

DATABASE THEORY

Lecture 15: Datalog Evaluation (2)

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Semi-Naive Evaluation: Example

$$\begin{array}{cccc} & \text{e}(1,2) & \text{e}(2,3) & \text{e}(3,4) & \text{e}(4,5) \\ \\ (R1) & & \mathsf{T}(x,y) \leftarrow \mathsf{e}(x,y) \\ \\ (R2.1) & & \mathsf{T}(x,z) \leftarrow \Delta_\mathsf{T}^i(x,y) \wedge \mathsf{T}^i(y,z) \\ \\ (R2.2') & & \mathsf{T}(x,z) \leftarrow \mathsf{T}^{i-1}(x,y) \wedge \Delta_\mathsf{T}^i(y,z) \end{array}$$

How many body matches do we need to iterate over?

$$\begin{split} T_P^0 &= \emptyset & \text{initialisation} \\ T_P^1 &= \{\mathsf{T}(1,2),\mathsf{T}(2,3),\mathsf{T}(3,4),\mathsf{T}(4,5)\} & 4 \times (R1) \\ T_P^2 &= T_P^1 \cup \{\mathsf{T}(1,3),\mathsf{T}(2,4),\mathsf{T}(3,5)\} & 3 \times (R2.1) \\ T_P^3 &= T_P^2 \cup \{\mathsf{T}(1,4),\mathsf{T}(2,5),\mathsf{T}(1,5)\} & 3 \times (R2.1),2 \times (R2.2') \\ T_P^4 &= T_P^3 &= T_P^\infty & 1 \times (R2.1),1 \times (R2.2') \end{split}$$

In total, we considered 14 matches to derive 11 facts

Review: Datalog Evaluation

A rule-based recursive query language

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\begin{aligned} & \text{father(alice, bob)} \\ & \text{mother(alice, carla)} \\ & & \text{Parent}(x,y) \leftarrow \text{father}(x,y) \\ & & \text{Parent}(x,y) \leftarrow \text{mother}(x,y) \\ & \text{SameGeneration}(x,x) \\ & \text{SameGeneration}(x,y) \leftarrow \text{Parent}(x,v) \land \text{Parent}(y,w) \land \text{SameGeneration}(v,w) \end{aligned}
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Perfect static optimisation for Datalog is undecidable

Datalog queries can be evaluated bottom-up or top-down

Simplest practical bottom-up technique: semi-naive evaluation

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slide 2 of 27

Semi-Naive Evaluation: Full Definition

In general, a rule of the form

$$H(\vec{x}) \leftarrow e_1(\vec{y}_1) \wedge \ldots \wedge e_n(\vec{y}_n) \wedge I_1(\vec{z}_1) \wedge I_2(\vec{z}_2) \wedge \ldots \wedge I_m(\vec{z}_m)$$

is transformed into m rules

$$\begin{split} \mathsf{H}(\vec{x}) &\leftarrow \mathsf{e}_1(\vec{y}_1) \wedge \ldots \wedge \mathsf{e}_n(\vec{y}_n) \wedge \Delta^i_{l_1}(\vec{z}_1) \wedge l_2^i(\vec{z}_2) \wedge \ldots \wedge l_m^i(\vec{z}_m) \\ \mathsf{H}(\vec{x}) &\leftarrow \mathsf{e}_1(\vec{y}_1) \wedge \ldots \wedge \mathsf{e}_n(\vec{y}_n) \wedge l_1^{i-1}(\vec{z}_1) \wedge \Delta^i_{l_2}(\vec{z}_2) \wedge \ldots \wedge l_m^i(\vec{z}_m) \\ &\cdots \\ \mathsf{H}(\vec{x}) &\leftarrow \mathsf{e}_1(\vec{y}_1) \wedge \ldots \wedge \mathsf{e}_n(\vec{y}_n) \wedge l_1^{i-1}(\vec{z}_1) \wedge l_2^{i-1}(\vec{z}_2) \wedge \ldots \wedge \Delta^i_1(\vec{z}_m) \end{split}$$

Advantages and disadvantages:

- · Huge improvement over naive evaluation
- Some redundant computations remain (see example)
- Some overhead for implementation (store level of entailments)

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Top-Down Evaluation

Idea: we may not need to compute all derivations to answer a particular query

Example 15.1:

$$\begin{array}{ccccc} & \text{e}(1,2) & \text{e}(2,3) & \text{e}(3,4) & \text{e}(4,5) \\ & & \text{T}(x,y) \leftarrow \text{e}(x,y) \\ & & \text{T}(x,z) \leftarrow \text{T}(x,y) \land \text{T}(y,z) \\ & & \text{Query}(z) \leftarrow \text{T}(2,z) \end{array}$$

The answers to Query are the T-successors of 2.

