

A Comprehensive Analysis of the cf2 Argumentation Semantics: From Characterization to Implementation

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- Argumentation is one of the major fields in **Artificial Intelligence (AI)**.
- **Applications** in diverse domains (legal reasoning, multi-agent systems, social networks, e-government, decision support).
- Concept of **abstract Argumentation Frameworks (AFs)** [Dung, 1995] is one of the most popular approaches.
- **Arguments** and a binary **attack** relation between them, denoting conflicts, are the only components.
- Numerous **semantics** to solve the inherent conflicts by selecting acceptable sets of argument.
- **Admissible-based** versus **naive-based** semantics.
- Development of **competitive systems**.

cf2 Semantics

- is based on **decomposition** of the framework along its **strongly connected components (SCCs)** [Baroni et al., 2005];
- does not require to defend arguments against attacks;
- allows to **treat cycles** in a more **sensitive way** than other semantics;
- is **not well studied**, due to quite complicated definition.

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Goals of the Thesis

- **Answer-set programming encodings** for *cf2*.
- **Alternative characterization.**
- Verification of **behavior** on concrete instances.
- Identification of possible **redundancies.**
- Complete **complexity analysis.**

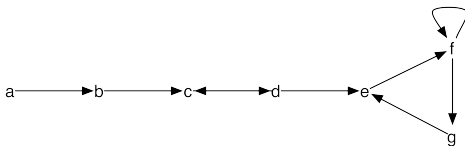


- 1 Background on abstract argumentation frameworks and semantics
- 2 Alternative characterization of *cf2*
- 3 Combining *cf2* and stage semantics
- 4 Redundancies and strong equivalence
- 5 Computational complexity
- 6 Implementations
- 7 Conclusion

Abstract Argumentation Framework [Dung, 1995]

An **abstract argumentation framework** (AF) is a pair $F = (A, R)$, where A is a finite set of arguments and $R \subseteq A \times A$. Then $(a, b) \in R$ if a attacks b . Argument $a \in A$ is **defended** by $S \subseteq A$ (in F) iff, for each $b \in A$ with $(b, a) \in R$, S attacks b .

Example

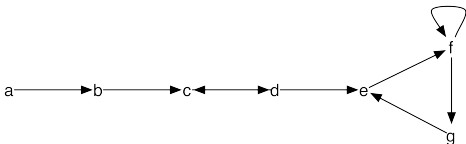


Semantics for AFs

Let $F = (A, R)$ and $S \subseteq A$, we say

- S is **conflict-free** in F , i.e. $S \in cf(F)$, if $\forall a, b \in S: (a, b) \notin R$;
- $S \in cf(F)$ is maximal conflict-free or **naive** (in F), i.e. $S \in naive(F)$, if $\forall T \in cf(F), S \not\subseteq T$.

Example



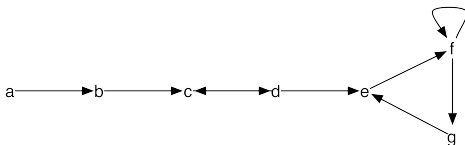
$$naive(F) = \{\{a, d, g\}, \{a, c, e\}, \{a, c, g\}\}.$$

Naive-based Semantics

Let $F = (A, R)$ and $S \subseteq A$. Let $S_R^+ = S \cup \{b \mid \exists a \in S, \text{ s. t. } (a, b) \in R\}$ be the **range** of S . Then, a set $S \in cf(F)$ is

- a **stable** extension (of F), i.e. $S \in stable(F)$, if $S_R^+ = A$;
- **stage** in F , i.e. $S \in stage(F)$, if for each $T \in cf(F)$, $S_R^+ \not\subseteq T_R^+$.

Example



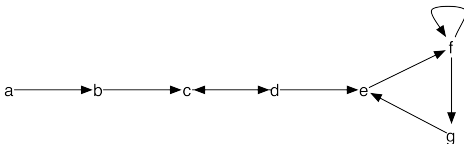
$$stable(F) = \emptyset, stage(F) = \{\{a, d, g\}, \{a, c, e\}, \{a, c, g\}\}.$$

Admissible-based Semantics

Then, $S \in cf(F)$ is

- **admissible** in F , i.e. $S \in adm(F)$, if each $a \in S$ is defended by S ;
- a **preferred** extension (of F), i.e. $S \in pref(F)$, if $S \in adm(F)$ and for each $T \in adm(F)$, $S \not\subseteq T$.

