

FOUNDATIONS OF SEMANTIC WEB TECHNOLOGIES

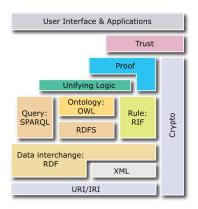
OWL 2 – Syntax and Semantics

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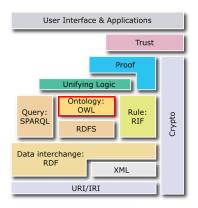


OWL





OWL





Agenda

- Recap OWL & Overview OWL 2
- The Description Logic \mathcal{SROIQ}
- Inferencing with SROIQ
- OWL 2 DL
- OWL 2 Profiles
- OWL 2 Full
- Summary



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 → FOL-based rule extensions, SWRL & RIF



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Should the OWL standard itself be extended?



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Should the OWL standard itself be extended?

→ OWI 2



Development of OWL 2

OWL 2 as "next version" of OWL

extensions due to practical experiences with OWL 1.0:

- additional expressivity due to new ontological axioms
- extralogical extensions (syntax, metadata, ...)
- revision of the OWL variants (Lite/DL/Full)

goals:

- most extensive compatibility with the existing OWL standard
- preservation of decidability of OWL DL
- correction of problems in the OWL 1.0 standard



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From SHOIN to SROIQ

OWL DL based on DL SHOIN(D):

- axioms:
 - TBox: subclass relationships $C \sqsubseteq D$
 - RBox: subrole relationships R ⊆ S (H), inverse roles R⁻ (I), transitivity
 - ABox: class assertions C(a), role assertions R(a,b), equality $a\approx b$, inequality $a\not\approx b$
- class constructors:
 - conjunction $C \sqcap D$, disjunction $C \sqcup D$, negation $\neg C$ of classes
 - role restrictions: universal $\forall R.C$ and existential $\exists R.C$
 - number restrictions (\mathcal{N}): $\leq nR$ and $\geq nR$ (n non-negative integer)
 - nominals (\mathcal{O}): $\{a\}$
- datatypes (D)

OWL 2 extends this to SROIQ(D)



ABox

\mathcal{SHOIN} supports different ABox assertions:

- class membership C(a) (C complex class),
- special case: negated class membership $\neg C(a)$ (C complex class),
- equality $a \approx b$,
- inequality $a \not\approx b$
- role membership R(a,b)



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- role membership R(a, b)
- negated role membership?
- $\rightsquigarrow SROIQ$ allows negated roles in der ABox: $\neg R(a,b)$



Number Restrictions

 \mathcal{SHOIN} supports only unqualified number restrictions (\mathcal{N}):

Person $\square \ge 3$ has Child

"'class of all persons with 3 or more children"'



Number Restrictions

 \mathcal{SHOIN} supports only unqualified number restrictions (\mathcal{N}):

Person $\square \ge 3$ has Child

"'class of all persons with 3 or more children" $\rightsquigarrow SROIQ$ also allows qualified

number restrictions (Q):

Person $\sqcap > 3$ hasChild.(Woman \sqcap Professor)

"'class of all persons with 3 or more daughters who are professors"'



The Self "Concept"

modeling task: "'Every human knows himself/herself."'



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• SHOIN:

knows(tom, tom) knows(tina, tina) knows(udo, udo) ...



The Self "Concept"

modeling task: "'Every human knows himself/herself."'

• SHOIN:

```
knows(tom,tom) \quad knows(tina,tina) \quad knows(udo,udo) \quad \dots
```

→ not generally applicable

• SROIQ: specific notation Self

Human ⊑ ∃knows.Self



Role Axioms in SHOIN

\mathcal{SHOIN} provides few role axioms:

 Trans(r), owl: TransitiveProperty: r is transitive Example: Trans(locatedIn)



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Role Axioms in \mathcal{SHOIN}

SHOIN provides few role axioms:

- Trans(r), owl: TransitiveProperty: r is transitive Example: Trans(locatedIn)
- Func(r), owl:FunctionalProperty: r is functional Example: Func(hasFather) also: ⊤ □≤ 1r



Role Axioms in SHOIN

SHOIN provides few role axioms:

