

Exercise 2

Employ tilings to show that the satisfiability problem for the three-variable fragment FO^3 of FO is undecidable.

Exercise 3

Show that the problem of checking if two input FO formulae are equivalent (are satisfied by exactly the same structures) is undecidable.

Exercise 4

Analyse lecture notes and convince yourself that you understand why query evaluation in FO is in PSPACE in combined complexity but only LOGSPACE in data complexity.

Exercise 5

QBF is a well-known PSPACE -complete problem. Provide a polynomial reduction from QBF to the query evaluation problem for FO and conclude its PSPACE -completeness. Hint: Two-element structure suffices.