Example



$$adm(F) = \{\emptyset, \{a\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}\}, \quad pref(F) = \{\{a, c\}, \{a, d\}\}.$$

- One of the SCC-recursive semantics introduced in [Baroni et al., 2005].
- Naive-based semantics.
- Handles odd- and even-length cycles in a uniform way.
- Can accept arguments out of odd-length cycles.
- Can accept arguments attacked by self-attacking arguments.
- Satisfies most of the evaluation criteria proposed in [Baroni and Giacomin, 2007].

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Further Notations, let $F = (A, R)$

- $SCCs(F)$: set of strongly connected components of F ,
- $C_F(a)$: the unique set $C \in SCCs(F)$, s.t. $a \in C$,
- $F|_S = ((A \cap S), R \cap (S \times S))$: sub-framework of F w.r.t. S ,
- $F|_S - S' = F|_{S \setminus S'}$, $F - S = F|_{A \setminus S}$.

Definition ($D_F(S)$)

Let $F = (A, R)$ be an AF and $S \subseteq A$. An argument $b \in A$ is **component-defeated** by S (in F), if there exists an $a \in S$, such that $(a, b) \in R$ and $a \notin C_F(b)$. The set of arguments component-defeated by S in F is denoted by $D_F(S)$.

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cf2 Extensions [Baroni et al., 2005]

Let $F = (A, R)$ be an argumentation framework and S a set of arguments. Then, S is a **cf2 extension** of F , i.e. $S \in cf2(F)$, iff

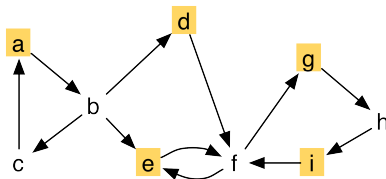
- $S \in naive(F)$, in case $|SCCs(F)| = 1$;
- otherwise, $\forall C \in SCCs(F)$, $(S \cap C) \in cf2(F|_C - D_F(S))$.

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Example

$S = \{a, d, e, g, i\}$, $S \in cf2(F)$?

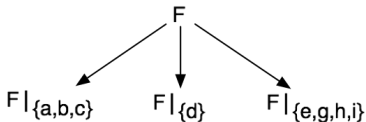
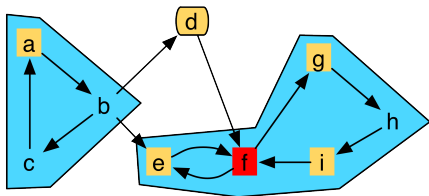


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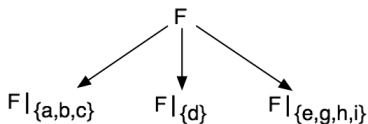
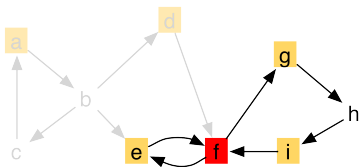


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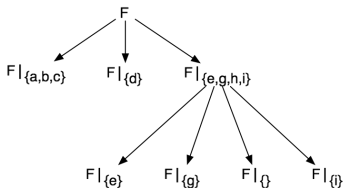
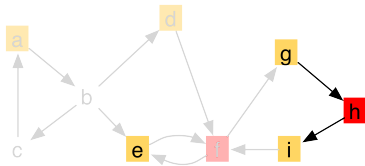


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Example

$S = \{a, d, e, g, i\}$, $S \in cf2(F)$? $C_4 = \{e\}, C_5 = \{g\}, C_6 = \{h\}, C_7 = \{i\}$
 and $D_F|_{\{e,g,h,i\}}(\{e, g, i\}) = \{h\}$.

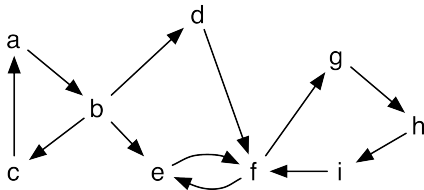


- Original definition of $cf2$ is rather **cumbersome** to be directly encoded in **ASP** due to the **recursive computation** of different **sub-frameworks**.
- In **alternative characterization** we shift the **recursion** to a certain **set** of arguments.
- This enables to directly
 - **guess** a set S ;
 - **check** whether S is a **naive extension** of a certain **instance** of F .