- Trans(r), owl: TransitiveProperty: r is transitive Example: Trans(locatedIn)
- Func(r), owl:FunctionalProperty: r is functional Example: Func(hasFather) also: ⊤ □≤ 1r
- InvFunc(r), owl: InverseFunctionalProperty: r is inverse functional
 - Example: InvFunc(isFatherOf) also $\top \sqsubseteq \leqslant 1r^-$ or Func(r^-)



\mathcal{SROIQ} provides additional statements about roles:

• Ref(r), owl:ReflexiveProperty: r is reflexive, $(x,x) \in r^{\mathcal{I}}$ for all domain individuals x Example: Ref(knows)



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- Ref(r), owl: ReflexiveProperty: r is reflexive, $(x,x) \in r^{\mathcal{I}}$ for all domain individuals x Example: Ref(knows)
- Irr(r), owl: IrreflexiveProperty: r is irreflexive, $(x,x) \not\in r^{\mathcal{I}}$ for all domain individuals x Example: Irr(hasChild)



\mathcal{SROIQ} provides additional statements about roles:

- Ref(r), owl: ReflexiveProperty: r is reflexive, (x,x) ∈ r^T for all domain individuals x
 Example: Ref(knows)
- Irr(r), owl: IrreflexiveProperty: r is irreflexive, (x, x) ∉ r^T for all domain individuals x
 Example: Irr(hasChild)
- Asym(r), owl: AsymmtericProperty: r is asymmetric, $(x,y) \in r^{\mathcal{I}}$ implies $(y,x) \not\in r^{\mathcal{I}}$ Example: Asym(hasChild)



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- Ref(r), owl: ReflexiveProperty: r is reflexive, (x,x) ∈ r^T for all domain individuals x
 Example: Ref(knows)
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 Example: Irr(hasChild)
- Asym(r), owl: AsymmtericProperty: r is asymmetric, (x, y) ∈ r[⊥] implies (y, x) ∉ r[⊥] Example: Asym(hasChild)
- $\mathsf{Dis}(r,s)$, owl : $\mathsf{propertyDisjointWith}$, owl : $\mathsf{AllDisjointProperties}$: r and s are disjoint, $(x,y) \not\in r^{\mathcal{I}} \cap s^{\mathcal{I}}$ for all x,y

Example: Dis(hasFather, hasSon)



The Universal Role

SROIQ provides the universal role:

• universal role U (owl:TopObjectProperty): $(x,y) \in U^{\mathcal{I}}$ for all x,y

Example

 $\top \sqsubseteq \leqslant 7\,000\,000\,000\,U$.Human (not recommended!)

- → U is mainly comfortable as a counterpart for ⊤, e.g. as root element in a
 graphically displayed role hierarchy
- the converse owl:BottomObjectProperty has been introduced in OWL, but has no corresponding syntactic element in DLs
- for datatype properties analog owl: TopDataProperty and owl:BottomDataProperty



Complex Role Inclusion

"'The friends of my friends are my friends."'

→ can be expressed in SHOIN: hasFriend is transitive

"'The enemies of my friends are my enemies."'

 \rightsquigarrow Cannot be expressed in \mathcal{SHOIN} !



Complex Role Inclusion

- "'The friends of my friends are my friends."'
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complex role inclusion

- RBox-expressions of the form $r_1 \circ r_2 \circ \ldots \circ r_n \sqsubseteq s$
- semantics: $(x_0, x_1) \in r_1^{\mathcal{I}}, (x_1, x_2) \in r_2^{\mathcal{I}}, \dots, (x_{n-1}, x_n) \in r_n^{\mathcal{I}},$ implies $(x_0, x_n) \in s^{\mathcal{I}}$



Complex Role Inclusions – Example

Example

```
hasFriend \circ hasEnemy \sqsubseteq hasEnemy: if (x,y) \in \text{hasFriend}^{\mathcal{I}} and (y,z) \in \text{hasEnemy}^{\mathcal{I}}, then also holds (x,z) \in \text{hasEnemy}^{\mathcal{I}}
```

further examples

partOf ∘ belongsTo

belongsTo

hasBrother ∘ hasChild ⊑ isUncleOf



Expressivity of Complex Role Inclusions

How complicated are complex role inclusions?

