

Exercise 10: Datalog Evaluation

Database Theory

2020-06-22

Maximilian Marx, David Carral

Exercise 1

Exercise. Consider the program

$$P = \{ T(x) \leftarrow e(x), T(x) \leftarrow a(x, y) \wedge T(y) \wedge b(x, z) \wedge T(z) \}.$$

1. Describe, in your own words, the kind of structures that the query $\langle T, P \rangle$ recognises.
2. Compute the semi-naive evaluation of P for the database D with the following facts:

$e(1)$ $e(2)$ $e(6)$ $a(3, 1)$ $a(4, 3)$ $a(5, 3)$ $a(7, 5)$ $b(3, 2)$ $b(5, 3)$ $b(7, 6)$

Specify for each newly derived fact which of the rule(s) of will produce it at the given point in the derivation.

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Solution.

1. $\langle T, P \rangle$ recognises binary forests with leafs labelled e and branches labelled a and b .
2. Transformed program:

$$\hat{P} = \left\{ \underbrace{T(x) \leftarrow e(x)}_{(R1)}, \underbrace{T(x) \leftarrow a(x, y) \wedge \Delta_T^i(y) \wedge b(x, z) \wedge T^i(z)}_{(R2.1)}, \underbrace{T(x) \leftarrow a(x, y) \wedge T^{i-1}(y) \wedge b(x, z) \wedge \Delta_T^i(z)}_{(R2.2)} \right\}$$

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$$T_{\hat{P}}^0 = \emptyset$$

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$$T_{\hat{P}}^4 = T_{\hat{P}}^3 \cup \{ T(7) \} = T_{\hat{P}}^5 = T_{\hat{P}}^{\infty} \tag{R2.1}$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

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$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$h(1) \quad h(2) \quad h(3) \quad h(4) \quad h(5) \quad h(6) \quad h(7) \qquad p(1, 2) \quad p(2, 3) \quad p(4, 3) \quad p(5, 4) \quad p(6, 1) \quad p(7, 1)$$

1. Sketch the database as a tree. What are the expected answers to the query?
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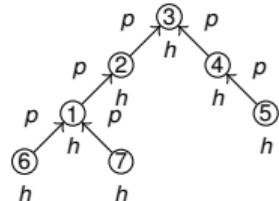
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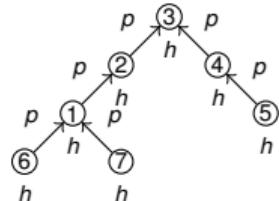
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Expected answers:

$$\{\text{Query}(1), \text{Query}(5)\}$$

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Solution.

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$$\text{input}_{\text{Query}}^f[] = \emptyset$$

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$$\text{sup}_1^{r_1}[x] = \emptyset$$

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$$\text{sup}_0^{r_2}[x] = \emptyset$$

$$\text{sup}_1^{r_2}[x] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

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$$\text{sup}_0^{r_3}[x] = \emptyset$$

$$\text{sup}_1^{r_3}[x, w] = \emptyset$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

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$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

1. Sketch the database as a tree. What are the expected answers to the query?
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$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \emptyset$$

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$$\text{output}_S^{bf}[x, y] = \emptyset$$

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$$\text{sup}_1^{r_3}[x, w] = \emptyset$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

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$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$h(1) \quad h(2) \quad h(3) \quad h(4) \quad h(5) \quad h(6) \quad h(7) \quad p(1, 2) \quad p(2, 3) \quad p(4, 3) \quad p(5, 4) \quad p(6, 1) \quad p(7, 1)$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \emptyset$$

$$\text{sup}_1^{r_2}[x] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \emptyset$$

$$\text{sup}_1^{r_3}[x, w] = \emptyset$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$h(1) \quad h(2) \quad h(3) \quad h(4) \quad h(5) \quad h(6) \quad h(7) \quad p(1, 2) \quad p(2, 3) \quad p(4, 3) \quad p(5, 4) \quad p(6, 1) \quad p(7, 1)$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \emptyset$$

$$\text{sup}_1^{r_3}[x, w] = \emptyset$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & & p(1,2) & p(2,3) & p(4,3) & p(5,4) & p(6,1) & p(7,1) \end{array}$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \emptyset$$

