see <http://www.dmi.unipg.it/conarg/>)

## Other systems

- Collection:  
<http://wyner.info/LanguageLogicLawSoftware/index.php/software/>
- System Demos at COMMA 2014:  
<http://comma2014.arg.dundee.ac.uk/demoprogram>

# Summary

What did we learn today?

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⋮





P. Baroni, P. E. Dunne, and M. Giacomin.

On the resolution-based family of abstract argumentation semantics and its grounded instance.  
Artif. Intell., 175(3-4):791–813, 2011.



Philippe Besnard and Sylvie Doutre.

Checking the acceptability of a set of arguments.

In Proceedings of the 10th International Workshop on Non-Monotonic Reasoning (NMR'02), pages 59–64, 2004.



S. Bistarelli, F. Santini, Conarg: a tool to solve (weighted) abstract argumentation frameworks with (soft) constraints, CoRR abs/1212.2857.



Dung, P. M. (1995).

On the acceptability of arguments and its fundamental role in nonmonotonic reasoning, logic programming and n-person games.

Artif. Intell., 77(2):321–358.



Dvořák, W., Gaggl, S. A., Wallner, J., and Woltran, S. (2011).

Making use of advances in answer-set programming for abstract argumentation systems.



Uwe Egly and Stefan Woltran.

Reasoning in argumentation frameworks using quantified boolean formulas.

In Proceedings of the 1st Conference on Computational Models of Argument (COMMA'06), pages 133–144. IOS Press, 2006.



Uwe Egly, Sarah Gaggl, and Stefan Woltran.

Answer-set programming encodings for argumentation frameworks.

In Argument and Computation, 1(2):147–177, 2010.



Gebser, M., Kaminski, R., and Schaub, T. (2011).

Complex optimization in answer set programming.

TPLP, 11(4-5):821–839.



Juan Carlos Nieves, Mauricio Osorio, and Ulises Cortés.

Preferred extensions as stable models.

Theory and Practice of Logic Programming, 8(4):527–543, July 2008.



P. M. Dung, P. Mancarella, and F. Toni.

Computing ideal sceptical argumentation.

Artif. Intell. 171(10-15):642–674, 2007.



P. E. Dunne.

Computational properties of argument systems satisfying graph-theoretic constraints.

Artif. Intell., 171(10-15):701–729, 2007.



P. E. Dunne.

The computational complexity of ideal semantics I: Abstract argumentation frameworks.

In Proc. COMMA'08, pages 147–158. IOS Press, 2008.



P. E. Dunne and T. J. M. Bench-Capon.

Coherence in finite argument systems.

Artif. Intell., 141(1/2):187–203, 2002.



P. E. Dunne and T. J. M. Bench-Capon.

Complexity in value-based argument systems.

In Proc. JELIA 2004, pages 360–371. Springer, 2004.



W. Dvořák, P. Dunne, and S. Woltran.

Parametric properties of ideal semantics.

In Proc. IJCAI 2011, pages 851–856, 2011.



W. Dvořák and S. Woltran

On the intertranslatability of argumentation semantics

J. Artif. Intell. Res. 41:445–475, 2011



S. Gaggl and S. Woltran.

cf2 semantics revisited.

In Proc. COMMA 2010, pages 243–2540. IOS Press, 2010.



S. Gaggl and S. Woltran.

Strong equivalence for argumentation semantics based on conflict-free sets.

In Proc. ECSQARU 2011, pages 38–49. Springer, 2011.



E. Oikarinen and S. Woltran.

Characterizing strong equivalence for argumentation frameworks.

Artif. Intell. 175(14-15): 1985–2009, 2011.



B. Verheij.

Two approaches to dialectical argumentation: admissible sets and argumentation stages.

In Proc. NAIC'96, pages 357–368, 1996.



M. Caminada.

Semi-stable semantics.

In Proc. COMMA 2006, pages 121–130. IOS Press, 2006.



M. Caminada.

Comparing two unique extension semantics for formal argumentation: ideal and eager

In Proc. BNAIC 2007, pages 81–87, 2007.



P. Baroni, M. Giacomin, and G. Guida.

SCC-Recursiveness: A General Schema for Argumentation Semantics.

Artif. Intell., 168(1-2): 162–210. Springer, 2005.