



International Center for Computational Logic

KNOWLEDGE GRAPHS

Lecture 1: Introduction

Markus Krötzsch

Knowledge-Based Systems

TU Dresden, 10th Oct 2023

More recent versions of this slide deck might be available. For the most current version of this course, see https://iccl.inf.tu-dresden.de/web/Knowledge_Graphs/en

Introduction and Organisation

Course Tutors



Markus Krötzsch Lectures



Maximilian Marx Exercises

Organisation

• Lectures

Tuesday, DS 3 (11:10–12:40), room yet to be determined (watch the web page) Videos are available online:

https://youtube.com/channel/UCCvDWNsR8YlQrB1tSj9Xqsw

(see playlist "Knowledge Graphs")

• Exercise Sessions

Tuesday, DS 5 (14:50–16:20), APB E005

• Web Page

https://iccl.inf.tu-dresden.de/web/Knowledge_Graphs_(WS2023/24)

• Lecture Notes

Slides of current and past lectures will be online.

• Modules: INF-B-510, INF-B-520, INF-BAS2, INF-VERT2, INF-BAS6, INF-VERT6, INF-E-3, INF-PM-FOR, MCL-KR, MCL-TCSL, CMS-COR-KM

How exercises work

Exercise classes are interactive events:

- Tasks are published online
- Students solve the tasks before the date of the class
- In the meeting, students ask questions and present their solutions
- The tutor answers questions and helps with problems

How exercises work

Exercise classes are interactive events:

- Tasks are published online
- Students solve the tasks before the date of the class
- In the meeting, students ask questions and present their solutions
- The tutor answers questions and helps with problems

Corollary: You must do your homework to benefit from the classes.

How the examination works

The details of the examination depend on your module:

- · Most modules: oral examination, sometimes in combination with other subjects
- For students of Computational Modelling and Simulation in module CMS-LM-COR:
 - written (60min) if more than 10 examinees
 - oral (20min) otherwise

All examinations are "closed book" (no auxiliary materials allowed)

How to be prepared for examinations

Here are some hints that can help you to succeed in the examination:

- Follow the course closely during the semester
- Do all your homework
- When watching videos or attending classes: take hand-written notes
- Be prepared to reproduce most of the material that is on the slides when asked
- · Be prepared to solve tasks that are like those in the exercises
- Expect that you will have to write answers on paper (also during oral exams)

How to be prepared for examinations

Here are some hints that can help you to succeed in the examination:

- Follow the course closely during the semester
- Do all your homework
- When watching videos or attending classes: take hand-written notes
- Be prepared to reproduce most of the material that is on the slides when asked
- · Be prepared to solve tasks that are like those in the exercises
- Expect that you will have to write answers on paper (also during oral exams)

Main conclusion: You need to be able to produce knowledge and solutions actively rather than merely understanding them passively.

Goals and Prerequisites

Goals

- Introduce basic notions of graph-based knowledge representation(s)
- Study important graph data management approaches (RDF, Property Graph) and query languages
- Learn about relevant methods, tools, and datasets
- Discuss aspects of modelling and quality assurance
- Get to know some methods for analysing networks and graphs

(Non-)Prerequisites

- No particular prior courses needed
- Basic programming skills are assumed; practical experience beyond basic courses will be helpful
- Interesting optional synergies: databases, machine learning, social networks, graph theory

Course Outline

• Resource Description Framework (RDF)

Underlying graph model; URIs; syntax

• SPARQL

Query features; syntax and semantics; expressive power and complexlity

• Property graph

Underlying graph model; syntax and semantics of Cypher

• Wikidata

Data model; applications; aspects of modelling; query answering

Ontologies and rules

Datalog; negation; existential rules; ontological models; OWL

RDF constraint languages

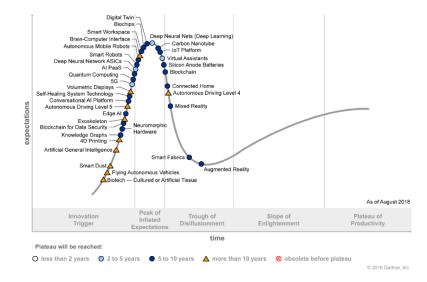
SHACL & ShEX; syntax and semantics; complexity and implementation