RBoxes allow for encoding formal languages:

grammar for language of words ab, aabb, aaabbb, ...:

In fact, this way, all context-free languages can be encoded. This even enables us to encode the emptiness problem for intersection of two context-free languages into KB satisfiability.

→ OWL with (unrestricted) role inclusions is undecidable.



Regular RBoxes

Can complex role inclusion be restricted in order to retain decidability?

- RBoxes correspond to grammars for context-free languages
- intersection of these problematic
- → restriction to regular languages!



Regularity Conditions for RIAs

in order to guarantee decidability of inferenceing, the set of role inclusions has to be regular

- there has to be a strict linear order ≺ over the roles such that every RIA has one of the following forms (with s_i ≺ r for all 1 < i < n):
 - $r \circ r \sqsubseteq r$
 - $r^- \sqsubseteq r$
 - $s_1 \circ s_2 \circ \ldots \circ s_n \sqsubseteq r$

- $r \circ s_1 \circ s_2 \circ \ldots \circ s_n \sqsubseteq r$
- $s_1 \circ s_2 \circ \ldots \circ s_n \circ r \sqsubseteq r$



• Example 1: $r \circ s \sqsubseteq r$ $s \circ s \sqsubseteq s$ $r \circ s \circ r \sqsubseteq t$



- Example 1: $r \circ s \sqsubseteq r$ $s \circ s \sqsubseteq s$ $r \circ s \circ r \sqsubseteq t$ \rightsquigarrow regular with order $s \prec r \prec t$
- Example 2: $r \circ t \circ s \sqsubseteq t$



Example 1: r ∘ s ⊑ r s ∘ s ⊑ s r ∘ s ∘ r ⊑ t
 → regular with order s ≺ r ≺ t
 Example 2: r ∘ t ∘ s ⊑ t

→ not regular, form not allowed

• Example 3: $r \circ s \sqsubseteq s \quad s \circ r \sqsubseteq r$



- Example 1: $r \circ s \sqsubseteq r$ $s \circ s \sqsubseteq s$ $r \circ s \circ r \sqsubseteq t$ \Rightarrow regular with order $s \prec r \prec t$
- Example 2: $r \circ t \circ s \sqsubseteq t$
 - → not regular, form not allowed
- Example 3: $r \circ s \sqsubseteq s \quad s \circ r \sqsubseteq r$
 - → not regular, since no appropriate order exists



Revisiting the Definition of Simple Roles

- simple roles in \mathcal{SHOIN} = roles without transitive subroles
- $\bullet \ \ \text{in } \mathcal{SROIQ}$ we need to take RIAs into account



Revisiting the Definition of Simple Roles

simple roles are all roles...

- that do not occur on the rhs of a role inclusion,
- that are inverses of other simple roles,
- that occur only on the rhs of RIAs where the lhs consists of a length-one chain with a simple role.

(Caution: inductive definition)

 \leadsto non-simple are roles that can be derived from a chain of roles with length at least 2



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```
Expressions \leq n \, r.C, \geq n \, r.C, |rr(r), |rr(s)|, |rr(s)|, |rr(a,b)| are only allowed for simple roles r and s! (Reason: ensure decidability)
```



Overview SROIQ – TBoxes

class expressions

class names A. B $C \sqcap D$ conjunction disjunction $C \sqcup D$ negation $\neg C$ existential role restriction $\exists r.C$ universal role restriciton $\forall r.C$ Self $\exists s. Self$ atleast restriction $\geq n s.C$ atmost restriction $\leq n s.C$ nominals {*a*}

TBox (class axioms)

inclusion $C \sqsubseteq D$ equivalence $C \equiv D$



Overview SROIQ - RBoxes & ABoxes

Roles	
roles	r, s, t
simple roles	s, t
universal role	11

ABox (assertions)

class membership	C(a)
role membership	r(a,b)
neg. role membership	$\neg s(a,b)$
equality	$a \approx b$
inequality	$a \not\approx b$

RBox (role axioms)

inclusion	$r_1 \sqsubseteq r_2$
complex role inclusion	$r_1 \circ \ldots \circ r_n \sqsubseteq r$
transitivity	Trans(r)
symmetry	Sym(r)
reflexivity	Ref(r)
irreflexivity	Irr(s)
disjointness	Dis(s,t)



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How complicated is SROIQ?

recap: \mathcal{SHOIN} (OWL DL) is very complex (NExpTime)



How complicated is SROIQ?

recap: \mathcal{SHOIN} (OWL DL) is very complex (NExpTime) observation: some modeling features are not really necessary ("syntactic sugar")

- Trans(r) can be expressed as $r \circ r \sqsubseteq r$
- Sym(r) can be expressed as $r^- \sqsubseteq r$
- Asym(r) can be expressed as $Dis(r, r^-)$
- Irr(s) can be expressed as $\top \sqsubseteq \neg \exists S.Self$

qualifizierte number restrictions do not cause problems (known and implemented before)

