

DATABASE THEORY

Lecture 14: Datalog Implementation

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Implementing Datalog

FO queries (and thus also CQs and UCQs) are supported by almost all DBMS \sim many specific implementation and optimisation techniques

How can Datalog queries be answered in practice?

ightarrow techniques for dealing with recursion in DBMS query answering

There are two major paradigms for answering recursive queries:

- Bottom-up: derive conclusions by applying rules to given facts
- Top-down: search for proofs to infer results given query

Review: Datalog

A rule-based recursive query language

father(alice, bob)
mother(alice, carla)
$Parent(x, y) \leftarrow father(x, y)$
$Parent(x, y) \leftarrow mother(x, y)$
SameGeneration(<i>x</i> , <i>x</i>)
SameGeneration(x, y) \leftarrow Parent(x, v) \land Parent(y, w) \land SameGeneration(v, w)

- Datalog is more complex than FO query answering
- Datalog is more expressive than FO query answering
- Semipositive Datalog with a successor ordering captures P
- Datalog containment is undecidable

Remaining question: How can Datalog query answering be implemented?

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slide 2 of 13

Computing Datalog Query Answers Bottom-Up

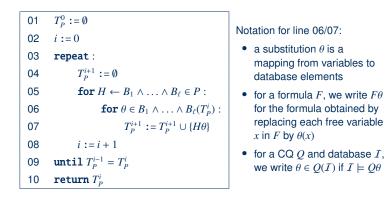
We already saw a way to compute Datalog answers bottom-up: the step-wise computation of the consequence operator T_P

Bottom-up computation is known under many names:

- Forward-chaining since rules are "chained" from premise to conclusion (common in logic programming)
- Materialisation since inferred facts are stored ("materialised") (common in databases)
- Saturation since the input database is "saturated" with inferences (common in theorem proving)
- Deductive closure since we "close" the input under entailments (common in formal logic)

Naive Evaluation of Datalog Queries

A direct approach for computing T_P^{∞}



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Less Naive Evaluation Strategies

Does it really matter how often we consider a rule match? After all, each fact is added only once ...

In practice, finding applicable rules takes significant time, even if the conclusion does not need to be added – iteration takes time!

 \rightsquigarrow huge potential for optimisation

Observation:

we derive the same conclusions over and over again in each step

Idea: apply rules only to newly derived facts

 \rightsquigarrow semi-naive evaluation

What's Wrong with Naive Evaluation?

An example Datalog program:

	e(1,2)	e(2,3)	e(3,4)	e(4, 5)
(R 1)	T(x, y)	$\leftarrow \mathbf{e}(x, y)$		
(<i>R</i> 2)	T(x, z)	$\leftarrow T(x, y)$	$\wedge T(y, z)$	

How many body matches do we need to iterate over?

$T_P^0 = \emptyset$	initialisation		
$T_P^1 = \{T(1,2),T(2,3),T(3,4),T(4,5)\}$	4 matches for (R1)		
$T_P^2 = T_P^1 \cup \{T(1,3),T(2,4),T(3,5)\}$	$4\times(R1)+3\times(R2)$		
$T_P^3 = T_P^2 \cup \{T(1,4),T(2,5),T(1,5)\}$	$4\times(R1)+8\times(R2)$		
$T_P^4 = T_P^3 = T_P^\infty$	$4\times(R1)+10\times(R2)$		
In total, we considered 37 matches to derive 11 facts			

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slide 6 of 13

Semi-Naive Evaluation

The computation yields sets $T_P^0 \subseteq T_P^1 \subseteq T_P^2 \subseteq \ldots \subseteq T_P^\infty$

- For an IDB predicate R, let Rⁱ be the "predicate" that contains exactly the R-facts in Tⁱ_P
- For $i \leq 1$, let Δ_{R}^{i} be the collection of facts $\mathsf{R}^{i} \setminus \mathsf{R}^{i-1}$

We can restrict rules to use only some computations.

Some options for the computation in step i + 1:

$T(x,z) \leftarrow T^i(x,y) \wedge T^i(y,z)$	
$T(x,z) \leftarrow \Delta^i_T(x,y) \land \Delta^i_T(y,z)$	
$T(x,z) \leftarrow \Delta^i_T(x,y) \wedge T^i(y,z)$	
$T(x,z) \leftarrow T^{i}(x,y) \land \Delta^{i}_{T}(y,z)$	

same as original rule restrict to new facts partially restrict to new facts partially restrict to new facts

What to choose?

slide 5 of 13

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Semi-Naive Evaluation (2)

Inferences that involve new and old facts are necessary:

	e(1 2) e(2 3	e(3,4) $e(4,5)$
(<i>R</i> 1)	$T(x, y) \leftarrow e(x, y)$	
(<i>R</i> 2)	$T(x,z) \leftarrow T(x,z)$	$y \land T(y, z)$
		T^0 ϕ
		$T_P^0 = \emptyset$
$\Delta_{T}^{1} = \{T(1,2), T(2,3), T(3,4), T$	$F(3,4), T(4,5)\}$	$T_P^1 = \Delta_T^1$
$\Delta_{T}^2 = \{T(1,3),T(2,4),T(3,5)\}$		$T_P^2 = T_P^1 \cup \Delta_{T}^2$
A^{3} (T(1 4) T(2 5) T(1 5))		T^{3} $T^{2} + \Lambda^{3}$