• Network analysis

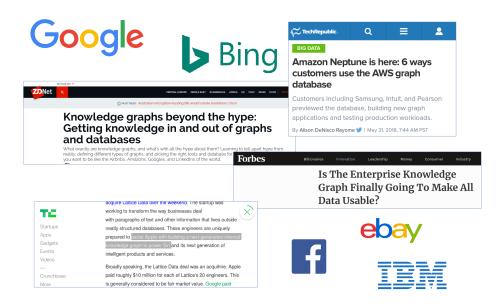
Centrality measures, PageRank, community detection

Motivation

The Hype



Knowledge Graphs Everywhere



The original "Knowledge Graph" (Google, 2012):

Google Inside Search Home How Search Works Tips & Tricks Features Search Stories Playground Blog Help The Knowledge Graph See it in action Learn more about one of the key breakthroughs Discover answers to questions you never behind the future of search thought to ask, and explore collections and lists.

Many knowledge graphs, many technologies

There are a number of widely used publicly available knowledge graphs:











... and a variety of technologies for working with them:









Markus Krötzsch, 10th Oct 2023

Knowledge Graphs

A first attempt at a definition:

A Knowledge Graph is a knowledge base that is a graph.

A first attempt at a definition:

A Knowledge Graph is a knowledge base that is a graph.

So what is a knowledge base?

A first attempt at a definition:

A Knowledge Graph is a knowledge base that is a graph.

So what is a knowledge base?

- "A knowledge base is a technology used to store complex structured and unstructured information used by a computer system. [...] [It] represents facts about the world" – Wikipedia (26 Oct 2020, id 983269427)
- "A collection of knowledge expressed using some formal knowledge representation language." Free Online Dictionary of Computing, 15 Oct 2018
- 1. a store of information or data that is available to draw on.
 - 2. the underlying set of facts, assumptions, and rules which a computer system has available to solve a problem.
 - Lexico (Oxford University Press/Dictionary.com), 26 Oct 2020

A first attempt at a definition:

A Knowledge Graph is a knowledge base that is a graph.

So what is a graph?

A first attempt at a definition:

A Knowledge Graph is a knowledge base that is a graph.

So what is a graph?

- "a collection of points and lines connecting some (possibly empty) subset of them"
 Wolfram MathWorld, 26 Oct 2020
- "a collection of vertices and edges that join pairs of vertices" Merriam-Webster, 26 Oct 2020
- "a structure amounting to a set of objects in which some pairs of the objects are in some sense 'related'." Wikipedia (26 Oct 2020, id 984093316)

(we'll have more to say about mathematical graphs later)

A first attempt at a definition:

A Knowledge Graph is a knowledge base that is a graph.

In summary:

A first attempt at a definition:

A Knowledge Graph is a knowledge base that is a graph.

In summary:

- a collection of facts, rules, or other forms of knowledge
- · that express some kind of relationships or connections
- \rightsquigarrow a paradigm rather than a specific class of things

What is special about Knowledge Graphs?

A second attempt at a definition:

A Knowledge Graph is a data set that is:

- structured (in the form of a specific data structure)
- normalised (consisting of small units, such as vertices and edges)
- connected (defined by the possibly distant connections between objects)

Moreover, knowledge graphs are typically:

- explicit (created purposefully with an intended meaning)
- declarative (meaningful in itself, independent of a particular implementation or algorithm)
- annotated (enriched with contextual information to record additional details and meta-data)
- non-hierarchical (more than just a tree-structure)
- large (millions rather than hundreds of elements)

Typical knowledge graphs:

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

Debatable cases:

• Facebook's social graph: structured, normalised, connected, but not explicit (emerging from user interactions, without intended meaning beyond local relations)

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

- Facebook's social graph: structured, normalised, connected, but not explicit (emerging from user interactions, without intended meaning beyond local relations)
- WordNet: structured dictionary and thesaurus, but with important unstructured content (descriptions); explicit, declarative model

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

- Facebook's social graph: structured, normalised, connected, but not explicit (emerging from user interactions, without intended meaning beyond local relations)
- WordNet: structured dictionary and thesaurus, but with important unstructured content (descriptions); explicit, declarative model
- Global data from schema.org: maybe not very connected