However, bottom-up computation would also produce facts like T(1,4), which are neither directly nor indirectly relevant for computing the query result.

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Query-Subquery (QSQ)

QSQ is a technique for organising top-down Datalog query evaluation

Main principles:

- Apply backward chaining/resolution: start with query, find rules that can derive query, evaluate body atoms of those rules (subqueries) recursively
- Evaluate intermediate results "set-at-a-time" (using relational algebra on tables)
- Evaluate queries in a "data-driven" way, where operations are applied only to newly computed intermediate results (similar to idea in semi-naive evaluation)
- "Push" variable bindings (constants) from heads (queries) into bodies (subqueries)
- "Pass" variable bindings (constants) "sideways" from one body atom to the next

Details can be realised in several ways.

Assumption

Assumption: For all techniques presented in this lecture, we assume that the given Datalog program is safe.

- This is without loss of generality (as shown in exercise).
- One can avoid this by adding more cases to algorithms.

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Adornments

To guide evaluation, we distinguish free and bound parameters in a predicate.

Example 15.2: If we want to derive atom T(2, z) from the rule $T(x, z) \leftarrow T(x, y) \wedge T(y, z)$, then x will be bound to 2, while z is free.

We use adornments to denote the free/bound parameters in predicates.

Example 15.3:

$$\mathsf{T}^{bf}(x,z) \leftarrow \mathsf{T}^{bf}(x,y) \wedge \mathsf{T}^{bf}(y,z)$$

- since x is bound in the head, it is also bound in the first atom
- any match for the first atom binds *y*, so *y* is bound when evaluating the second atom (in left-to-right evaluation)

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 slide 7 of 27
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 slide 8 of 27

slide 5 of 27

Adornments: Examples

The adornment of the head of a rule determines the adornments of the body atoms:

$$\mathsf{R}^{bbb}(x,y,z) \leftarrow \mathsf{R}^{bbf}(x,y,v) \wedge \mathsf{R}^{bbb}(x,v,z)$$
$$\mathsf{R}^{fbf}(x,y,z) \leftarrow \mathsf{R}^{fbf}(x,y,v) \wedge \mathsf{R}^{bbf}(x,v,z)$$

The order of body predicates affects the adornment:

$$S^{ff}(x, y, z) \leftarrow T^{ff}(x, v) \wedge T^{ff}(y, w) \wedge R^{bbf}(v, w, z)$$

$$S^{ff}(x, y, z) \leftarrow R^{ff}(v, w, z) \wedge T^{fb}(x, v) \wedge T^{fb}(y, w)$$

→ For optimisation, some orders might be better than others

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slide 9 of 27

Auxiliary Relations for QSQ (2)

When evaluating body atoms from left to right, we use supplementary relations sup-

- → bindings required to evaluate rest of rule after the *i*th body atom
- \rightarrow the first set of bindings sup₀ comes from input_p^{α}
- \rightarrow the last set of bindings sup, go to output^{α}

Example 15.4:

$$\begin{split} \mathbf{T}^{bf}(x,z) \leftarrow \mathbf{T}^{bf}(x,y) \wedge \mathbf{T}^{bf}(y,z) \\ & \qquad \\ & \text{input}_{\mathbf{T}}^{bf} \Rightarrow \sup_{\mathbf{Z}}[x] \quad \sup_{\mathbf{Z}}[x,y] \quad \sup_{\mathbf{Z}}[x,z] \Rightarrow \text{output}_{\mathbf{T}}^{bf} \end{split}$$

- $\sup_0[x]$ is copied from $\inf_T[x]$ (with some exceptions, see exercise)
- $\sup_1[x,y]$ is obtained by joining tables $\sup_0[x]$ and $\operatorname{output}_T^{bf}[x,y]$
- $\sup_{z}[x, z]$ is obtained by joining tables $\sup_{z}[x, y]$ and $\sup_{z}[y, z]$
- output $_{\mathsf{T}}^{bf}[x,z]$ is copied from $\sup_{z}[x,z]$

(we use "named" notation like [x,y] to suggest what to join on; the relations are the same)

Auxiliary Relations for QSQ

To control evaluation, we store intermediate results in auxiliary relations.