$\Delta_{T}^3 = \{T(1,4), T(2,5), T(1,5)\}$	$T_P^3 = T_P^2 \cup \Delta_T^3$
$\Delta_{T}^4 = \emptyset$	$T_P^4 = T_P^3 = T_P^\infty$

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To derive T(1, 4) in \Delta_T^3, we need to combine
T(1, 3) \in \Delta_T^2 with T(3, 4) \in \Delta_T^1 or T(1, 2) \in \Delta_T^1 with T(2, 4) \in \Delta_T^2
\rightarrow rule T(x, z) \leftarrow \Delta_T^i(x, y) \land \Delta_T^i(y, z) is not enough
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Semi-Naive Evaluation: Example

	e(1,2) $e(2,3)$ $e(3,4)$ $e(4,5)$	<i>i</i>)
(<i>R</i> 1)	$T(x, y) \leftarrow e(x, y)$	
(<i>R</i> 2.1)	$T(x,z) \leftarrow \Delta^i_T(x,y) \wedge T^i(y,z)$	
(R2.2')	$T(x,z) \leftarrow T^{i-1}(x,y) \land \Delta^i_T(y,z)$	

How many body matches do we need to iterate over?

$T_P^0 = \emptyset$	initialisation
$T_P^1 = \{T(1,2), T(2,3), T(3,4), T(4,5)\}$	$4 \times (R1)$
$T_P^2 = T_P^1 \cup \{T(1,3),T(2,4),T(3,5)\}$	$3 \times (R2.1)$
$T_P^3 = T_P^2 \cup \{T(1,4),T(2,5),T(1,5)\}$	$3\times(R2.1), 2\times(R2.2')$
$T_P^4 = T_P^3 = T_P^\infty$	$1\times(R2.1), 1\times(R2.2')$

In total, we considered 14 matches to derive 11 facts

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slide 9 of 13

Semi-Naive Evaluation (3)

Correct approach: consider only rule application that use at least one newly derived IDB atom

For example program:

	e(1,2) $e(2,3)$ $e(3,4)$ $e(3,4)$	(4, 5)
(<i>R</i> 1)	$T(x,y) \gets e(x,y)$	
(R2.1)	$T(x,z) \leftarrow \Delta^i_T(x,y) \land T^i(y,z)$	
(R2.2)	$T(x,z) \leftarrow T^{i}(x,y) \wedge \Delta^{i}_{T}(y,z)$	

There is still redundancy here: the matches for $T(x, z) \leftarrow \Delta_T^i(x, y) \land \Delta_T^i(y, z)$ are covered by both (*R*2.1) and (*R*2.2)

 \rightarrow replace (*R*2.2) by the following rule:

 $(R2.2') \qquad \mathsf{T}(x,z) \leftarrow \mathsf{T}^{i-1}(x,y) \land \Delta^{i}_{\mathsf{T}}(y,z)$

EDB atoms do not change, so their Δ would be \emptyset \rightarrow ignore such rules after the first iteration				
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Semi-Naive Evaluation: Full Definition				
In general, a rule of the form				
	$H(\vec{x}) \leftarrow e_1(\vec{y}_1) \land \ldots \land e_n(\vec{y}_n) \land$	$\wedge I_1(\vec{z}_1) \wedge I_2(\vec{z}_2) \wedge \ldots \wedge I_m(\vec{z}_m)$		
is transformed into <i>m</i> rules				
	$H(\vec{x}) \leftarrow e_1(\vec{y}_1) \land \ldots \land e_n(\vec{y}_n) \land \vec{x}$	$\Delta_{I_1}^i(\vec{z}_1) \wedge I_2^i(\vec{z}_2) \wedge \ldots \wedge I_m^i(\vec{z}_m)$		
	$H(\vec{x}) \leftarrow e_1(\vec{y}_1) \land \ldots \land e_n(\vec{y}_n) \land I$	$\Delta_{\mathbf{l}_{2}}^{i-1}(\vec{z}_{1}) \wedge \Delta_{\mathbf{l}_{2}}^{i}(\vec{z}_{2}) \wedge \ldots \wedge \mathbf{l}_{m}^{i}(\vec{z}_{m})$		

....

$\mathsf{H}(\vec{x}) \leftarrow \mathsf{e}_1(\vec{y}_1) \land \ldots \land \mathsf{e}_n(\vec{y}_n) \land \mathsf{I}_1^{i-1}(\vec{z}_1) \land \mathsf{I}_2^{i-1}(\vec{z}_2) \land \ldots \land \Delta^i_{\mathsf{I}_m}(\vec{z}_m)$

Advantages and disadvantages:

- Huge improvement over naive evaluation
- Some redundant computations remain (see example)
- · Some overhead for implementation (store level of entailments)

Summary and Outlook

Datalog queries can be evaluated bottom-up or top-down

Simplest practical bottom-up technique: semi-naive evaluation

Next question:

- Can we improve Datalog evaluation further?
- What about practical implementations?

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slide 13 of 13