

FOUNDATIONS OF DATABASES AND QUERY LANGUAGES

Lecture 11: Implementation and Optimisation of Datalog

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TU Dresden, 29 June 2015

Review: Datalog Expressivity and Complexity

A rule-based recursive query language

```
\begin{aligned} & \text{father(alice, bob)} \\ & \text{mother(alice, carla)} \\ & & \text{Parent}(x,y) \leftarrow \text{father}(x,y) \\ & & \text{Parent}(x,y) \leftarrow \text{mother}(x,y) \\ & \text{SameGeneration}(x,x) \\ & \text{SameGeneration}(x,y) \leftarrow \text{Parent}(x,v) \land \text{Parent}(y,w) \land \text{SameGeneration}(v,w) \end{aligned}
```

Datalog is more complex than FO query answering:

- $\bullet \ \mathrm{ExpTime}\text{-}\text{complete}$ for query and combined complexity
- P-complete for data complexity

Datalog cannot express all query mappings in P but semipositive Datalog with a successor ordering can

Overview

- 1. Introduction | Relational data model
- 2. First-order queries
- 3. Complexity of guery answering
- 4. Complexity of FO query answering
- 5. Conjunctive queries
- 6. Tree-like conjunctive queries
- 7. Query optimisation
- 8. Conjunctive Query Optimisation / First-Order Expressiveness
- 9. First-Order Expressiveness / Introduction to Datalog
- 10. Expressive Power and Complexity of Datalog
- 11. Implementation techniques for Datalog
- 12. Path queries
- 13. Constraints
- 14. Outlook: database theory in practice

See course homepage [⇒ link] for more information and materials

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slide 2 of 29

Datalog Implementation and Optimisation

How can Datalog query answering be implemented? How can Datalog queries be optimised?

Recall: static query optimisation

- Query equivalence
- Query emptiness
- Query containment

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ightarrow all undecidable for FO queries, but decidable for (U)CQs

Learning from CQ Containment?

How did we manage to decide the question $Q_1 \stackrel{?}{\sqsubseteq} Q_2$ for conjunctive queries Q_1 and Q_2 ?

Key ideas were:

- We want to know if all situations where Q_1 matches are also matched by Q_2 .
- We can simply view Q_1 as a database I_{Q_1} : the most general database that Q_1 can match to
- Containment $Q_1 \stackrel{?}{\sqsubseteq} Q_2$ holds if Q_2 matches the database I_{Q_1} .

 \rightarrow decidable in NP

A CQ $Q[x_1, ..., x_n]$ can be expressed as a Datalog query with a single rule $Ans(x_1, ..., x_n) \leftarrow Q$

→ Could we apply a similar technique to Datalog?

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slide 5 of 29

Example: Rule Entailment

Let *P* be the program

Ancestor(
$$x, y$$
) \leftarrow parent(x, y)
Ancestor(x, z) \leftarrow parent(x, y) \wedge Ancestor(y, z)

and consider the rule $\mathsf{Ancestor}(x,z) \leftarrow \mathsf{parent}(x,y) \land \mathsf{parent}(y,z).$

Then $I_{\mathsf{parent}(x,y) \land \mathsf{parent}(y,z)} = \{\mathsf{parent}(c_x,c_y), \mathsf{parent}(c_y,c_z)\}$ (abbr. as I). We can compute $I_p^\infty(I)$:

$$\begin{split} T_P^0(I) &= I \\ T_P^1(I) &= \{\mathsf{Ancestor}(c_x, c_y), \mathsf{Ancestor}(c_y, c_z)\} \cup I \\ T_P^2(I) &= \{\mathsf{Ancestor}(c_x, c_z) \cup T_P^1(I) \\ T_P^3(I) &= T_P^2(I) = T_P^\infty(I) \end{split}$$

Therefore, Ancestor $(x, z)^c$ = Ancestor $(c_x, c_z) \in T_P^{\infty}(I)$, so P entails Ancestor $(x, z) \leftarrow \text{parent}(x, y) \land \text{parent}(y, z)$.

