Foundations of Databases and Query Languages

Exercise 2: First-order Queries

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Excercise 2.1 Express the queries from Exercise 1.1 as domain independent FO-queries.

Excercise 2.2 Let R be a table (relational instance) with attributes A and B. Use the construction from the lecture to express the following RA_{named} query as a $DI_{unnamed}$ query:

$$(\pi_A(R) \bowtie \pi_B(R)) - (R \bowtie (\delta_{A,B \rightarrow B,A}(R)))$$

Excercise 2.3 It was stated in the lecture that query mappings under named perspective can be translated into query mappings under unnamed perspective. Specify this translation.

Excercise 2.4 Complete the proof that $RA_{named} \subseteq DI_{unnamed}$ from the lecture by showing that the results of the transformation are (a) domain independent and (b) equivalent to the input query. In each case, show that the claimed property holds true for each case of the recursive construction under the assumption (induction hypothesis) that it has already been established for all subqueries. Use the mappings from Exercise 2.3 to compare named and unnamed results.

Excercise 2.5 Consider a binary predicate R and the $AD_{unnamed}$ query

$$\varphi[x, y] = \neg (R(x, y) \land R(y, x)).$$

Use the construction from the lecture to express it as an RA_{named} query.

Excercise 2.6 Complete the constructions for the proof of $AD \sqsubseteq RA$ given in the lecture.

- (a) Define the relational algebra expression $E_{a,adom}$, such that $E_{a,adom}(I) = \{\{a \mapsto c\} \mid c \in adom(I,q)\}$. Hint: Assume that the query and the database schema are known.
- (b) Define the expressions E_{φ} for $\varphi = \varphi_1 \vee \varphi_2$ and $\varphi = \forall y.\psi$ in terms of expressions that have already been defined in the lecture.
- (c) Give a direct definition for the expression E_{φ} for $\varphi = \varphi_1 \vee \varphi_2$.

Excercise 2.7 Use the function rr from the lecture to compute the set of range-restricted variables for the following FO queries:

- (a) $\exists y_{SID}, y_{Stop}, y_{To}.(Stops(y_{SID}, y_{Stop}, "true") \land Connect(y_{SID}, y_{To}, x_{Line}))[x_{Line}]$
- (b) $\neg Lines(x, "bus")[x]$
- (c) (Connect $(x_1, "42", "85") \vee Connect("57", x_2, "85"))[x_1, x_2]$
- (d) $\forall y.p(x,y)[x]$
- (e) $\exists x.(((p(x) \rightarrow q(c)) \rightarrow p(x)) \rightarrow p(x))$

Which of these queries is a safe-range query? Which of the queries is domain independent?