```
→ main problem: role axioms (RBox)
```



Role Inclusions, Languages, Automata

How to deal with RBoxes?

- RBox inclusions resemble formal grammars
- every role r defines a regular language: the language of role chains from which it follows
- regular languages \equiv regular Expressions \equiv finite automata

→ approach: tableau methods are extended by "'RBox automata"



Decidability of SROIQ

tableau method for SROIQ shows decidability

- algorithm has a good adaptation behaviour: modeling features that are not used do hardly impede computation ("pay as you go")
- tableau method not useful for complexity considerations
- SROIQ 2-NExpTime-complete
 - RIQ and SROIQ are Harder than SHOIQ. Yevgeny Kazakov.
 In Gerhard Brewka and Jérôme Lang, editors, KR 2008. Pages 274-284. AAAI Press. 2008
 - lower bound: encoding of a 2Exp tiling problem
 - upper bound: exponential translation into the 2-variable fragment of FOL with counting quantifiers, \mathcal{C}_2 , for which satisfiability checking is known to be NExpTime-complete)



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OWL 2 DL: Further Aspects

 \mathcal{SROIQ} is "only" logical foundation of OWL 2 DL

further non-logical aspects:

- Syntax (extension necessary)
- datatype declarations and datatype functions, new datatypes?
- metamodeling: "punning"
- · comments and ontological metadata
- invers-functional conkrete roles (datatype properties): Keys?
- mechanisms for ontology import?
- ..
- → diverse smaller changes



Metamodeling

Metamodeling

specification of ontological knowledge about elements of the ontology (including classes, roles, axioms).

Examples:

- "The class Person was created on the 30.1.2008 by bglimm."
- "For the class City, we recommend the property numberOfCitizens."
- "The statement ,Dresden was founded in 1206' was extracted automatically with a confidence of 85%."

(Compare Reification in RDF Schema)



Punning in OWL

Metamodeling in expressive logics is dangerous and expensive!

OWL 2 currently supports the simples form of metamodeling:

Punning

- the names for classes, roles, individuals do not have to be disjoint
- no logical relationship between class, individual and role of the same name
- only relevant for pragmatic interpretation

Example:

Person(Birte) classCreatedBy(Person, bglimm)



Comments and Metadata

punning supports simple metadata with (weak) semantic meaning

How can one make purely syntactic comments in an ontology?

• comments in XML files: <!-- comment -->



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How can one make purely syntactic comments in an ontology?

- comments in XML files: <!-- comment -->
 no relation to the OWL axioms in this file
- non-logical annotations in OWL 2: owl:AnnotationProperty



Comments and Metadata

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How can one make purely syntactic comments in an ontology?

- comments in XML files: <!-- comment -->
 no relation to the OWL axioms in this file
- non-logical annotations in OWL 2: owl:AnnotationProperty
 → attached to (semantic) ontological element



Syntactic Aspects

new/extended syntaxes:

- RDF/XML: extension by OWL 2 elements
- functional-style syntax: replaces "abstract syntax" in OWL 1
- OWL/XML: syntax for simpler processing in XML tools
- Turtle: RDF triple syntax
- Manchester syntax: syntax that is easier to read for humans



Quo vadis, OWL Lite?



Quo vadis, OWL Lite?

OWL Lite as a Failure:

- almost as complex as OWL DL
- complicated syntax that does not provide direct access to actual modeling power
- use in ontologies today only "'by accident"', not deliberately

original goal:

capture the part of OWL that is easy and efficiently implementable



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→ OWL 2 Profiles



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OWL 2 Profiles

OWL 2 defines three fragments where automated inferencing can be done in PTime

- OWL EL
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OWL 2 Profiles

OWL 2 defines three fragments where automated inferencing can be done in PTime

- OWL EL
 - computation of the class hierarchy (all subclass relationships) in PTime
