

Artificial Intelligence, Computational Logic

PROBLEM SOLVING AND SEARCH IN ARTIFICIAL INTELLIGENCE

Lecture 1

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Dresden, 8th April 2019



What to expect

- The course has 12 lectures, 6 tutorials and a practical part
- Lecture is on Monday in DS 3, 11:10-12:40
- Tutorials are on Monday in DS 2, 9:20-10:50
- Schedule and lecture material will be available at course web-page https://iccl.inf.tu-dresden.de/web/Problem_Solving_ and_Search_in_Artificial_Intelligence_(SS2019)
- The practical part consists of solving (implementing) a problem and its presentation. Should be performed in groups of two, assignments will be ready at April 15th.
- 3 fixed Dates for practical part (see web-page)
 - 1) Analysis of the problem, group building
 - 2) Concept how to solve it
 - 3) Presentation of solution last questions
- DEADLINE?
- EXAM?

Literature

- Zbigniew Michalewicz and David B. Fogel. How to Solve It: Modern Heuristics, volume 2. Springer, 2004.
- Stuart J. Russell and Peter Norvig. Artificial Intelligence A Modern Approach (3. edition). Pearson Education, 2010.
- plus additional articles

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Agenda

- Introduction
- 2 Uninformed Search versus Informed Search (Best First Search, A* Search, Heuristics)
- Icocal Search, Stochastic Hill Climbing, Simulated Annealing
- 4 Tabu Search
- 5 Answer-set Programming (ASP)
- 6 Constraint Satisfaction Problems (CSP)
- 2 Evolutionary Algorithms/ Genetic Algorithms
- 8 Structural Decomposition Techniques (Tree/Hypertree Decompositions)

Two men meet on the street. One gives the other a puzzle

- A: "All three of my sons celebrate their birthday this very day! So, can you tell me how old each of them is?"
- B: "Sure, but you'll have to tell me something about them."
- A: "The product of the ages of my sons is 36."
- B: "That's fine but I need more than just this."
- A: "The sum of their ages is equal to the number of windows in that building."
- B: "Still, I need an additional hint to solve your puzzle."
- A: "My oldest son has blue eyes."
- B: "Oh, this is sufficient!"



"The product of the ages of my sons is 36."

son 1	son 2	son 3
36	1	1
18	2	1
12	3	1
9	4	1
9	2	2
6	6	1
6	3	2
4	3	3

"The sum of their ages is equal to the number of windows in that building."

son 1	son 2	son 3
36	1	1
18	2	1
12	3	1
9	4	1
9	2	2
6	6	1
6	3	2
4	3	3

"The sum of their ages is equal to the number of windows in that building."

36	+	1	+	1	=	38
18	+	2	+	1	=	21
12	+		+	1	=	16
9	+	4	+	1	=	14
9	+	2	+	2	=	13
6	+	6	+	1	=	13
6	+	3	+	2	=	11
4	+	3	+	3	=	10

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4	+	3	+	3	=	10

"My oldest son has blue eyes."

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What was difficult on this problem?

Problem Solving

- Where to begin?
- You have to create the plan for generating a solution.
- Always consider all of the available data.
- Can you make connections between the goal and what is given?



Why are Some Problems Difficult to Solve?

- The number of possible solutions in the search space is too large for an exhaustive search.
- The problem is too complicated, and simplified models of the problem are useless.
- The evaluation function of the quality of a solution is noisy or varies with time, which requires an entire series of solutions.
- There are so many constraints that finding even one feasible answer is difficult, let alone searching for an optimal solution.
- The person solving the problem is inadequately prepared.



Boolean Satisfiability Problem (SAT)

Make a compound statement of Boolean variables evaluate to TRUE.

• For example, consider the following problem of 100 variables given in conjunctive normal form (CNF):

 $F(x) = (x_{17} \lor \neg x_{37} \lor x_{73}) \land (\neg x_{11} \lor \neg x_{56}) \land \dots \land (x_2 \lor x_{43} \lor \neg x_{77} \lor \neg x_{89} \lor \neg x_{97}).$

• Challenge: find the truth assignment for each variable x_i , for all i = 1, ..., 100 s.t. F(x) = TRUE.

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Space of possible solutions.

- Any binary string of length 100 is a possible solution.
- Two choices for each variable, and taken over 100 variables, generates 2¹⁰⁰ possibilities.

- The number of bacterial cells on Earth is estimated at around 5×10^{30} .
- If we had a computer that could test 1000 strings per second and could have started at the beginning of time itself, 15 billion years ago (Big Bang!) we would have examined fewer than 1% of all the possibilities by now!
- Trying out all alternatives is out of the question.
- Choice of which evaluation function to use.
- Solutions closer to the right answer should yield better evaluations than those who are far away.
- If we try a string *x* and *F*(*x*) returns TRUE, we are done. But what if *F*(*x*) returns FALSE?
- How to find a function which gives more than just "right" or "wrong"?