Separation

An AF $F = (A, R)$ is called **separated** if for each $(a, b) \in R$, there exists a path from b to a . We define $[[F]] = \bigcup_{C \in SCCs(F)} F|_C$ and call $[[F]]$ the **separation** of F .

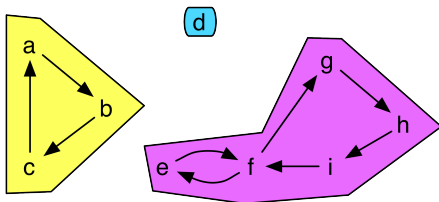
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Example



Reachability

Let $F = (A, R)$ be an AF, B a set of arguments, and $a, b \in A$. We say that b is **reachable** in F from a **modulo** B , in symbols $a \Rightarrow_F^B b$, if there exists a path from a to b in $F|_B$.

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Definition ($\Delta_{F,S}$)

For an AF $F = (A, R)$, $D \subseteq A$, and a set S of arguments,

$$\Delta_{F,S}(D) = \{a \in A \mid \exists b \in S : b \neq a, (b, a) \in R, a \not\Rightarrow_F^{A \setminus D} b\},$$

and $\Delta_{F,S}$ be the least fixed-point of $\Delta_{F,S}(\emptyset)$.

$cf2$ Extensions [Gaggl and Woltran, 2012]

Given an AF $F = (A, R)$.

$$cf2(F) = \{S \mid S \in naive(F) \cap naive([F - \Delta_{F,S}])\}.$$

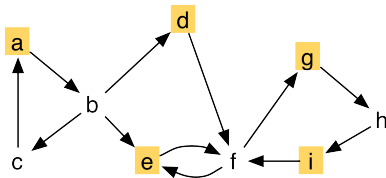
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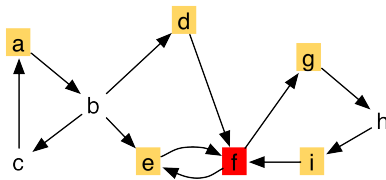
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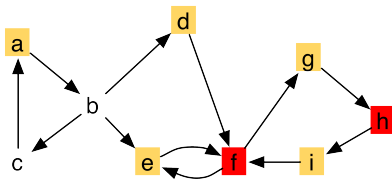
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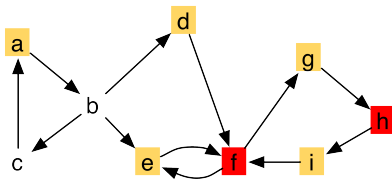
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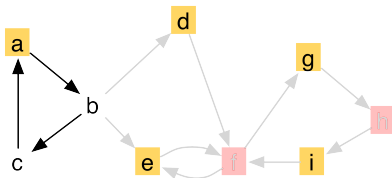
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Example

$S = \{a, d, e, g, i\}$, $S \in naive(F)$, $\Delta_{F,S} = \{f, h\}$, $S \in naive([F - \Delta_{F,S}])$,
thus $S \in cf2(F)$.



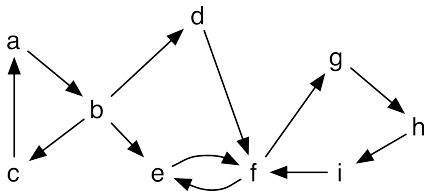
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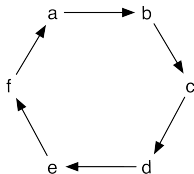
Example

$$cf2(F) = \{\{a, d, e, g, i\}, \{c, d, e, g, i\}, \{b, f, h\}, \{b, g, i\}\}.$$



- *cf2* produces questionable results on AFs with cycles of length ≥ 6 .

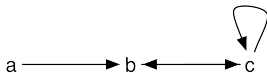
Example



$$\begin{aligned}cf2(F) &= naive(F) = \{\{a, d\}, \{b, e\}, \{c, f\}, \{a, c, e\}, \{b, d, f\}\}; \\ stage(F) &= \{\{a, c, e\}, \{b, d, f\}\}.\end{aligned}$$

- $cf2$ produces questionable results on AFs with cycles of length ≥ 6 .
- The grounded extension is not necessarily contained in every stage extension.
 - Stage semantics does not satisfy directionality.