$$\text{sup}_1^{r_3}[x, w] = \emptyset$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$h(1) \quad h(2) \quad h(3) \quad h(4) \quad h(5) \quad h(6) \quad h(7) \quad p(1, 2) \quad p(2, 3) \quad p(4, 3) \quad p(5, 4) \quad p(6, 1) \quad p(7, 1)$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x, w] = \emptyset$$

$$\text{sup}_1^{r_3}[x, v] = \emptyset$$

$$\text{sup}_2^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$h(1) \quad h(2) \quad h(3) \quad h(4) \quad h(5) \quad h(6) \quad h(7) \qquad p(1, 2) \quad p(2, 3) \quad p(4, 3) \quad p(5, 4) \quad p(6, 1) \quad p(7, 1)$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x, w] = \{1\}$$

$$\text{sup}_1^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$h(1) \quad h(2) \quad h(3) \quad h(4) \quad h(5) \quad h(6) \quad h(7) \quad p(1, 2) \quad p(2, 3) \quad p(4, 3) \quad p(5, 4) \quad p(6, 1) \quad p(7, 1)$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \emptyset$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \emptyset$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{2\}$$

$$\text{sup}_0^{r_4}[x] = \emptyset$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \{2\}$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{2\}$$

$$\text{sup}_0^{r_4}[x] = \{2\}$$

$$\text{sup}_1^{r_4}[x] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \{2\}$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{2\}$$

$$\text{sup}_0^{r_4}[x] = \{2\}$$

$$\text{sup}_1^{r_4}[x] = \{2\}$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[y] = \{2\}$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{2\}$$

$$\text{sup}_0^{r_4}[x] = \{2\}$$

$$\text{sup}_1^{r_4}[x] = \{2\}$$

$$\text{output}_S^{fb}[x, y] = \{(2, 2)\}$$

$$\text{input}_S^{fb}[y] = \{2\}$$

$$\text{sup}_0^{r_5}[y] = \emptyset$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$h(1) \quad h(2) \quad h(3) \quad h(4) \quad h(5) \quad h(6) \quad h(7) \quad p(1, 2) \quad p(2, 3) \quad p(4, 3) \quad p(5, 4) \quad p(6, 1) \quad p(7, 1)$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{2\}$$

$$\text{sup}_0^{r_4}[x] = \{2\}$$

$$\text{sup}_1^{r_4}[x] = \{2\}$$

$$\text{output}_S^{fb}[x, y] = \{(2, 2)\}$$

$$\text{input}_S^{fb}[y] = \{2\}$$

$$\text{sup}_0^{r_5}[y] = \{2\}$$

$$\text{sup}_1^{r_5}[x, w, y] = \emptyset$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{2\}$	$\text{input}_S^{fb}[y] = \{2\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{2\}$	$\text{sup}_0^{r_5}[y] = \{2\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$	$\text{sup}_1^{r_4}[x] = \{2\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 2), (2, 3, 2), \dots, (7, 1, 2)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \emptyset$	$\text{sup}_2^{r_4}[x] = \{2\}$	$\text{sup}_2^{r_5}[x, v, y] = \emptyset$
			$\text{sup}_3^{r_3}[x, y] = \emptyset$	$\text{output}_S^{fb}[x, y] = \{(2, 2)\}$	$\text{sup}_3^{r_5}[x, y] = \emptyset$
			$\text{output}_S^{bf}[x, y] = \emptyset$		$\text{output}_S^{fb}[x, y] = \emptyset$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{2\}$	$\text{sup}_0^{r_5}[y] = \{2\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$	$\text{sup}_1^{r_4}[x] = \{2\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 2), (2, 3, 2), \dots, (7, 1, 2)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \emptyset$	$\text{output}_S^{fb}[x, y] = \{(2, 2)\}$	$\text{sup}_2^{r_5}[x, v, y] = \emptyset$
			$\text{sup}_3^{r_3}[x, y] = \emptyset$		$\text{sup}_3^{r_5}[x, y] = \emptyset$
			$\text{output}_S^{bf}[x, y] = \emptyset$		$\text{output}_S^{fb}[x, y] = \emptyset$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[y] = \{1, 2\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \emptyset$	$\text{sup}_1^{r_4}[x] = \{2\}$	$\text{sup}_2^{r_5}[x, w, y] = \{(1, 2, 2), (2, 3, 2), \dots, (7, 1, 2)\}$
			$\text{sup}_3^{r_3}[x, y] = \emptyset$	$\text{output}_S^{fb}[x, y] = \{(2, 2)\}$	$\text{sup}_2^{r_5}[x, v, y] = \emptyset$
			$\text{output}_S^{bf}[x, y] = \emptyset$		$\text{sup}_3^{r_5}[x, y] = \emptyset$
					$\text{output}_S^{fb}[x, y] = \emptyset$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

