

DATABASE THEORY

Lecture 15: Datalog Evaluation (2)

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Knowledge-Based Systems

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Semi-Naive Evaluation: Example

$$e(1,2)$$
 $e(2,3)$ $e(3,4)$ $e(4,5)$

(R1)
$$\mathsf{T}(x,y) \leftarrow \mathsf{e}(x,y)$$

(R2.1)
$$\mathsf{T}(x,z) \leftarrow \Delta^i_\mathsf{T}(x,y) \wedge \mathsf{T}^i(y,z)$$

$$(R2.2') \qquad \mathsf{T}(x,z) \leftarrow \mathsf{T}^{i-1}(x,y) \wedge \Delta_\mathsf{T}^i(y,z)$$

How many body matches do we need to iterate over?

$$T_P^0 = \emptyset$$
 initialisation

$$T_P^1 = \{\mathsf{T}(1,2), \mathsf{T}(2,3), \mathsf{T}(3,4), \mathsf{T}(4,5)\} \quad 4 \times (R1)$$

$$T_P^2 = T_P^1 \cup \{\mathsf{T}(1,3), \mathsf{T}(2,4), \mathsf{T}(3,5)\}$$
 $3 \times (R2.1)$

$$T_P^3 = T_P^2 \cup \{\mathsf{T}(1,4), \mathsf{T}(2,5), \mathsf{T}(1,5)\}$$
 $3 \times (R2.1), 2 \times (R2.2')$

In total, we considered 14 matches to derive 11 facts

Review: Datalog Evaluation

A rule-based recursive query language

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\begin{aligned} & \text{father(alice, bob)} \\ & \text{mother(alice, carla)} \\ & & \text{Parent}(x,y) \leftarrow \text{father}(x,y) \\ & \text{Parent}(x,y) \leftarrow \text{mother}(x,y) \\ & \text{SameGeneration}(x,x) \\ & \text{SameGeneration}(x,y) \leftarrow \text{Parent}(x,v) \land \text{Parent}(y,w) \land \text{SameGeneration}(v,w) \end{aligned}
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Perfect static optimisation for Datalog is undecidable

Datalog queries can be evaluated bottom-up or top-down

Simplest practical bottom-up technique: semi-naive evaluation

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Semi-Naive Evaluation: Full Definition

In general, a rule of the form

$$H(\vec{x}) \leftarrow e_1(\vec{v}_1) \wedge \ldots \wedge e_n(\vec{v}_n) \wedge |_1(\vec{z}_1) \wedge |_2(\vec{z}_2) \wedge \ldots \wedge |_m(\vec{z}_m)$$

is transformed into m rules

$$\begin{split} & H(\vec{x}) \leftarrow e_1(\vec{y}_1) \wedge \ldots \wedge e_n(\vec{y}_n) \wedge \Delta^i_{l_1}(\vec{z}_1) \wedge l^i_2(\vec{z}_2) \wedge \ldots \wedge l^i_m(\vec{z}_m) \\ & H(\vec{x}) \leftarrow e_1(\vec{y}_1) \wedge \ldots \wedge e_n(\vec{y}_n) \wedge l^{i-1}_1(\vec{z}_1) \wedge \Delta^i_{l_2}(\vec{z}_2) \wedge \ldots \wedge l^i_m(\vec{z}_m) \\ & \ldots \\ & H(\vec{x}) \leftarrow e_1(\vec{y}_1) \wedge \ldots \wedge e_n(\vec{y}_n) \wedge l^{i-1}_1(\vec{z}_1) \wedge l^{i-1}_2(\vec{z}_2) \wedge \ldots \wedge \Delta^i_1(\vec{z}_m) \end{split}$$

Advantages and disadvantages:

- Huge improvement over naive evaluation
- Some redundant computations remain (see example)
- Some overhead for implementation (store level of entailments)

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Top-Down Evaluation

Idea: we may not need to compute all derivations to answer a particular query

Example 15.1:

The answers to Query are the T-successors of 2.

However, bottom-up computation would also produce facts like T(1,4), which are neither directly nor indirectly relevant for computing the query result.

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Query-Subquery (QSQ)

QSQ is a technique for organising top-down Datalog query evaluation

Main principles:

- Apply backward chaining/resolution: start with query, find rules that can derive query, evaluate body atoms of those rules (subqueries) recursively
- Evaluate intermediate results "set-at-a-time" (using relational algebra on tables)
- Evaluate queries in a "data-driven" way, where operations are applied only to newly computed intermediate results (similar to idea in semi-naive evaluation)
- "Push" variable bindings (constants) from heads (queries) into bodies (subqueries)
- "Pass" variable bindings (constants) "sideways" from one body atom to the next

Details can be realised in several ways.