Example



$stage(F) = \{\{a\}, \{b\}\}$ but $cf2(F) = ground(F) = \{\{a\}\}$.

We combine *cf2* and stage semantics [Dvorák and Gaggl, 2012a], by

- using the SCC-recursive schema of the *cf2* semantics and
- instantiate the base case with stage semantics.

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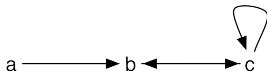
stage2 Extensions

For any AF F ,

$$\text{stage2}(F) = \{S \mid S \in \text{naive}(F) \cap \text{stage}([F - \Delta_{F,S}])\}.$$

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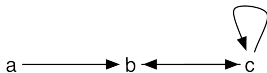
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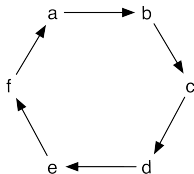
$stage2(F) = cf2(F) = \{\{a\}\}$, where $stage(F) = \{\{a\}, \{b\}\}$.

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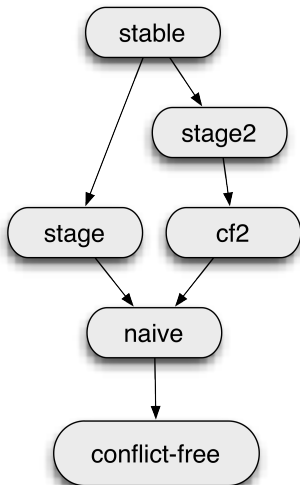
Example



$stage2(F) = cf2(F) = \{\{a\}\}$, where $stage(F) = \{\{a\}, \{b\}\}$.



$stage2(G) = stage(G) = \{\{a, c, e\}, \{b, d, f\}\}$, but
 $cf2(G) = naive(F) = \{\{a, d\}, \{b, e\}, \{c, f\}, \{a, c, e\}, \{b, d, f\}\}$.



- Argumentation is a **dynamic reasoning process**.
- Which **effect** has **additional information** w.r.t. a semantics?
- Which information **does not contribute to results** no matter which changes are performed?
- Identification of **kernels** to remove **redundant attacks** [Oikarinen and Woltran, 2011].

Definition

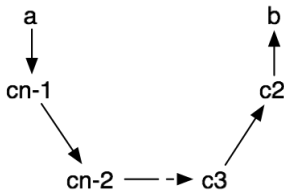
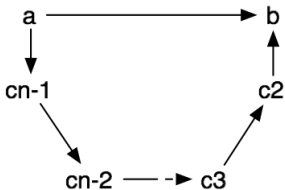
Two AFs F and G are **strongly equivalent** to each other w.r.t. a semantics σ , in symbols $F \equiv_s^\sigma G$, iff for each AF H , $\sigma(F \cup H) = \sigma(G \cup H)$.

Theorem

For any AFs F and G , $F \equiv_s^{cf_2} G$ iff $F = G$.

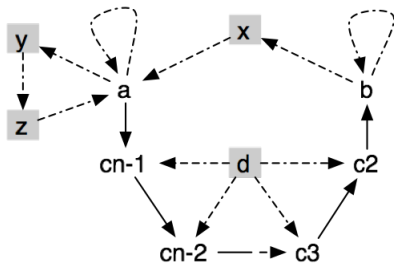
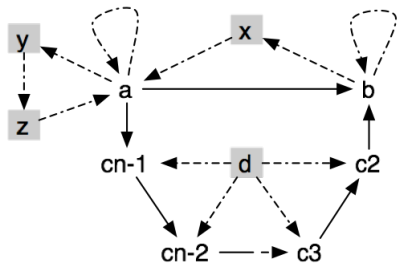
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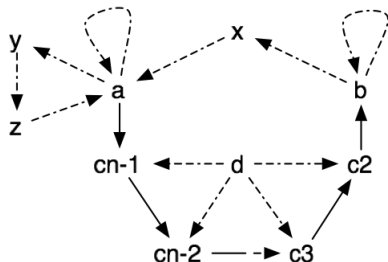
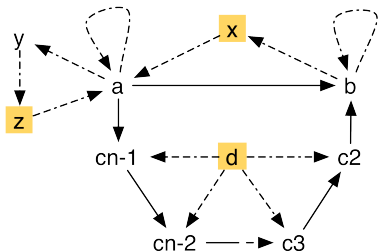
For any AFs F and G , $F \equiv_s^{cf_2} G$ iff $F = G$.