Checking Rule Entailment

The containment decision procedure for CQs suggests a procedure for single Datalog rules:

- Consider a Datalog program P and a rule $H \leftarrow B_1 \wedge \ldots \wedge B_n$.
- Define a database $I_{B_1 \wedge ... \wedge B_n}$ as for CQs:
 - For every variable x in $H \leftarrow B_1 \wedge ... \wedge B_n$, we introduce a fresh constant c_x , not used anywhere yet
 - We define H^c to be the same as H but with each variable x replaced by c_x ; similarly we define B_i^c for each $1 \le i \le n$
 - The database $\mathcal{I}_{B_1 \wedge ... \wedge B_n}$ contains exactly the facts B_i^c $(1 \le i \le n)$
- Now check if $H^c \in T_p^{\infty}(\mathcal{I}_{B_1 \wedge ... \wedge B_n})$:
 - − If no, then there is a database on which $H \leftarrow B_1 \land ... \land B_n$ produces an entailment that P does not produce.
 - If yes, then $P \models H \leftarrow B_1 \land \ldots \land B_n$

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slide 6 of 29

Deciding Datalog Containment?

Idea for two Datalog programs P_1 and P_2 :

- If $P_2 \models P_1$, then every entailment of P_1 is also entailed by P_2
- In particular, this means that P_1 is contained in P_2
- We have $P_2 \models P_1$ if $P_2 \models H \leftarrow B_1 \land \ldots \land B_n$ for every rule $H \leftarrow B_1 \land \ldots \land B_n \in P_1$
- We can decide $P_2 \models H \leftarrow B_1 \land \ldots \land B_n$.

Can we decide Datalog containment this way?

→ No! In fact, Datalog containment is undecidable. What's wrong?

Implication Entailment vs. Datalog Entailment

$$P_1:$$
 $P_2:$ $B(x,y) \leftarrow \mathsf{parent}(x,y)$ $B(x,y) \leftarrow \mathsf{parent}(x,y)$ $A(x,z) \leftarrow \mathsf{parent}(x,y) \land A(y,z)$ $B(x,z) \leftarrow \mathsf{parent}(x,y) \land B(y,z)$

Consider the Datalog queries $\langle A, P_1 \rangle$ and $\langle B, P_2 \rangle$:

- Clearly, $\langle A, P_1 \rangle$ and $\langle B, P_2 \rangle$ are equivalent (and mutually contained in each other).
- However, P_2 entails no rule of P_1 and P_1 entails no rule of P_2 .

→ IDB predicates do not matter in Datalog, but predicate names matter in first-order implications

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slide 9 of 29

First-Order vs. Second-Order Logic

A Datalog program looks like a set of first-order implications, but it has a second-order semantics

We have already seen that Datalog can express things that are impossible to express in FO gueries – that's why we introduced it!¹

Consequences for query optimisation:

- Entailment between sets of first-order implications is decidable (shown above)
- Containment between Datalog gueries is not decidable (shown next)

Datalog as Second-Order Logic

Datalog is a fragment of second-order logic: IDB pred's are like variables that can take any set of tuples as value!

Example: the query $\langle A, P_1 \rangle$ can be expressed by the formula

$$\forall \mathsf{A}. \left(\begin{array}{ccc} \forall x, y. \mathsf{A}(x,y) & \leftarrow \mathsf{parent}(x,y) & \land \\ \forall x, y, z. \mathsf{A}(x,z) & \leftarrow \mathsf{parent}(x,y) \land \mathsf{A}(y,z) \end{array} \right) \rightarrow \mathsf{A}(v,w)$$

- This is a formula with two free variables v and w.
 - → query with two result variables
- Intuitive semantics: " $\langle c, d \rangle$ is a query result if A(c, d) holds for all possible values of A that satisfy the rules"
 - → Datalog semantics in other words

We can express any Datalog query like this, with one second-order variable per IDB predicate.

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slide 10 of 29

Undecidability of Datalog Query Containment

A classical undecidable problem: Post Correspondence Problem

- Input: two lists of words $\alpha_1, \ldots, \alpha_n$ and β_1, \ldots, β_n
- Output: "yes" if there is a sequence of indices $i_1, i_2, i_3, \ldots, i_m$ such that $\alpha_{i_1}\alpha_{i_2}\alpha_{i_3}\cdots\alpha_{i_m}=\beta_{i_1}\beta_{i_2}\beta_{i_3}\cdots\beta_{i_m}$.