When we "call" a rule with a head where some variables are bound, we need to provide the bindings as input

- \rightarrow for adorned relation R^{α} , we use an auxiliary relation input
- \rightarrow arity of input_p = number of b in α

The result of calling a rule should be the "completed" input, with values for the unbound variables added

- \rightarrow for adorned relation R^{α} , we use an auxiliary relation output^{α}
- \rightarrow arity of output^{α} = arity of R (= length of α)

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slide 10 of 27

OSO Evaluation

The set of all auxiliary relations is called a QSQ template (for the given set of adorned rules)

General evaluation:

- add new tuples to auxiliary relations until reaching a fixed point
- evaluation of a rule can proceed as sketched on previous slide
- in addition, whenever new tuples are added to a sup relation that feeds into an IDB atom, the input relation of this atom is extended to include all binding given by sup (may trigger subquery evaluation)
- → there are many strategies for implementing this general scheme

Notation

 \bullet for an EDB atom A, we write $A^{\mathcal{I}}$ for table that consists of all matches for A in the database

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Recursive OSO

Recursive QSQ (QSQR) takes a "depth-first" approach to QSQ

Evaluation of single rule in QSQR:

Given: adorned rule r with head predicate R^{α} ; current values of all QSQ relations

- (1) Copy tuples input $^{\alpha}_{p}$ (that unify with rule head) to $\sup_{n=1}^{r}$
- (2) For each body atom A_1, \ldots, A_n , do:
 - If A_i is an EDB atom, compute $\sup_{i=1}^r$ as projection of $\sup_{i=1}^r \bowtie A_i^I$
 - If A_i is an IDB atom with adorned predicate S^{β} :
 - (a) Add new bindings from $\sup_{i=1}^r,$ combined with constants in $A_i,$ to $\mathsf{input}_{\mathbf{c}}^{\theta}$
 - (b) If input_S^{\beta} changed, recursively evaluate all rules with head predicate S^{β}
 - (c) Compute $\sup_{i=1}^{r} as projection of <math>\sup_{i=1}^{r} \bowtie output_{S}^{\beta}$
- (3) Add tuples in $\sup_{n=1}^{r}$ to $\operatorname{output}_{\mathbf{R}}^{\alpha}$

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QSQR Transformation: Example

Predicates S (same generation), p (parent), h (human)

$$S(x, x) \leftarrow h(x)$$

 $S(x, y) \leftarrow p(x, w) \land S(v, w) \land p(y, v)$

with query S(1, x). \sim Query rule: Query $(x) \leftarrow S(1, x)$

Transformed rules:

Query^f(x)
$$\leftarrow$$
 S^{bf}(1,x)
S^{bf}(x,x) \leftarrow h(x)
S^{bf}(x,y) \leftarrow p(x,w) \wedge S^{fb}(v,w) \wedge p(y,v)
S^{fb}(x,x) \leftarrow h(x)
S^{fb}(x,y) \leftarrow p(x,w) \wedge S^{fb}(v,w) \wedge p(y,v)

QSQR Algorithm

Evaluation of query in QSQR:

Given: a Datalog program P and a conjunctive query $q[\vec{x}]$ (possibly with constants)

- (1) Create an adorned program P^a :
 - Turn the query $q[\vec{x}]$ into an adorned rule Query $q[\vec{x}] \leftarrow q[\vec{x}]$
 - Recursively create adorned rules from rules in P for all adorned predicates in P^a.
- (2) Initialise all auxiliary relations to empty sets.
- (3) Evaluate the rule Query $f^{f..f}(\vec{x}) \leftarrow q[\vec{x}]$. Repeat until no new tuples are added to any QSQ relation.
- (4) Return output^{ff...f}_{Query}.

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Magic

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Magic Sets

QSQ(R) is a goal directed procedure: it tries to derive results for a specific query.

Semi-naive evaluation is not goal directed: it computes all entailed facts.

Can a bottom-up technique be goal-directed?
→ yes, by magic

Magic Sets

- "Simulation" of QSQ by Datalog rules
- Can be evaluated bottom up, e.g., with semi-naive evaluation
- The "magic sets" are the sets of tuples stored in the auxiliary relations
- · Several other variants of the method exist

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Magic Sets as Simulation of QSQ (2)

Observation: $\sup_{0}(x)$ and $\sup_{2}(x,z)$ are redundant. Simpler:

$$\sup_{\mathbf{I}}(x,y) \leftarrow \operatorname{input}_{\mathbf{T}}^{bf}(x) \wedge \operatorname{output}_{\mathbf{T}}^{bf}(x,y)$$

$$\operatorname{output}_{\mathbf{T}}^{bf}(x,z) \leftarrow \sup_{\mathbf{I}}(x,y) \wedge \operatorname{output}_{\mathbf{T}}^{bf}(y,z)$$

We still need to "call" subqueries recursively:

$$\mathsf{input}^{bf}_\mathsf{T}(y) \leftarrow \mathsf{sup}_1(x,y)$$

It is easy to see how to do this for arbitrary adorned rules.

Magic Sets as Simulation of QSQ

Idea: the information flow in QSQ(R) mainly uses join and projection → can we just implement this in Datalog?