Traveling Salesperson Problem (TSP)

- Given *n* cities and the distances between each pair of cities;
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Seach Space

- Set of permutations of *n* cities.
- 2n different ways (for symmetrical TSP) to represent one tour.
- There are *n*! ways to permute *n* numbers.
- |S| = n!/(2n) = (n-1)!/2



DENMARK

GERMANY

- |S| = n!/(2n) = (n-1)!/2
- For any *n* > 6, number of possible solutions to the TSP with *n* cities is larger than the number of possible solutions to the SAT problem with *n* variables.
- For n = 6: 5!/2 = 60 solutions to the TSP and $2^6 = 64$ solutions to a SAT.
- For n = 7: 360 solutions to the TSP and 128 to the SAT.
- Search space increases very quickly with increasing *n*.
- A 50-city TSP has more solutions than existing liters of water on the planet.
- However, the evaluation function for the TSP is more straightforward than for SAT.
- Table with distances between each pair of cities.
- After *n* addition operations we could calculate the distance of any candidate tour and use this to evaluate its merit.
- $cost = dist(15, 3) + dist(3, 11) + \dots + dist(6, 15)$

Modeling the problem

- We only find the solution to a model of the problem.
- All models are simplifications of the real world.
- Problem \rightarrow Model \rightarrow Solution



- Use an approximate model of a problem and find the precise solution: Problem \rightarrow Model_a \rightarrow Solution_p(Model_a)
- 2 Use a precise model of the problem and find an approximate solution: Problem $\rightarrow Model_p \rightarrow Solution_a(Model_p)$
- Which one is better?

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- 2 Use a precise model of the problem and find an approximate solution: Problem $\rightarrow Model_p \rightarrow Solution_a(Model_p)$
- Which one is better?
- Solution_{*a*}(Model_{*p*}) is better than Solution_{*p*}(Model_{*a*}).

Change over time

Problems my change

- before you model them,
- while you derive a solution, and
- after you execute the solution.
- TSP Travel time between two cities depends on many factors:
 - traffic lights
 - slow-moving trucks
 - flat tire
 - weather
 - many more...



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Constraints

- Almost all practical problems pose constraints
- Two types of constraints:
 - Hard constraints, and
 - Soft constraints.
- Constraints make the search space smaller, but
 - It is hard to create operators that will act on feasible solution and generate in turn new feasible solutions that are an improvement of previous solution.
 - The geometry of search space gets tricky.

Timetable of the classes at a college in one semester

We are given

- list of courses that are offered;
- list of students assigned to each class;
- professors assigned to each class;
- list of available classrooms, and information for size and other facilities that each offer.



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Construct timetables that fulfill hard constraints:

- Each class must be assigned to an available room that has enough seats and requisite facilities.
- Students who are enrolled in more than one class can not have their classes held at the same time on the same day.
- Professors can not be assigned to teach courses that overlap in time.

Timetable - Soft Constraints:

- Courses that meets twice a week should preferably be assigned to Mondays and Wednesdays or Tuesdays and Thursdays.
- Courses that meets three times per week should preferably be assigned to Mondays, Wednesdays, and Fridays.
- Course time should be assigned so that students do not have to take final exams for multiple courses without any break in between.
- If more than one room satisfies the requirements for a course and is available at the designated time, the course should be assigned to the room with the capacity that is closest to the class size.

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- Any timetable that meets the hard constraints is feasible.
- The timetable has to be optimized in the light of soft constraints.
- Each soft constraint has to be quantified.
- We can evaluate two candidate assignments and decide that one is better than other.

Solve the Problem!

- Mr. Smith and his wife invited four other couples for a party.
- When everyone arrived, some of the people in the room shook hands with some of the others.
- Nobody shook hands with their spouse and nobody shook hands with the same person twice.
- After that, Mr. Smith asked everyone how many times they shook someone's hand.
- He received different answers from everybody.
- How many times did Mrs. Smith shake someone's hand?



Summary

Problem solving is difficult for several reasons:

- Complex problems often pose an enormous number of possible solutions.
- To get any sort of solution at all, we often have to introduce simplifications that make the problem tractable. As a result, the solutions that we generate may not be very valuable.
- The conditions of the problem change over time and might even involve other people who want to fail you.
- Real-world problems often have constraints that require special operations to generate feasible solutions.

References

Zbigniew Michalewicz and David B. Fogel. How to Solve It: Modern Heuristics, volume 2. Springer, 2004.