→ we will reduce PCP to Datalog containment

We need to define Datalog programs that work on databases that encode words:

- We represent words by chains of binary predicates
- Binary EDB predicates represent a letters
- For each letter σ , we use a binary EDB predicate letter $[\sigma]$
- We assume that the words α_i have the form $a_1^i \cdots a_{|\alpha|}^i$, and that the words β_i have the form $b_1^i \cdots b_{|\beta_i|}^i$

¹Possible confusion when comparing of FO and Datalog: entailments of first-order implications agree with answers of Datalog queries, so it seems we can break the FO locality restrictions; but query answering is model checking not entailment; FO model checking is much weaker than second-order model checking Foundations of Databases and Query Languages

Solving PCP with Datalog Containment

A program P_1 to recognise potential PCP solutions.

Rules to recognise words α_i and β_i for every $i \in \{1, ..., m\}$:

$$\begin{aligned} &\mathsf{A}_i(x_0,x_{|\alpha_i|}) \leftarrow \mathsf{letter}[a_1^i](x_0,x_1) \wedge \ldots \wedge \mathsf{letter}[a_{|\alpha_i|}^i](x_{|\alpha_i|-1},x_{|\alpha_i|}) \\ &\mathsf{B}_i(x_0,x_{|\beta_i|}) \leftarrow \mathsf{letter}[b_1^i](x_0,x_1) \wedge \ldots \wedge \mathsf{letter}[b_{|\beta_i|}^i](x_{|\beta_i|-1},x_{|\beta_i|}) \end{aligned}$$

Rules to check for synchronised chairs (for all $i \in \{1, ..., m\}$):

$$\begin{aligned} \mathsf{PCP}(x,y_1,y_2) &\leftarrow A_i(x,y_1) \land B_i(x,y_2) \\ \mathsf{PCP}(x,z_1,z_2) &\leftarrow \mathsf{PCP}(x,y_1,y_2) \land A_i(y_1,z_1) \land B_i(y_2,z_2) \\ \mathsf{Accept}() &\leftarrow \mathsf{PCP}(x,z,z) \end{aligned}$$

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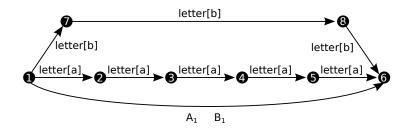
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slide 13 of 29

Solving PCP with Datalog Containment (3)

Example: $\alpha_1 = aaaaa$, $\beta_1 = bbb$

Problem: P₁ also accepts some unintended cases



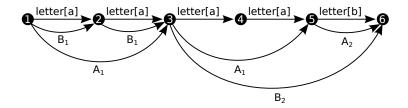
Additional IDB facts that are derived:

PCP(1,6,6) Accept()

Solving PCP with Datalog Containment (2)

Example: $\alpha_1 = aa$, $\beta_1 = a$, $\alpha_2 = b$, $\beta_2 = aab$

Example for an indented database and least model (selected parts):



Additional IDB facts that are derived (among others):

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slide 14 of 29

Solving PCP with Datalog Containment (4)

Solution: specify a program P_2 that recognises all unwanted cases

 P_2 consists of the following rules (for all letters σ, σ'):

$$\begin{split} \mathsf{EP}(x,x) \leftarrow \\ \mathsf{EP}(y_1,y_2) \leftarrow \mathsf{EP}(x_1,x_2) \wedge \mathsf{letter}[\sigma](x_1,y_1) \wedge \mathsf{letter}[\sigma](x_2,y_2) \\ \mathsf{Accept}() \leftarrow \mathsf{EP}(x_1,x_2) \wedge \mathsf{letter}[\sigma](x_1,y_1) \wedge \mathsf{letter}[\sigma'](x_2,y_2) \quad \sigma \neq \sigma' \\ \mathsf{NEP}(x_1,y_2) \leftarrow \mathsf{EP}(x_1,x_2) \wedge \mathsf{letter}[\sigma](x_2,y_2) \\ \mathsf{NEP}(x_1,y_2) \leftarrow \mathsf{NEP}(x_1,x_2) \wedge \mathsf{letter}[\sigma](x_2,y_2) \\ \mathsf{Accept}() \leftarrow \mathsf{NEP}(x,x) \end{split}$$

Intuition:

- EP defines equal paths (forwards, from one starting point)
- NEP defines paths of different length (from one starting point to the same end point)

 \rightarrow P_2 accepts all databases with distinct parallel paths

Solving PCP with Datalog Containment (5)

What does it mean if $\langle Accept, P_1 \rangle$ is contained in $\langle Accept, P_2 \rangle$?