Assumption

Assumption: For all techniques presented in this lecture, we assume that the given Datalog program is safe.

- This is without loss of generality (as shown in exercise).
- One can avoid this by adding more cases to algorithms.

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Adornments

To guide evaluation, we distinguish free and bound parameters in a predicate.

Example 15.2: If we want to derive atom T(2, z) from the rule $T(x, z) \leftarrow T(x, y) \land T(y, z)$, then x will be bound to 2, while z is free.

We use adornments to denote the free/bound parameters in predicates.

Example 15.3:

$$\mathsf{T}^{bf}(x,z) \leftarrow \mathsf{T}^{bf}(x,y) \wedge \mathsf{T}^{bf}(y,z)$$

- since x is bound in the head, it is also bound in the first atom
- any match for the first atom binds y, so y is bound when evaluating the second atom (in left-to-right evaluation)

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Adornments: Examples

The adornment of the head of a rule determines the adornments of the body atoms:

$$\mathsf{R}^{bbb}(x, y, z) \leftarrow \mathsf{R}^{bbf}(x, y, v) \wedge \mathsf{R}^{bbb}(x, v, z)$$
$$\mathsf{R}^{fbf}(x, y, z) \leftarrow \mathsf{R}^{fbf}(x, y, v) \wedge \mathsf{R}^{bbf}(x, v, z)$$

The order of body predicates affects the adornment:

$$\begin{split} \mathbf{S}^{fff}(x,y,z) \leftarrow \mathbf{T}^{ff}(x,v) \wedge \mathbf{T}^{ff}(y,w) \wedge \mathbf{R}^{bbf}(v,w,z) \\ \mathbf{S}^{fff}(x,y,z) \leftarrow \mathbf{R}^{fff}(v,w,z) \wedge \mathbf{T}^{fb}(x,v) \wedge \mathbf{T}^{fb}(y,w) \end{split}$$

→ For optimisation, some orders might be better than others

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Auxiliary Relations for QSQ (2)

When evaluating body atoms from left to right, we use supplementary relations sup,

- → bindings required to evaluate rest of rule after the ith body atom
- \rightarrow the first set of bindings \sup_0 comes from $input_R^{\alpha}$
- \rightarrow the last set of bindings \sup_n go to $\operatorname{output}_R^\alpha$

Example 15.4:

$$\begin{split} \mathsf{T}^{bf}(x,z) \leftarrow \mathsf{T}^{bf}(x,y) \wedge \mathsf{T}^{bf}(y,z) \\ & \qquad \\ \mathsf{input}_\mathsf{T}^{bf} \Rightarrow \mathsf{sup}_0[x] \quad \mathsf{sup}_1[x,y] \quad \mathsf{sup}_2[x,z] \Rightarrow \mathsf{output}_\mathsf{T}^{bf} \end{split}$$

- $\sup_0[x]$ is copied from $\operatorname{input}_T^{bf}[x]$ (with some exceptions, see exercise)
- $\sup_{1}[x, y]$ is obtained by joining tables $\sup_{0}[x]$ and $\operatorname{output}_{T}^{bf}[x, y]$
- $\sup_2[x, z]$ is obtained by joining tables $\sup_1[x, y]$ and $\operatorname{output}_T^{bf}[y, z]$
- output $_{\mathsf{T}}^{bf}[x,z]$ is copied from $\sup_{z}[x,z]$

(we use "named" notation like [x, y] to suggest what to join on; the relations are the same)

Auxiliary Relations for QSQ

To control evaluation, we store intermediate results in auxiliary relations.

When we "call" a rule with a head where some variables are bound, we need to provide the bindings as input

- \rightarrow for adorned relation R^{α} , we use an auxiliary relation input_R
- \rightarrow arity of input^{α}_B = number of b in α

The result of calling a rule should be the "completed" input, with values for the unbound variables added

- \rightarrow for adorned relation R^{α} , we use an auxiliary relation output
- \rightarrow arity of output^{α}_R = arity of R (= length of α)

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QSQ Evaluation

The set of all auxiliary relations is called a QSQ template (for the given set of adorned rules)

General evaluation:

- add new tuples to auxiliary relations until reaching a fixed point
- evaluation of a rule can proceed as sketched on previous slide
- in addition, whenever new tuples are added to a sup relation that feeds into an IDB atom, the input relation of this atom is extended to include all binding given by sup (may trigger subquery evaluation)
- \rightarrow there are many strategies for implementing this general scheme

Notation:

• for an EDB atom A, we write $A^{\mathcal{I}}$ for table that consists of all matches for A in the database

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Recursive QSQ

Recursive QSQ (QSQR) takes a "depth-first" approach to QSQ

Evaluation of single rule in QSQR:

Given: adorned rule r with head predicate R^{α} ; current values of all QSQ relations