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$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

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$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{output}_S^{fb}[x, y] = \{(2, 2)\}$$

$$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_5}[y] = \{2\}$$

$$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 2), (2, 3, 2), \dots, (7, 1, 2)\}$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

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$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{2\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 2), (2, 3, 2), \dots, (7, 1, 2)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \emptyset$	$\text{sup}_2^{r_4}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_2^{r_5}[x, v, y] = \emptyset$
			$\text{sup}_3^{r_3}[x, y] = \emptyset$		$\text{sup}_3^{r_5}[x, y] = \emptyset$
			$\text{output}_S^{bf}[x, y] = \emptyset$		$\text{output}_S^{fb}[x, y] = \emptyset$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

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$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$$

$$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$$

$$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 2), (2, 3, 2), \dots, (7, 1, 2)\}$$

$$\text{sup}_2^{r_5}[x, v, y] = \emptyset$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \emptyset$	$\text{sup}_2^{r_4}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_2^{r_5}[x, v, y] = \emptyset$
			$\text{sup}_3^{r_3}[x, y] = \emptyset$		$\text{sup}_3^{r_5}[x, y] = \emptyset$
			$\text{output}_S^{bf}[x, y] = \emptyset$		$\text{output}_S^{fb}[x, y] = \emptyset$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_2^{r_4}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$$

$$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$$

$$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$$

$$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$$

$$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$$

$$\text{sup}_3^{r_5}[x, y] = \emptyset$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

1. Sketch the database as a tree. What are the expected answers to the query?
2. Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.

$$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$$

$$\text{sup}_1^{r_1}[x] = \emptyset$$

$$\text{output}_{\text{Query}}^f[x] = \emptyset$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_2}[x] = \{1\}$$

$$\text{sup}_1^{r_2}[x] = \{1\}$$

$$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$$

$$\text{input}_S^{bf}[x] = \{1\}$$

$$\text{sup}_0^{r_3}[x] = \{1\}$$

$$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$$

$$\text{sup}_2^{r_3}[x, v] = \emptyset$$

$$\text{sup}_3^{r_3}[x, y] = \emptyset$$

$$\text{output}_S^{bf}[x, y] = \emptyset$$

$$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$$

$$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$$

$$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$$

$$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$$

$$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$$

$$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$$

$$\text{sup}_3^{r_5}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$$

$$\text{output}_S^{fb}[x, y] = \emptyset$$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \emptyset$	$\text{sup}_2^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
			$\text{sup}_3^{r_3}[x, y] = \emptyset$	$\text{sup}_3^{r_4}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_3^{r_5}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$
			$\text{output}_S^{bf}[x, y] = \emptyset$	$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1,2) & p(2,3) & p(4,3) & p(5,4) & p(6,1) & p(7,1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2), (1, 4)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \{(1, 2), (1, 4)\}$	$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
			$\text{sup}_3^{r_3}[x, y] = \emptyset$		$\text{sup}_3^{r_5}[x, y] = \{(1, 1), (2, 2), (2, 4), (4, 2), (4, 4)\}$
			$\text{output}_S^{bf}[x, y] = \emptyset$		$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (2, 4), (4, 2), (4, 4)\}$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2), (1, 4)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \{(1, 5)\}$	$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
			$\text{sup}_3^{r_3}[x, y] = \{(1, 5)\}$		$\text{sup}_3^{r_5}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$
			$\text{output}_S^{bf}[x, y] = \emptyset$		$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1,2) & p(2,3) & p(4,3) & p(5,4) & p(6,1) & p(7,1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \emptyset$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \{(1, 2), (1, 4)\}$	$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
			$\text{sup}_3^{r_3}[x, y] = \{(1, 5)\}$		$\text{sup}_3^{r_5}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$
			$\text{output}_S^{bf}[x, y] = \{(1, 5)\}$		$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (2, 4), (4, 2), (4, 4)\}$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

