# Science of Computational Logic 

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## Problem 3.1

We have three tiles, called $a, b$ and $c$, placed in a squared ordered field that can contain exactly four tiles, as illustrated in the figure below. Tile $X$ can be moved via the action move( $X$ ) either horizontally or vertically to occupy the adjacent free portion of the field. It cannot be moved diagonally and it cannot overlap another tile.


1. Formalize the actions move( $X$ ) in fluent calculus.
2. Formalize the state (A).
3. Give a plan that transforms state (A) to state (B).

## Problem 3.2

Consider the decision variant of the knapsack problem:
Given a set of items $\left\{i_{1}, \ldots, i_{n}\right\}$, each with a mass $m_{i} \in \mathbb{N}$ and a value $v_{i} \in \mathbb{N}$, can we include them in in a collection so that the total weight is less than $m$ and the total value is more than $v$ ?

Specify a planning problem that has a solution if and only if the above problem can be answered with 'yes'.

## Problem 3.3

Let $\mathcal{I}$ be an initial state containing, and $\mathcal{G}$ be a goal state and let $\mathcal{A}$ be the set of actions of Blocks World as specified in the lecture.

Specify a propositional formula $F_{n}$ such that $F$ is satisfiabile if and only if the planning problem has a solution of length $n$.