- (1) Copy tuples input^{α}_B (that unify with rule head) to sup^r₀
- (2) For each body atom A_1, \ldots, A_n , do:
 - If A_i is an EDB atom, compute $\sup_{i=1}^r$ as projection of $\sup_{i=1}^r \bowtie A_i^I$
 - If A_i is an IDB atom with adorned predicate S^{β} :
 - (a) Add new bindings from $\sup_{i=1}^r$, combined with constants in $A_i,$ to input $^\beta_{\rm S}$
 - (b) If input $^{\!\beta}_{\rm S}$ changed, recursively evaluate all rules with head predicate ${\bf S}^{\!\beta}$
 - (c) Compute $\sup_{i=1}^{r} as$ projection of $\sup_{i=1}^{r} \bowtie output_{S}^{\beta}$
- (3) Add tuples in $\sup_{n=1}^{r}$ to $\operatorname{output}_{R}^{\alpha}$

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QSQR Transformation: Example

Predicates S (same generation), p (parent), h (human)

$$S(x, x) \leftarrow h(x)$$

 $S(x, y) \leftarrow p(x, w) \land S(v, w) \land p(y, v)$

with query S(1, x).

 \rightarrow Query rule: Query(x) \leftarrow S(1, x)

Transformed rules:

$$\begin{aligned} & \mathsf{Query}^f(x) \leftarrow \mathsf{S}^{bf}(1,x) \\ & \mathsf{S}^{bf}(x,x) \leftarrow \mathsf{h}(x) \\ & \mathsf{S}^{bf}(x,y) \leftarrow \mathsf{p}(x,w) \land \mathsf{S}^{fb}(v,w) \land \mathsf{p}(y,v) \\ & \mathsf{S}^{fb}(x,x) \leftarrow \mathsf{h}(x) \\ & \mathsf{S}^{fb}(x,y) \leftarrow \mathsf{p}(x,w) \land \mathsf{S}^{fb}(v,w) \land \mathsf{p}(y,v) \end{aligned}$$

QSQR Algorithm

Evaluation of query in QSQR:

Given: a Datalog program P and a conjunctive query $q[\vec{x}]$ (possibly with constants)

- (1) Create an adorned program P^a :
 - Turn the query $q[\vec{x}]$ into an adorned rule Query $f(\vec{x}) \leftarrow q[\vec{x}]$
 - Recursively create adorned rules from rules in P for all adorned predicates in P^a.
- (2) Initialise all auxiliary relations to empty sets.
- (3) Evaluate the rule $Query^{f...f}(\vec{x}) \leftarrow q[\vec{x}]$. Repeat until no new tuples are added to any QSQ relation.
- (4) Return output $f_{Query}^{f...f}$.

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Magic

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Magic Sets

QSQ(R) is a goal directed procedure: it tries to derive results for a specific query.

Semi-naive evaluation is not goal directed: it computes all entailed facts.

Can a bottom-up technique be goal-directed?
→ yes, by magic

Magic Sets

- "Simulation" of QSQ by Datalog rules
- Can be evaluated bottom up, e.g., with semi-naive evaluation
- The "magic sets" are the sets of tuples stored in the auxiliary relations
- · Several other variants of the method exist

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Magic Sets as Simulation of QSQ (2)

Observation: $\sup_{0}(x)$ and $\sup_{2}(x, z)$ are redundant. Simpler:

$$\sup_{\mathbf{T}}(x,y) \leftarrow \operatorname{input}_{\mathbf{T}}^{bf}(x) \wedge \operatorname{output}_{\mathbf{T}}^{bf}(x,y)$$

$$\operatorname{output}_{\mathbf{T}}^{bf}(x,z) \leftarrow \sup_{\mathbf{T}}(x,y) \wedge \operatorname{output}_{\mathbf{T}}^{bf}(y,z)$$

We still need to "call" subqueries recursively:

$$\mathsf{input}^{bf}_\mathsf{T}(y) \leftarrow \mathsf{sup}_1(x,y)$$

It is easy to see how to do this for arbitrary adorned rules.

Magic Sets as Simulation of QSQ

Idea: the information flow in QSQ(R) mainly uses join and projection → can we just implement this in Datalog?