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

- Facebook's social graph: structured, normalised, connected, but not explicit (emerging from user interactions, without intended meaning beyond local relations)
- WordNet: structured dictionary and thesaurus, but with important unstructured content (descriptions); explicit, declarative model
- Global data from schema.org: maybe not very connected
- Document stores (Lucene, MongoDB, etc.): structured, but not normalised; connections sub-ordinary

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

Debatable cases:

- Facebook's social graph: structured, normalised, connected, but not explicit (emerging from user interactions, without intended meaning beyond local relations)
- WordNet: structured dictionary and thesaurus, but with important unstructured content (descriptions); explicit, declarative model
- Global data from schema.org: maybe not very connected
- Document stores (Lucene, MongoDB, etc.): structured, but not normalised; connections sub-ordinary

Primarily not knowledge graphs:

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

Debatable cases:

- Facebook's social graph: structured, normalised, connected, but not explicit (emerging from user interactions, without intended meaning beyond local relations)
- WordNet: structured dictionary and thesaurus, but with important unstructured content (descriptions); explicit, declarative model
- Global data from schema.org: maybe not very connected
- Document stores (Lucene, MongoDB, etc.): structured, but not normalised; connections sub-ordinary

Primarily not knowledge graphs:

• Wikipedia: mostly unstructured text; not normalised; connections (links) important but sub-ordinary (similar: The Web)

Typical knowledge graphs:

- Wikidata, Yago 2, Freebase, DBpedia (though hardly annotated)
- OpenStreetMap
- Google Knowledge Graph, Microsoft Bing Satori (presumably; we can't really know)

Debatable cases:

- Facebook's social graph: structured, normalised, connected, but not explicit (emerging from user interactions, without intended meaning beyond local relations)
- WordNet: structured dictionary and thesaurus, but with important unstructured content (descriptions); explicit, declarative model
- Global data from schema.org: maybe not very connected
- Document stores (Lucene, MongoDB, etc.): structured, but not normalised; connections sub-ordinary

Primarily not knowledge graphs:

- Wikipedia: mostly unstructured text; not normalised; connections (links) important but sub-ordinary (similar: The Web)
- Relational database of company X: structured and possibly normalised, but no focus on connections (traditional RDBMS support connectivity queries only poorly)

Graphs in Computer Science and Mathematics

What is a graph?

Definition 1.1: A simple undirected graph *G* consists of a set *V* of vertices and a set *E* of edges, where each edge is a set of two vertices. Two vertices $v_1, v_2 \in V$ are adjacent (in *G*) if there is an edge $\{v_1, v_2\} \in E$.

Vertices are sometimes also called nodes; undirected edges are sometimes also called arcs.

Unless otherwise noted, we assume all graphs to be finite.

What is a graph?

Definition 1.1: A simple undirected graph *G* consists of a set *V* of vertices and a set *E* of edges, where each edge is a set of two vertices. Two vertices $v_1, v_2 \in V$ are adjacent (in *G*) if there is an edge $\{v_1, v_2\} \in E$.

Vertices are sometimes also called nodes; undirected edges are sometimes also called arcs.

Unless otherwise noted, we assume all graphs to be finite.

Discrete mathematics considers a variety of other kinds of "graphs":

- Directed or undirected
- Simple graph or multi-graph
- Possibly labelled edges or vertices
- Possibly with self-loops
- Possibly with higher arity edges (hypergraphs)

Directed and other graphs

Definition 1.2: A simple directed graph (a.k.a. simple digraph) *G* consists of a set *V* of vertices and a set $E \subseteq V \times V$ of (directed) edges from a source vertex to a target vertex.

Other terms are similar to undirected graphs; directed edges are also known as arrows and are often denoted as such, e.g., $v_1 \stackrel{e_1}{\rightarrow} v_2$.

Directed and other graphs

Definition 1.2: A simple directed graph (a.k.a. simple digraph) *G* consists of a set *V* of vertices and a set $E \subseteq V \times V$ of (directed) edges from a source vertex to a target vertex.

Other terms are similar to undirected graphs; directed edges are also known as arrows and are often denoted as such, e.g., $v_1 \stackrel{e_1}{\rightarrow} v_2$.

Definition 1.3: The following generalisations apply to directed and to undirected graphs.