$$\begin{aligned}
 H = & (A \cup \{d, x, y, z\}, \\
 & \{(a, a), (b, b), (b, x), (x, a), (a, y), (y, z), (z, a), \\
 & (d, c) \mid c \in A \setminus \{a, b\}\}).
 \end{aligned}$$

Theorem

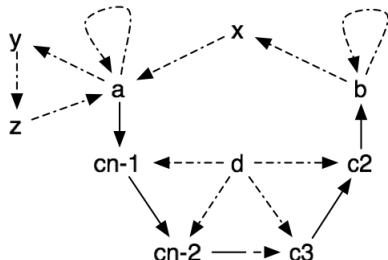
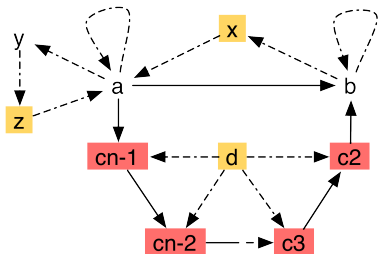
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Let $E = \{d, x, z\}$, $E \in cf_2(F \cup H)$ but $E \notin cf_2(G \cup H)$.

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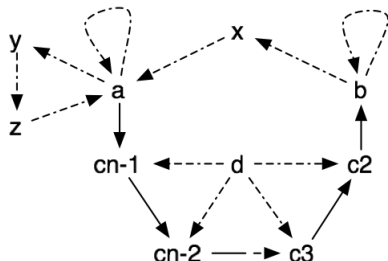
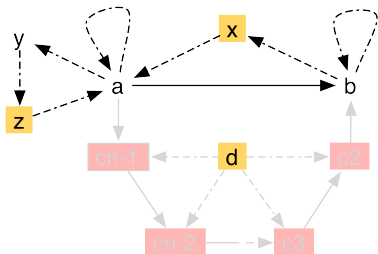
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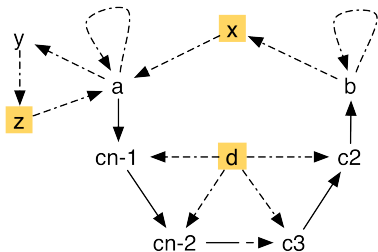
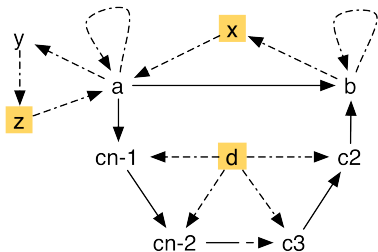
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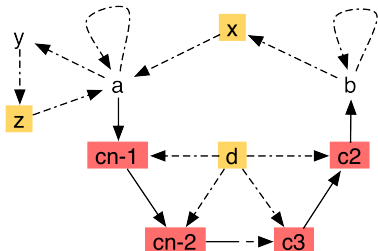
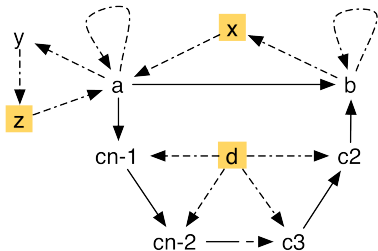
For any AFs F and G , $F \equiv_s^{cf_2} G$ iff $F = G$.



Let $E = \{d, x, z\}$, $E \in cf_2(F \cup H)$ but $E \notin cf_2(G \cup H)$.