and the adorned version for query $S(1, x)$:

$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

$$r_2 = S^{bf}(x, x) \leftarrow h(x)$$

$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1,2) & p(2,3) & p(4,3) & p(5,4) & p(6,1) & p(7,1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \{1, 5\}$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2), (1, 4)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
	$\text{output}_{\text{Query}}^f[x] = \emptyset$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
			$\text{sup}_3^{r_3}[x, y] = \{(1, 5)\}$		$\text{sup}_3^{r_5}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$
			$\text{output}_S^{bf}[x, y] = \{(1, 5)\}$		$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$

Exercise 2

Exercise. Consider the “Same generation” Datalog program given in the lecture (Lecture 15, Slide 15):

$$S(x, x) \leftarrow h(x)$$

$$S(x, y) \leftarrow p(x, w) \wedge S(v, w) \wedge p(y, v)$$

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$$r_1 = \text{Query}^f(x) \leftarrow S^{bf}(1, x)$$

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$$r_4 = S^{fb}(x, x) \leftarrow h(x)$$

$$r_3 = S^{bf}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

$$r_5 = S^{fb}(x, y) \leftarrow p(x, w) \wedge S^{fb}(v, w) \wedge p(y, v)$$

together with the database that contains the following facts for predicate p :

$$\begin{array}{ccccccccccccc} h(1) & h(2) & h(3) & h(4) & h(5) & h(6) & h(7) & p(1, 2) & p(2, 3) & p(4, 3) & p(5, 4) & p(6, 1) & p(7, 1) \end{array}$$

- Sketch the database as a tree. What are the expected answers to the query?
- Apply the QSQR algorithm to compute the answer to the query.

Solution.

2.	$\text{input}_{\text{Query}}^f[] = \{1, 2, \dots, 7\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{bf}[x] = \{1\}$	$\text{input}_S^{fb}[x] = \{1, 2, 3, 4\}$	$\text{input}_S^{fb}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_0^{r_1}[] = \{1, 2, \dots, 7\}$	$\text{sup}_0^{r_2}[x] = \{1\}$	$\text{sup}_0^{r_3}[x] = \{1\}$	$\text{sup}_0^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_0^{r_5}[y] = \{1, 2, 3, 4\}$
	$\text{sup}_1^{r_1}[x] = \{1, 5\}$	$\text{sup}_1^{r_2}[x] = \{1\}$	$\text{sup}_1^{r_3}[x, w] = \{(1, 2), (1, 4)\}$	$\text{sup}_1^{r_4}[x] = \{1, 2, 3, 4\}$	$\text{sup}_1^{r_5}[x, w, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
	$\text{output}_{\text{Query}}^f[x] = \{1, 5\}$	$\text{output}_S^{bf}[x, y] = \{(1, 1)\}$	$\text{sup}_2^{r_3}[x, v] = \{(1, 2), (1, 4)\}$	$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$	$\text{sup}_2^{r_5}[x, v, y] = \{(1, 2, 1), (2, 3, 1), \dots, (7, 1, 4)\}$
			$\text{sup}_3^{r_3}[x, y] = \{(1, 5)\}$		$\text{sup}_3^{r_5}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$
			$\text{output}_S^{bf}[x, y] = \{(1, 5)\}$		$\text{output}_S^{fb}[x, y] = \{(1, 1), (2, 2), (3, 3), (4, 4)\}$

Exercise 3

Exercise. Consider the following modified version of the same generation program:

$$\begin{aligned} S(x, x) &\leftarrow h(x) \\ S(x, y) &\leftarrow p(x, w) \wedge p(y, v) \wedge S(v, w) \end{aligned}$$

What is the adorned version of this program for the query $S(1, x)$? Use this program to show that it is possible that some tuples in an input-relation are not copied to the sup_0 relation of a rule during the execution of the QSQR algorithm.