The following are equivalent:

- All databases with potential PCP solutions also have distinct parallel paths.
- Databases without distinct parallel paths have no PCP solutions.
- Linear databases (words) have no PCP solutions.
- The answer to the PCP is "no".
- → If we could decide Datalog containment, we could decide PCP

Theorem

Containment and equivalence of Datalog queries are undecidable.

(Note that emptiness of Datalog queries is trivial)

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slide 17 of 29

Implementing Datalog

FO gueries (and thus also CQs and UCQs) are supported by almost all DMBS

→ many specific implementation and optimisation techniques

How can Datalog gueries be answered in practice?

→ techniques for dealing with recursion in DBMS query answering

There are two major paradigms for answering recursive queries:

- Bottom-up: derive conclusions by applying rules to given facts
- Top-down: search for proofs to infer results given query

Implementation of Datalog

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slide 18 of 29

Computing Datalog Query Answers Bottom-Up

We already saw a way to compute Datalog answers bottom-up: the step-wise computation of the consequence operator T_P

Bottom-up computation is known under many names:

- Forward-chaining since rules are "chained" from premise to conclusion (common in logic programming)
- Materialisation since inferred facts are stored ("materialised") (common in databases)
- Saturation since the input database is "saturated" with inferences (common in theorem proving)
- Deductive closure since we "close" the input under entailments (common in formal logic)

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Naive Evaluation of Datalog Queries

A direct approach for computing T_P^{∞}

```
T_{P}^{0} := \emptyset
01
        i := 0
02
03
         repeat:
                 T_{p}^{i+1} := \emptyset
04
                 for H \leftarrow B_1 \wedge \ldots \wedge B_\ell \in P:
05
06
                          for \theta \in B_1 \wedge \ldots \wedge B_\ell(T_p^i):
                                  T_{p}^{i+1} := T_{p}^{i+1} \cup \{H\theta\}
07
                 i := i + 1
80
        until T_{p}^{i-1} = T_{p}^{i}
09
        return T_p^i
10
```

Notation for line 06/07:

- a substitution θ is a mapping from variables to database elements
- for a formula F, we write $F\theta$ for the formula obtained by replacing each free variable x in F by $\theta(x)$
- for a CQ Q and database I, we write $\theta \in Q(I)$ if $I \models Q\theta$

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slide 21 of 29

Less Naive Evaluation Strategies

Does it really matter how often we consider a rule match? After all, each fact is added only once ...

In practice, finding applicable rules takes significant time, even if the conclusion does not need to be added – iteration takes time! \rightarrow huge potential for optimisation

Observation:

we derive the same conclusions over and over again in each step

Idea: apply rules only to newly derived facts

→ semi-naive evaluation

What's Wrong with Naive Evaluation?

An example Datalog program:

$$e(1,2) \quad e(2,3) \quad e(3,4) \quad e(4,5)$$
 $(R1) \quad T(x,y) \leftarrow e(x,y)$
 $(R2) \quad T(x,z) \leftarrow T(x,y) \wedge T(y,z)$

How many body matches do we need to iterate over?

$$\begin{split} T_P^0 &= \emptyset & \text{initialisation} \\ T_P^1 &= \{\mathsf{T}(1,2),\mathsf{T}(2,3),\mathsf{T}(3,4),\mathsf{T}(4,5)\} & 4 \text{ matches for } (R1) \\ T_P^2 &= T_P^1 \cup \{\mathsf{T}(1,3),\mathsf{T}(2,4),\mathsf{T}(3,5)\} & 4 \times (R1) + 3 \times (R2) \\ T_P^3 &= T_P^2 \cup \{\mathsf{T}(1,4),\mathsf{T}(2,5),\mathsf{T}(1,5)\} & 4 \times (R1) + 8 \times (R2) \\ T_P^4 &= T_P^3 = T_P^\infty & 4 \times (R1) + 10 \times (R2) \end{split}$$