Theorem

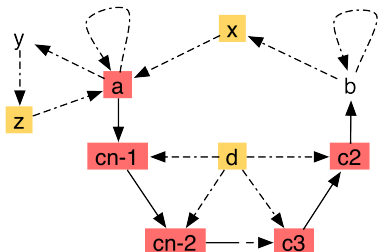
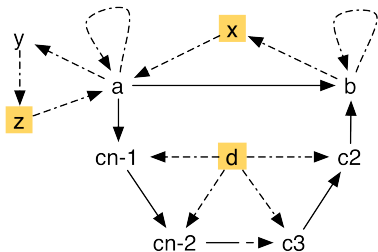
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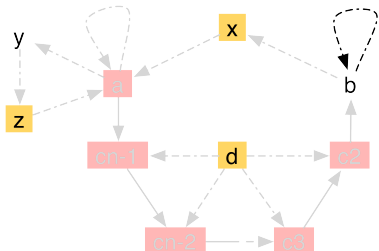
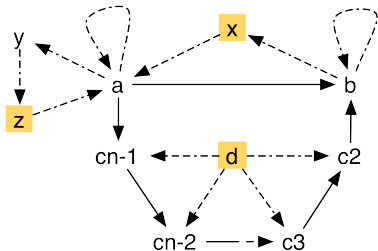
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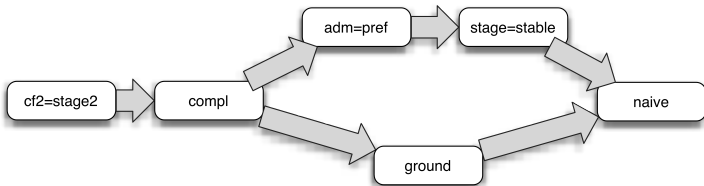
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Succinctness Property

An argumentation semantics σ satisfies the **succinctness property** or is **maximal succinct** iff no AF contains a redundant attack w.r.t. σ .



	<i>Ver</i>	<i>Cred</i>	<i>Skept</i>	<i>Exists</i> ^{-∅}
<i>naive</i>	in P	in P	in P	in P
<i>stable</i>	in P	NP-c	coNP-c	NP-c
<i>cf2</i>	in P	NP-c	coNP-c	in P
<i>stage</i>	coNP-c	Σ_2^P -c	Π_2^P -c	in P
<i>stage2</i>	coNP-c	Σ_2^P -c	Π_2^P -c	in P

Table: Computational complexity of naive-based semantics.

Reduction-based Approach

- Answer-set Programming (ASP) encodings for *cf2* and *stage2*.
- Saturation vs. `metasp` encodings for *stage2*.
- All encodings incorporated in the system
`ASPARTIX` [Egly et al., 2010].

Direct Approach




- Labeling-based algorithms for *cf2* and *stage2*.

Web-Application

`http://rull.dbai.tuwien.ac.at:8080/ASPARTIX`

- Alternative characterization for *cf2* to avoid the recursive computation of sub-frameworks.
- *stage2* semantics overcomes problems of *cf2*.
- Strong equivalence w.r.t. *cf2* (resp. *stage2*) coincides with syntactic equivalence.
- Provided the missing complexity results for *cf2* (resp. *stage2*).
- Implementation in terms of ASP and labeling-based algorithms.

- Further relations to other semantics like [intertranslatability](#).
- [Optimizations](#) of ASP encodings.
- Development of [appropriate instantiation methods](#) for naive-based semantics.
- [Other combinations](#) of semantics in the alternative characterization, like $sem(F) = \{S \mid \sigma(F) \cap \tau([[F - \Delta_{F,S}]])\}$.

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	<i>cf2</i>	<i>stage2</i>	<i>stable</i>	<i>stage</i>
$Cred_{\sigma}^{acycl}$	in P	in P	P-c	P-c
$Skept_{\sigma}^{acycl}$	in P	in P	P-c	P-c
$Cred_{\sigma}^{even-free}$	NP-c	coNP-h	P-c	Σ_2^P -c
$Skept_{\sigma}^{even-free}$	coNP-c	coNP-h	P-c	Π_2^P -c
$Cred_{\sigma}^{bipart}$	in P	in P	P-c	P-c
$Skept_{\sigma}^{bipart}$	in P	in P	P-c	P-c
$Cred_{\sigma}^{sym}$	in P	in P/ Σ_2^P *	in P	in P/ Σ_2^P *
$Skept_{\sigma}^{sym}$	in P	in P/ Π_2^P *	in P	in P/ Π_2^P *

Table: Complexity results for special AFs (* with self-attacking arguments).