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Solution.

$$r_1 = Q^f(x) \leftarrow S^{bf}(1, x)$$

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$$\begin{aligned} r_1 &= Q^f(x) \leftarrow S^{bf}(1, x) \\ r_2 &= S^{bf}(x, x) \leftarrow h(x) \end{aligned}$$

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- ▶ Consider the auxiliary relations for r_4 : $\text{input}_S^{bb}[x, y]$ has arity two, since two variables are bound.

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- ▶ Consider the auxiliary relations for r_4 : $\text{input}_S^{bb}[x, y]$ has arity two, since two variables are bound.
- ▶ However, $\text{sup}_0^{r_4}[x]$ has arity one, since r_4 forces $x = y$.

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What is the adorned version of this program for the query $S(1, x)$? Use this program to show that it is possible that some tuples in an input-relation are not copied to the sup_0 relation of a rule during the execution of the QSQR algorithm.

Solution.

$$\begin{aligned} r_1 &= Q^f(x) \leftarrow S^{bf}(1, x) \\ r_2 &= S^{bf}(x, x) \leftarrow h(x) \\ r_3 &= S^{bf}(x, y) \leftarrow p(x, w) \wedge p(y, w) \wedge S^{bb}(v, w) \\ r_4 &= S^{bb}(x, x) \leftarrow h(x) \\ r_5 &= S^{bb}(x, y) \leftarrow p(x, w) \wedge p(y, v) \wedge S^{bb}(v, w) \end{aligned}$$

- ▶ Consider the auxiliary relations for r_4 : $\text{input}_S^{bb}[x, y]$ has arity two, since two variables are bound.
- ▶ However, $\text{sup}_0^{r_4}[x]$ has arity one, since r_4 forces $x = y$.
- ▶ Thus, only tuples $\langle x, y \rangle$ with $x = y$ are copied.

Exercise 4

Exercise. Consider the following program:

$$\text{Sv}(x, y) \leftarrow \text{flat}(x, y)$$

$$\text{Sv}(x, y) \leftarrow \text{up}(x, z_1) \wedge \text{Sv}(z_1, z_2) \wedge \text{flat}(z_2, z_3) \wedge \text{Sv}(z_3, z_4) \wedge \text{down}(z_4, y)$$

Give the magic set transformation for this program and the query $\text{Sv}(a, y)$, where a is a constant.

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Exercise. Consider the following program:

$$Sv(x, y) \leftarrow \text{flat}(x, y)$$

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Give the magic set transformation for this program and the query $\text{Sv}(a, y)$, where a is a constant.

Solution.

Adorned program:

$$r_0 = \text{Query}^f(y) \leftarrow \text{Sv}^{bf}(a, y)$$

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Adorned program:

$$r_0 = \text{Query}^f(y) \leftarrow \text{Sv}^{bf}(a, y)$$

$$r_1 = \text{Sv}^{bf}(x, y) \leftarrow \text{flat}(x, y)$$

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Magic Sets transformation:

Exercise 4

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$$\text{input}_{\text{Sv}}^{bf}(a) \leftarrow$$

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Magic Sets transformation:

$$\text{input}_{\text{Sv}}^{bf}(a) \leftarrow \quad \text{output}_{\text{Sv}}^{bf}(x, y) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{flat}(x, y)$$

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Magic Sets transformation:

$$\text{input}_{\text{Sv}}^{bf}(a) \leftarrow \quad \text{output}_{\text{Sv}}^{bf}(x, y) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{flat}(x, y)$$

$$\text{sup}_2^{r_2}(x, z_1) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{up}(x, z_1)$$

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$$\text{sup}_2^{r_2}(x, z_1) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{up}(x, z_1)$$