In total, we considered 37 matches to derive 11 facts

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slide 22 of 29

Semi-Naive Evaluation

The computation yields sets $T_P^0 \subseteq T_P^1 \subseteq T_P^2 \subseteq \ldots \subseteq T_P^\infty$

- For an IDB predicate R, let \mathbf{R}^i be the "predicate" that contains exactly the R-facts in T_P^i
- For $i \leq 1$, let Δ_{R}^{i} be the collection of facts $R^{i} \setminus R^{i-1}$

We can restrict rules to use only some computations. Some options for the computation in step i + 1:

$$T(x, z) \leftarrow T^i(x, y) \wedge T^i(y, z)$$
 same as original rule $T(x, z) \leftarrow \Delta^i_T(x, y) \wedge \Delta^i_T(y, z)$ restrict to new facts $T(x, z) \leftarrow \Delta^i_T(x, y) \wedge T^i(y, z)$ partially restrict to new facts $T(x, z) \leftarrow T^i(x, y) \wedge \Delta^i_T(y, z)$ partially restrict to new facts

What to chose?

Semi-Naive Evaluation (2)

Inferences that involve new and old facts are necessary:

$$e(1,2)$$
 $e(2,3)$ $e(3,4)$ $e(4,5)$

(R1)
$$\mathsf{T}(x,y) \leftarrow \mathsf{e}(x,y)$$

(R2)
$$\mathsf{T}(x,z) \leftarrow \mathsf{T}(x,y) \wedge \mathsf{T}(y,z)$$

$$\begin{split} T_P^0 &= \emptyset \\ \Delta_\mathsf{T}^1 &= \{\mathsf{T}(1,2), \mathsf{T}(2,3), \mathsf{T}(3,4), \mathsf{T}(3,4), \mathsf{T}(4,5)\} & T_P^1 &= \Delta_\mathsf{T}^1 \\ \Delta_\mathsf{T}^2 &= \{\mathsf{T}(1,3), \mathsf{T}(2,4), \mathsf{T}(3,5)\} & T_P^2 &= T_P^1 \cup \Delta_\mathsf{T}^2 \\ \Delta_\mathsf{T}^3 &= \{\mathsf{T}(1,4), \mathsf{T}(2,5), \mathsf{T}(1,5)\} & T_P^3 &= T_P^2 \cup \Delta_\mathsf{T}^3 \\ \Delta_\mathsf{T}^4 &= \emptyset & T_P^4 &= T_P^3 &= T_P^\infty \end{split}$$

To derive T(1, 4) in Δ_{T}^3 , we need to combine T(1, 3) $\in \Delta_{\mathsf{T}}^2$ with T(3, 4) $\in \Delta_{\mathsf{T}}^1$ or T(1, 2) $\in \Delta_{\mathsf{T}}^1$ with T(2, 4) $\in \Delta_{\mathsf{T}}^2$ \sim rule T(x, z) $\leftarrow \Delta_{\mathsf{T}}^i(x, y) \wedge \Delta_{\mathsf{T}}^i(y, z)$ is not enough

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slide 25 of 29

Semi-Naive Evaluation: Example

$$\begin{array}{cccc} & & \mathsf{e}(1,2) & \mathsf{e}(2,3) & \mathsf{e}(3,4) & \mathsf{e}(4,5) \\ (R1) & & \mathsf{T}(x,y) \leftarrow \mathsf{e}(x,y) \\ (R2.1) & & \mathsf{T}(x,z) \leftarrow \Delta_\mathsf{T}^i(x,y) \wedge \mathsf{T}^i(y,z) \\ (R2.2') & & \mathsf{T}(x,z) \leftarrow \mathsf{T}^{i-1}(x,y) \wedge \Delta_\mathsf{T}^i(y,z) \end{array}$$

How many body matches do we need to iterate over?