- A graph with self-loops is a graph extended with the option of having edges that relate a vertex to itself.
- A multi-graph is a graph that may have multiple edges with the same vertices (in the same direction).
- An edge-labelled graph is a graph that has an additional labelling function $\lambda : E \to L$ that maps each edge in *E* to an element from a set of labels *L* (similarly for vertex-labelled graphs).

Other basic notions

Definition 1.4: An edge are said to be incidental to the vertices it connects. The degree of a vertex is the number of edges that are incidental to it. In a digraph, the in-degree of a vertex is the number of edges pointing towards it; analogously for out-degree.

Other basic notions

Definition 1.4: An edge are said to be incidental to the vertices it connects. The degree of a vertex is the number of edges that are incidental to it. In a digraph, the in-degree of a vertex is the number of edges pointing towards it; analogously for out-degree.

Definition 1.5: A directed path in a digraph is a sequence of consecutive edges $v_0 \xrightarrow{e_1} v_1 \xrightarrow{e_2} \cdots \xrightarrow{e_n} v_n$. An undirected path is a sequence of edges that may point either way (or that are simply undirected).

A simple path (directed or undirected) is a path without repeated vertices other than possibly the first and last node.

Other basic notions

Definition 1.4: An edge are said to be incidental to the vertices it connects. The degree of a vertex is the number of edges that are incidental to it. In a digraph, the in-degree of a vertex is the number of edges pointing towards it; analogously for out-degree.

Definition 1.5: A directed path in a digraph is a sequence of consecutive edges $v_0 \xrightarrow{e_1} v_1 \xrightarrow{e_2} \cdots \xrightarrow{e_n} v_n$. An undirected path is a sequence of edges that may point either way (or that are simply undirected).

A simple path (directed or undirected) is a path without repeated vertices other than possibly the first and last node.

Definition 1.6: Two vertices are connected if there is an undirected path from one to the other. A graph is connected if any pair of two distinct vertices is connected. A digraph is strongly connected if there is a directed path from any vertex to any other vertex (hence: one directed path in either direction).

Representing graphs (1)

There are several obvious ways of representing graphs in computer science.

Definition 1.7: The adjacency matrix of a graph $G = \langle V, E \rangle$ is the boolean $|V| \times |V|$ matrix that contains, at any coordinate $\langle v_1, v_2 \rangle$, the value **1** if there is an edge connecting v_1 and v_2 .

Notes:

- Adjacency matrices for undirected graphs are symmetric.
- Loops (if allowed) show up as 1 in the diagonal.
- The matrix could be adapted to multi-graphs by storing the numbers of edges.
- The matrix could be adapted to labelled simple graphs by storing the labels.

Representing graphs (2)

There are several obvious ways of representing graphs in computer science.

Definition 1.8: The adjacency list of a graph $G = \langle V, E \rangle$ is the list of all of its edges.

Notes:

- We can write edges as pairs (order is irrelevant for undirected graphs).
- Loops (if allowed) show up as edges with repeated vertices.
- The list could be adapted to multi-graphs by adding the number of edges to each line, or by allowing repeated lines.
- The list could be adapted to labelled graphs by adding labels to each line (for multi-graph: repeat lines rather than also storing number).
- The list does not encode *V*: vertices without edges are missing (might be listed separately if relevant to application)

There are also other options.

Example 1.9: We could also encode the adjacency matrix by giving, for each row, a list of all vertices whose column is set to 1. This is equivalent to ordering edges by first vertex and combining them into a single line.

Which graph representation to pick?

Each representation has its pros and cons:

- Matrix:
 - + space efficient for dense graphs (1 bit per edge);
 - + can be processed with matrix operations (highly parallel);
 - space inefficient for sparse graphs;
 - not natural for labelled multi-graphs
- List:
 - + space efficient for sparse graphs;
 - + easy to use for labelled multi-graphs;
 - harder to process (esp. if edge order can be random);
 - not space efficient for dense graphs

Note: Knowledge graphs are typically sparse and labelled, but parallel processing still makes matrices attractive in some applications.

Summary

The course will be 50% lectures and 50% tutorial classes

Active participation is important to succeed

Knowledge Graphs are a data management concept of practical importance

Mathematics studies various types of graphs, which can be represented by several common data structures

What's next?

- Encoding graphs in technical systems: the Resource Description Format RDF
- Formats for exchanging RDF
- Modelling knowledge in RDF graphs