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Magic Sets transformation:

$$\text{input}_{\text{Sv}}^{bf}(a) \leftarrow$$

$$\text{output}_{\text{Sv}}^{bf}(x, y) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{flat}(x, y)$$

$$\text{sup}_2^{r_2}(x, z_1) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{up}(x, z_1)$$

$$\text{input}_{\text{Sv}}^{bf}(z_1) \leftarrow \text{sup}_2^{r_2}(x, z_1)$$

$$\text{sup}_3^{r_2}(x, z_2) \leftarrow \text{sup}_2^{r_2}(x, z_1) \wedge \text{output}_{\text{Sv}}^{bf}(z_1, z_2)$$

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$$\text{input}_{\text{Sv}}^{bf}(a) \leftarrow$$

$$\text{output}_{\text{Sv}}^{bf}(x, y) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{flat}(x, y)$$

$$\text{sup}_2^{r_2}(x, z_1) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{up}(x, z_1)$$

$$\text{input}_{\text{Sv}}^{bf}(z_1) \leftarrow \text{sup}_2^{r_2}(x, z_1)$$

$$\text{sup}_3^{r_2}(x, z_2) \leftarrow \text{sup}_2^{r_2}(x, z_1) \wedge \text{output}_{\text{Sv}}^{bf}(z_1, z_2)$$

$$\text{sup}_4^{r_2}(x, z_3) \leftarrow \text{sup}_3^{r_2}(x, z_2) \wedge \text{flat}(z_2, z_3)$$

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$$r_1 = \text{Sv}^{bf}(x, y) \leftarrow \text{flat}(x, y)$$

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Magic Sets transformation:

$$\text{input}_{\text{Sv}}^{bf}(a) \leftarrow$$

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$$\text{input}_{\text{Sv}}^{bf}(z_1) \leftarrow \text{sup}_2^{r_2}(x, z_1)$$

$$\text{sup}_3^{r_2}(x, z_2) \leftarrow \text{sup}_2^{r_2}(x, z_1) \wedge \text{output}_{\text{Sv}}^{bf}(z_1, z_2)$$

$$\text{sup}_4^{r_2}(x, z_3) \leftarrow \text{sup}_3^{r_2}(x, z_2) \wedge \text{flat}(z_2, z_3)$$

$$\text{input}_{\text{Sv}}^{bf}(z_3) \leftarrow \text{sup}_4^{r_2}(x, z_3)$$

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$$\text{Sv}(x, y) \leftarrow \text{flat}(x, y)$$

$$\text{Sv}(x, y) \leftarrow \text{up}(x, z_1) \wedge \text{Sv}(z_1, z_2) \wedge \text{flat}(z_2, z_3) \wedge \text{Sv}(z_3, z_4) \wedge \text{down}(z_4, y)$$

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Adorned program:

$$r_0 = \text{Query}^f(y) \leftarrow \text{Sv}^{bf}(a, y)$$

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Magic Sets transformation:

$$\text{input}_{\text{Sv}}^{bf}(a) \leftarrow$$

$$\text{sup}_2^{r_2}(x, z_1) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{up}(x, z_1)$$

$$\text{sup}_3^{r_2}(x, z_2) \leftarrow \text{sup}_2^{r_2}(x, z_1) \wedge \text{output}_{\text{Sv}}^{bf}(z_1, z_2)$$

$$\text{input}_{\text{Sv}}^{bf}(z_3) \leftarrow \text{sup}_4^{r_2}(x, z_3)$$

$$\text{output}_{\text{Sv}}^{bf}(x, y) \leftarrow \text{input}_{\text{Sv}}^{bf}(x) \wedge \text{flat}(x, y)$$

$$\text{input}_{\text{Sv}}^{bf}(z_1) \leftarrow \text{sup}_2^{r_2}(x, z_1)$$

$$\text{sup}_4^{r_2}(x, z_3) \leftarrow \text{sup}_3^{r_2}(x, z_2) \wedge \text{flat}(z_2, z_3)$$

$$\text{output}_{\text{Sv}}^{bf}(x, y) \leftarrow \text{sup}_4^{r_2}(x, z_3) \wedge \text{output}_{\text{Sv}}^{bf}(z_3, z_4) \wedge \text{down}(z_4, y)$$