- OWL QL
 - conjunctive queries in AC₀ (data complexity) → reducible to SQL
- OWL RL
 - can be used as an extension of RDFS or as a fragment of OWL DL (OWL Direct Semantics)
 - complexity PTime



OWL 2 EL

- An (almost maximal) fragment of OWL 2 such that
 - satisfiability can be checked in PTime (PTime-complete)
 - data complexity for ABox queries also PTime-complete
- class hierarchy (all subsumption relationships between atomic classes)
 can be computed in one pass
- ullet uses a saturation method that was developed for the description logic \mathcal{EL}



OWL 2 EL

- allowed:
 - subclass axioms with conjunction, existential restriction, \top , \bot , singleton nominals
 - complex RIAs, range restrictions (under certain conditions)
- not allowed:
 - negation, disjunction, universal restrictions, inverse roles



OWL 2 QL

- an (almost maximal) fragment of OWL 2 such that
 - data complexity of conjunctive query answering is in AC⁰
- queries can be rewritten such that no terminological knowledge has to be taken into account
 - ⇒ standard RDBMS can be used for storage and querying



OWL 2 QL

- allowed:
 - simple role hierarchies, domain & range axioms
 - subclass axioms with
 - ullet Ihs: class name or existential restriction with \top
 - rhs: conjunction of class names, existential restriction and negation of lhs expressions
- supports RDFS with "well-formed" graphs



OWL 2 RL

- An (almost maximal) fragment of OWL 2 such that
 - automated inferencing is PTime-complete (consistency, satisfiability of classes, subsumption, class membership checks)
 - automated inferencing is correct (sound & complete) if the given RDF graph satisfies certain requirements
 - otherwise the automated reasoning may be be sound but incomplete.
- can operate directly on RDF triples in order to enrich instance data (materialization, forward chaining for facts)
- automated inferencing can be implemented via a set of rules (using a rule engine that supports equality)



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What to do with OWL Full?

Goal of OWL 2 DL: make many OWL Full 1.0 ontologies interpretable as OWL DL (cf. e.g. punning)



What to do with OWL Full?

Goal of OWL 2 DL: make many OWL Full 1.0 ontologies interpretable as OWL DL (cf. e.g. punning)

- extension of OWL Full by OWL 2 features is required by a few practitioners
- allows to work on all kinds of RDF graphs
- despite undecidability: many FOL verification tools do not guarantee termination and are still useful
- alternative implementation techniques can be used, which might be faster (but do not guarantee termination)



- annotations do not have a semantics in the direct semantics (which is used for OWL DL), but they do in the RDF-based semantics (which is used for OWL Full)
- import commands are only parser commands in the direct semantics, but do have a presence as triple in the RDF-based Semantics
- in the RDF-based semantics, classes are individuals, that are endowed with an extension → semantic conditions are only applicable to those classes that have an individual representant



Example

- C(a)
- ullet query for all instances of the class C \sqcup D



Example

- C(a)
- ullet query for all instances of the class C \sqcup D
- RDF-based semantics: Ø, direct semantics: a



Example

- C(a)
- query for all instances of the class C

 □ D
- RDF-based semantics: ∅, direct semantics: a
- under the RDF-based semantics, we only have the guarantee that the union of the extensions of C and D do exist as subsets of the domain, however it is not ensured that an element exists which has this set as extension.
- contrarily, in the direct semantics class names "directly" represent sets and not domain elements
- \leadsto the answer coincides for both semantics after adding E \equiv C \sqcup D



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Summary

OWL 2 as first extension of the OWL standard

- standardized 27.10.2009
- logical extension based on description logic SROIQ
- new modeling features, most notably complex RIAs, qualified number restrictions
- non-logical extensions: punning, comments, datatypes, etc.
- profiles with polynomial reasoning procedures