$$\begin{split} T_P^0 &= \emptyset & \text{initialisation} \\ T_P^1 &= \{\mathsf{T}(1,2), \mathsf{T}(2,3), \mathsf{T}(3,4), \mathsf{T}(4,5)\} & 4 \times (R1) \\ T_P^2 &= T_P^1 \cup \{\mathsf{T}(1,3), \mathsf{T}(2,4), \mathsf{T}(3,5)\} & 3 \times (R2) \\ T_P^3 &= T_P^2 \cup \{\mathsf{T}(1,4), \mathsf{T}(2,5), \mathsf{T}(1,5)\} & 5 \times (R2) \\ T_P^4 &= T_P^3 = T_P^\infty & 2 \times (R2) \end{split}$$

In total, we considered 14 matches to derive 11 facts

Semi-Naive Evaluation (3)

Correct approach: consider only rule application that use at least one newly derived IDB atom

For example program:

$$e(1,2)$$
 $e(2,3)$ $e(3,4)$ $e(4,5)$

(R1)
$$\mathsf{T}(x,y) \leftarrow \mathsf{e}(x,y)$$

(R2.1)
$$\mathsf{T}(x,z) \leftarrow \Delta^i_\mathsf{T}(x,y) \wedge \mathsf{T}^i(y,z)$$

$$(R2.2) \qquad \mathsf{T}(x,z) \leftarrow \mathsf{T}^i(x,y) \wedge \Delta^i_\mathsf{T}(y,z)$$

There is still redundancy here: the matches for $T(x,z) \leftarrow \Delta_T^i(x,y) \wedge \Delta_T^i(y,z)$ are covered by both (R2.1) and (R2.2) \rightarrow replace (R2.2) by the following rule:

$$(R2.2')$$
 $\mathsf{T}(x,z) \leftarrow \mathsf{T}^{i-1}(x,y) \wedge \Delta^i_\mathsf{T}(y,z)$

EDB atoms do not change, so their Δ would be \emptyset \rightarrow ignore such rules after the first iteration

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slide 26 of 29

Semi-Naive Evaluation: Full Definition

In general, a rule of the form

$$\mathsf{H}(\vec{x}) \leftarrow \mathsf{e}_1(\vec{y}_1) \wedge \ldots \wedge \mathsf{e}_n(\vec{y}_n) \wedge \mathsf{I}_1(\vec{z}_1) \wedge \mathsf{I}_2(\vec{z}_2) \wedge \ldots \wedge \mathsf{I}_m(\vec{z}_m)$$

is transformed into m rules

$$\begin{aligned} \mathsf{H}(\vec{x}) &\leftarrow \mathsf{e}_1(\vec{y}_1) \wedge \ldots \wedge \mathsf{e}_n(\vec{y}_n) \wedge \Delta^i_{\mathsf{l}_1}(\vec{z}_1) \wedge \mathsf{l}^i_2(\vec{z}_2) \wedge \ldots \wedge \mathsf{l}^i_m(\vec{z}_m) \\ \mathsf{H}(\vec{x}) &\leftarrow \mathsf{e}_1(\vec{y}_1) \wedge \ldots \wedge \mathsf{e}_n(\vec{y}_n) \wedge \mathsf{l}^{i-1}_1(\vec{z}_1) \wedge \Delta^i_{\mathsf{l}_2}(\vec{z}_2) \wedge \ldots \wedge \mathsf{l}^i_m(\vec{z}_m) \\ &\cdots \\ \mathsf{H}(\vec{x}) &\leftarrow \mathsf{e}_1(\vec{y}_1) \wedge \ldots \wedge \mathsf{e}_n(\vec{y}_n) \wedge \mathsf{l}^{i-1}_1(\vec{z}_1) \wedge \mathsf{l}^{i-1}_2(\vec{z}_2) \wedge \ldots \wedge \Delta^i_{\mathsf{l}}(\vec{z}_m) \end{aligned}$$

Advantages and disadvantages:

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- Huge improvement over naive evaluation
- Some redundant computations remain (see example)
- Some overhead for implementation (store level of entailments)

Summary and Outlook

Perfect Datalog optimisation is impossible

- same situation as for FO queries
- but for somewhat different reasons

Datalog queries can be evaluated bottom-up or top-down

Simplest practical bottom-up technique: semi-naive evaluation

Next topics:

- More on Datalog implementation
- Further query languages
- Applications

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slide 29 of 29