Example 15.5: The QSQ information flow

could be expressed using rules:

$$\begin{split} \sup_0(x) &\leftarrow \mathsf{input}_\mathsf{T}^{bf}(x) \\ \sup_1(x,y) &\leftarrow \mathsf{sup}_0(x) \land \mathsf{output}_\mathsf{T}^{bf}(x,y) \\ \sup_2(x,z) &\leftarrow \mathsf{sup}_1(x,y) \land \mathsf{output}_\mathsf{T}^{bf}(y,z) \\ \mathsf{output}_\mathsf{T}^{bf}(x,z) &\leftarrow \mathsf{sup}_2(x,z) \end{split}$$

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A Note on Constants

Constants in rule bodies must lead to bindings in the subquery.

Example 15.6: The following rule is correctly adorned

$$\mathsf{R}^{bf}(x,y) \leftarrow \mathsf{T}^{bbf}(x,a,y)$$

This leads to the following rules using Magic Sets:

$$\begin{split} \text{output}_{\mathsf{R}}^{bf}(x,y) &\leftarrow \mathsf{input}_{\mathsf{R}}^{bf}(x) \land \mathsf{output}_{\mathsf{T}}^{bbf}(x,a,y) \\ \mathsf{input}_{\mathsf{T}}^{bf}(x,a) &\leftarrow \mathsf{input}_{\mathsf{R}}^{bf}(x) \end{split}$$

Note that we do not need to use auxiliary predicates \sup_0 or \sup_1 here, by the simplification on the previous slide.

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Magic Sets: Summary

A goal-directed bottom-up technique:

- Rewritten program rules can be constructed on the fly
- Bottom-up evaluation can be semi-naive (avoid repeated rule applications)
- Supplementary relations can be cached in between queries

Nevertheless, a full materialisation might be better, if

- Database does not change very often (materialisation as one-time investment)
- Queries are very diverse and may use any IDB relation (bad for caching supplementary relations)
- → semi-naive evaluation is still very common in practice

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How to Implement Datalog

We saw several evaluation methods:

- · Semi-naive evaluation
- QSQ(R)
- Magic Sets

Don't we have enough algorithms by now?

No. In fact, we are still far from actual algorithms.

Issues on the way from "evaluation method" to basic algorithm:

- Data structures! (Especially: how to store derivations?)
- Joins! (low-level algorithms; optimisations)
- Duplicate elimination! (major performance factor)
- Optimisations! (further ideas for reducing redundancy)
- Parallelism! (using multiple CPUs)

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Implementation

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slide 22 of 27

General concerns

System implementations need to decide on their mode of operation:

- Interactive service vs. batch process
- Scale? (related: what kind of memory and compute infrastructure to target?)
- Computing the complete least model vs. answering specific queries
- Static vs. dynamic inputs (will data change? will rules change?)
- Which data sources should be supported?
- Should results be cached? Do we to update caches (view maintenance)?
- Is intra-query parallelism desirable? On which level and for how many CPUs?
- ...

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Datalog as a Special Case

Datalog is a special case of many approaches, leading to very diverse implementation techniques.

- Prolog is essentially "Datalog with function symbols" (and many built-ins).
- Answer Set Programming is "Datalog extended with non-monotonic negation and disjunction"
- Production Rules use "bottom-up rule reasoning with operational, non-monotonic built-ins"
- Recursive SQL Queries are a syntactically restricted set of Datalog rules
- → Different scenarios, different optimal solutions
- → Not all implementations are complete (e.g., Prolog)

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Summary and Outlook

Several implementation techniques for Datalog

- bottom up (from the data) or top down (from the guery)
- goal-directed (for a query) or not

Top-down: Query-Subquery (QSQ) approach (goal-directed)

Bottom-up:

- naive evaluation (not goal-directed)
- semi-naive evaluation (not goal-directed)
- Magic Sets (goal-directed)

Next topics:

- · Graph databases and path queries
- Dependencies

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Datalog Implementation in Practice

Dedicated Datalog engines as of 2018 (incomplete):

- RDFox Fast in-memory RDF database with runtime materialisation and updates
- VLog Fast in-memory Datalog materialisation with bindings to several databases, including RDF and RDBMS (co-developed at TU Dresden)
- Llunatic PostgreSQL-based implementation of a rule engine
- Graal In-memory rule engine with RDBMS bindings
- SociaLite and EmptyHeaded Datalog-based languages and engines for social network analysis
- DeepDive Data analysis platform with support for Datalog-based language "DDlog"
- LogicBlox Big data analytics platform that uses Datalog rules (commercial, discontinued?)
- DLV Answer set programming engine that is usable on Datalog programs (commercial)
- Datomic Distributed, versioned database using Datalog as main query language (commercial)
- E Fast theorem prover for first-order logic with equality; can be used on Datalog as well

slide 26 of 27

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→ Extremely diverse tools for very different requirements

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