Example 15.5: The QSQ information flow

$$\begin{split} \mathsf{T}^{bf}(x,z) \leftarrow \mathsf{T}^{bf}(x,y) \wedge \mathsf{T}^{bf}(y,z) \\ & \qquad \\ \mathsf{input}_\mathsf{T}^{bf} \Rightarrow \mathsf{sup}_0[x] \quad \mathsf{sup}_1[x,y] \quad \mathsf{sup}_2[x,z] \Rightarrow \mathsf{output}_\mathsf{T}^{bf} \end{split}$$

could be expressed using rules:

$$\begin{split} \sup_0(x) &\leftarrow \mathsf{input}_\mathsf{T}^{bf}(x) \\ \sup_1(x,y) &\leftarrow \mathsf{sup}_0(x) \land \mathsf{output}_\mathsf{T}^{bf}(x,y) \\ \sup_2(x,z) &\leftarrow \mathsf{sup}_1(x,y) \land \mathsf{output}_\mathsf{T}^{bf}(y,z) \\ \mathsf{output}_\mathsf{T}^{bf}(x,z) &\leftarrow \mathsf{sup}_2(x,z) \end{split}$$

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A Note on Constants

Constants in rule bodies must lead to bindings in the subquery.

Example 15.6: The following rule is correctly adorned

$$\mathsf{R}^{bf}(x,y) \leftarrow \mathsf{T}^{bbf}(x,a,y)$$

This leads to the following rules using Magic Sets:

$$\begin{aligned} \mathsf{output}^{bf}_\mathsf{R}(x,y) &\leftarrow \mathsf{input}^{bf}_\mathsf{R}(x) \land \mathsf{output}^{bbf}_\mathsf{T}(x,a,y) \\ \mathsf{input}^{bbf}_\mathsf{T}(x,a) &\leftarrow \mathsf{input}^{bf}_\mathsf{R}(x) \end{aligned}$$

Note that we do not need to use auxiliary predicates \sup_0 or \sup_1 here, by the simplification on the previous slide.

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Magic Sets: Summary

A goal-directed bottom-up technique:

- Rewritten program rules can be constructed on the fly
- Bottom-up evaluation can be semi-naive (avoid repeated rule applications)
- Supplementary relations can be cached in between gueries

Nevertheless, a full materialisation might be better, if

- Database does not change very often (materialisation as one-time investment)
- Queries are very diverse and may use any IDB relation (bad for caching supplementary relations)

→ semi-naive evaluation is still very common in practice

Implementation

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How to Implement Datalog

We saw several evaluation methods:

- Semi-naive evaluation
- QSQ(R)
- Magic Sets

Don't we have enough algorithms by now?

No. In fact, we are still far from actual algorithms.

Issues on the way from "evaluation method" to basic algorithm:

- Data structures! (Especially: how to store derivations?)
- Joins! (low-level algorithms; optimisations)
- Duplicate elimination! (major performance factor)
- Optimisations! (further ideas for reducing redundancy)
- Parallelism! (using multiple CPUs)

• . . .

General concerns

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System implementations need to decide on their mode of operation:

- Interactive service vs. batch process
- Scale? (related: what kind of memory and compute infrastructure to target?)
- Computing the complete least model vs. answering specific queries
- Static vs. dynamic inputs (will data change? will rules change?)
- Which data sources should be supported?
- Should results be cached? Do we to update caches (view maintenance)?
- Is intra-query parallelism desirable? On which level and for how many CPUs?
- ...

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Datalog as a Special Case

Datalog is a special case of many approaches, leading to very diverse implementation techniques.

- Prolog is essentially "Datalog with function symbols" (and many built-ins).
- Answer Set Programming is "Datalog extended with non-monotonic negation and disjunction"
- Production Rules use "bottom-up rule reasoning with operational, non-monotonic built-ins"
- Recursive SQL Queries are a syntactically restricted set of Datalog rules
- → Different scenarios, different optimal solutions
- → Not all implementations are complete (e.g., Prolog)

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Summary and Outlook

Several implementation techniques for Datalog

- bottom up (from the data) or top down (from the query)
- goal-directed (for a guery) or not

Top-down: Query-Subquery (QSQ) approach (goal-directed)

Bottom-up:

- naive evaluation (not goal-directed)
- semi-naive evaluation (not goal-directed)
- Magic Sets (goal-directed)

Next topics:

- Graph databases and path queries
- Dependencies

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Datalog Implementation in Practice

Dedicated Datalog engines as of 2018 (incomplete):

- RDFox Fast in-memory RDF database with runtime materialisation and updates
- VLog Fast in-memory Datalog materialisation with bindings to several databases, including RDF and RDBMS (co-developed at TU Dresden)
- Llunatic PostgreSQL-based implementation of a rule engine
- Graal In-memory rule engine with RDBMS bindings
- SociaLite and EmptyHeaded Datalog-based languages and engines for social network analysis
- DeepDive Data analysis platform with support for Datalog-based language "DDlog"
- LogicBlox Big data analytics platform that uses Datalog rules (commercial, discontinued?)
- DLV Answer set programming engine that is usable on Datalog programs (commercial)
- Datomic Distributed, versioned database using Datalog as main query language (commercial)
- E Fast theorem prover for first-order logic with equality; can be used on Datalog as well
- ..

→ Extremely diverse tools for very different requirements

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